

**CIV2802 – Sistemas Gráficos para Engenharia**  
2025.1

# **Modelagem Geométrica de Sólidos**



**Luiz Fernando Martha**

**André Pereira**



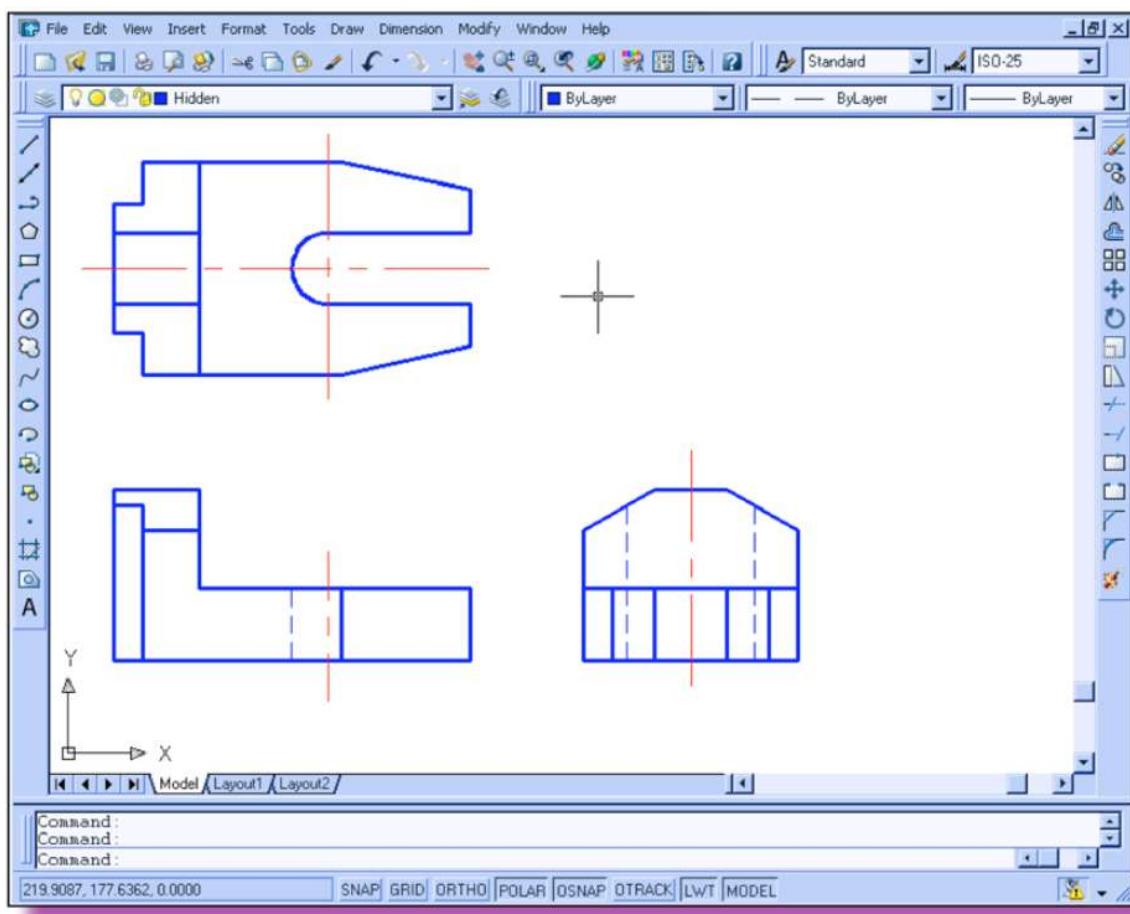
# Conteúdo

- Motivação
- Modelagem de Sólidos
- Modelagem em Engenharia
- Modelagem Geométrica
- Modelagem Paramétrica

# Desenho

## Abordagem Tradicional - Primeira Geração de CAD (Computer Aided Design)

[SHIH2006]



As primeiras gerações de CAD são apenas em 2D, basicamente substituindo lápis e papel.

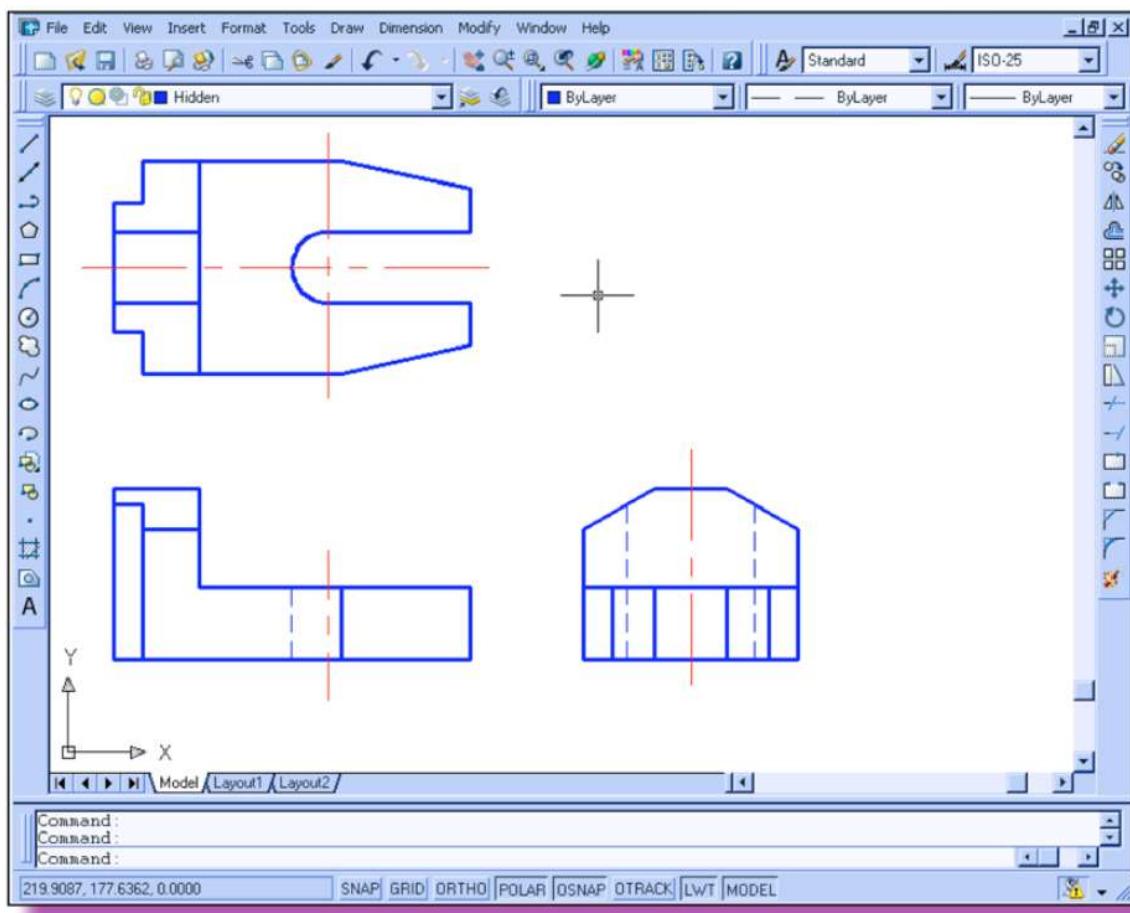
O tão popular AutoCAD, distribuído pela primeira vez em 1981, ganhou popularidade e é um dos principais sistemas CAD.

Ainda hoje, muitas empresas utilizam 2D CAD para criar projetos.

# Desenho

## Abordagem Tradicional - Primeira Geração de CAD (Computer Aided Design)

[SHIH2006]

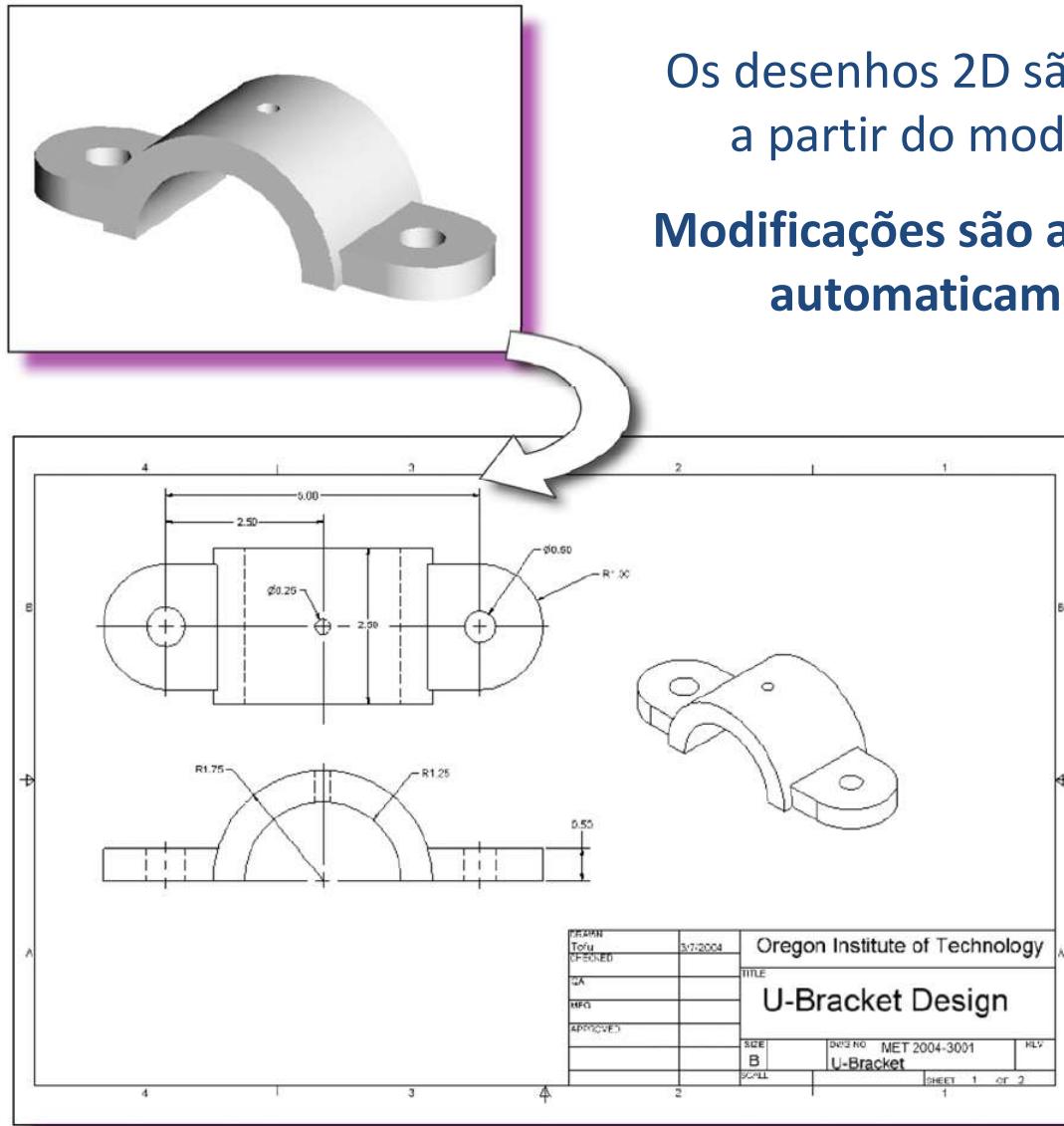


Esse tipo de abordagem requer o conhecimento das dimensões reais de projeto, sendo portanto pouco flexível.

Note na Figura que :

- (1)** A criação dessas vistas requer o conhecimento das dimensões.
- (2)** Cada uma das três vistas é criada e editada independentemente das outras.

# Modelagem de Sólidos

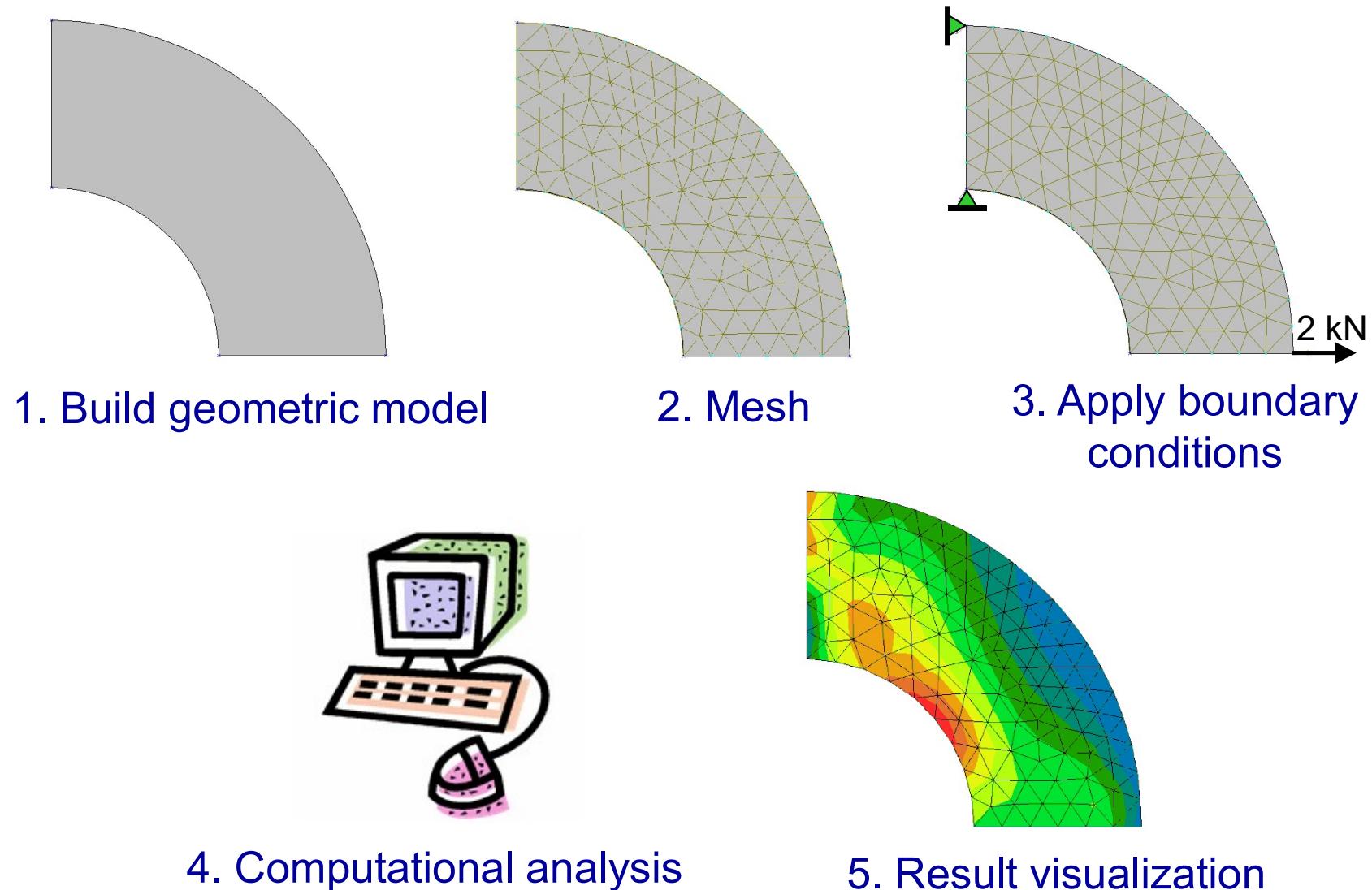


Os desenhos 2D são gerados  
a partir do modelo 3D.

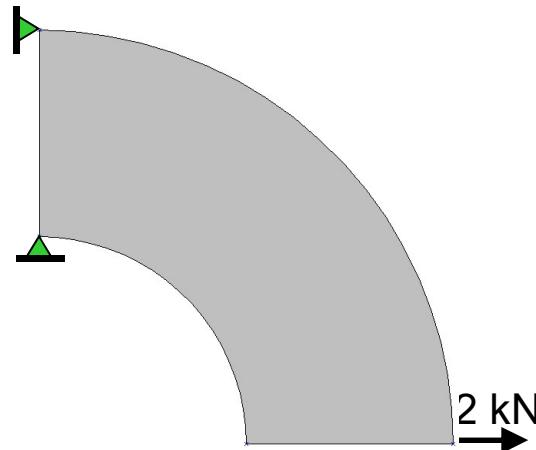
Modificações são atualizadas  
automaticamente.

# **Modelagem em Engenharia**

# Traditional FE Simulation Process



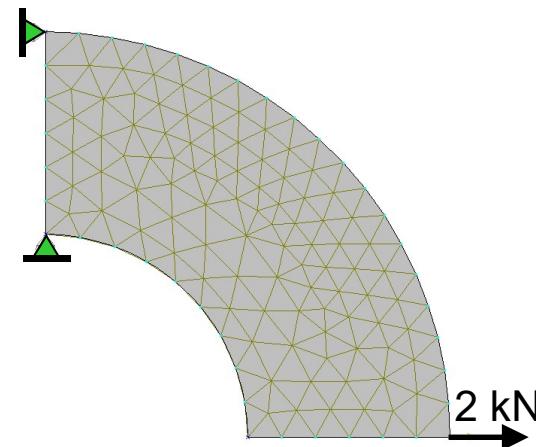
# Geometry-based Simulation Process



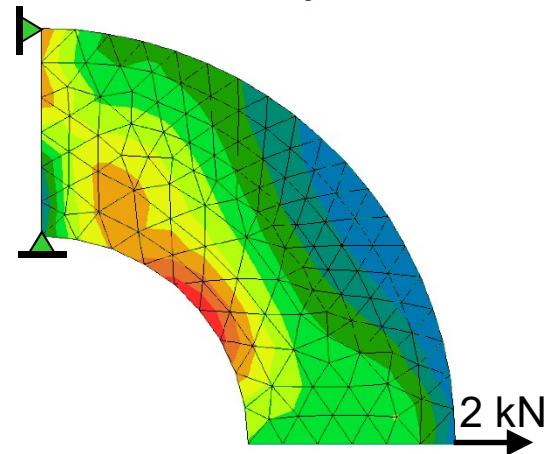
1. Geometric modelling, apply attributes and boundary conditions



3. Computational analysis



2. FE mesh generation, apply boundary conditions



4. Result visualization

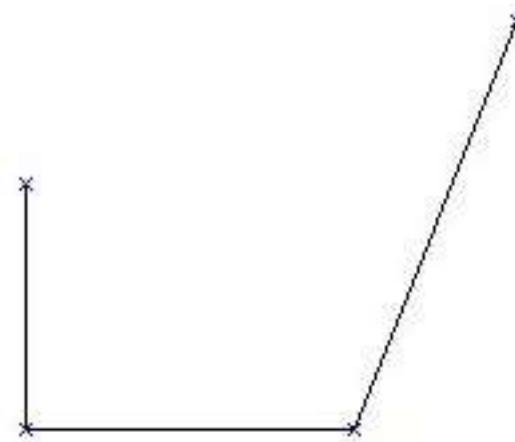
# **Construction of a Simple FE Model**



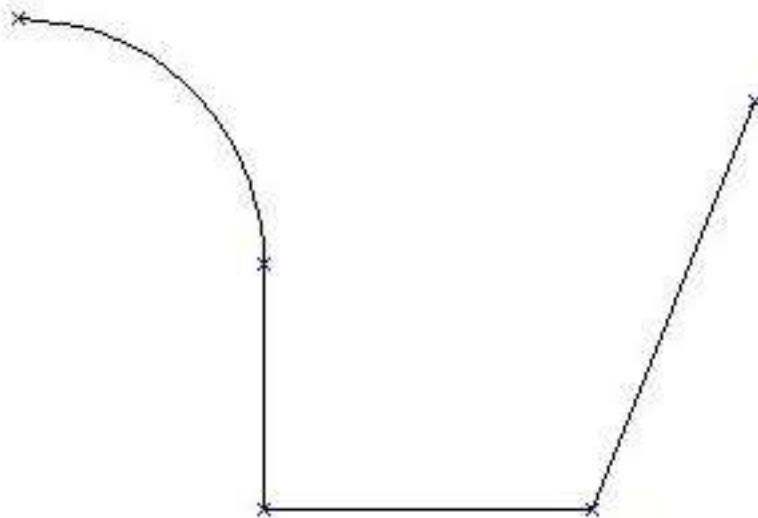
# **Construction of a Simple FE Model**



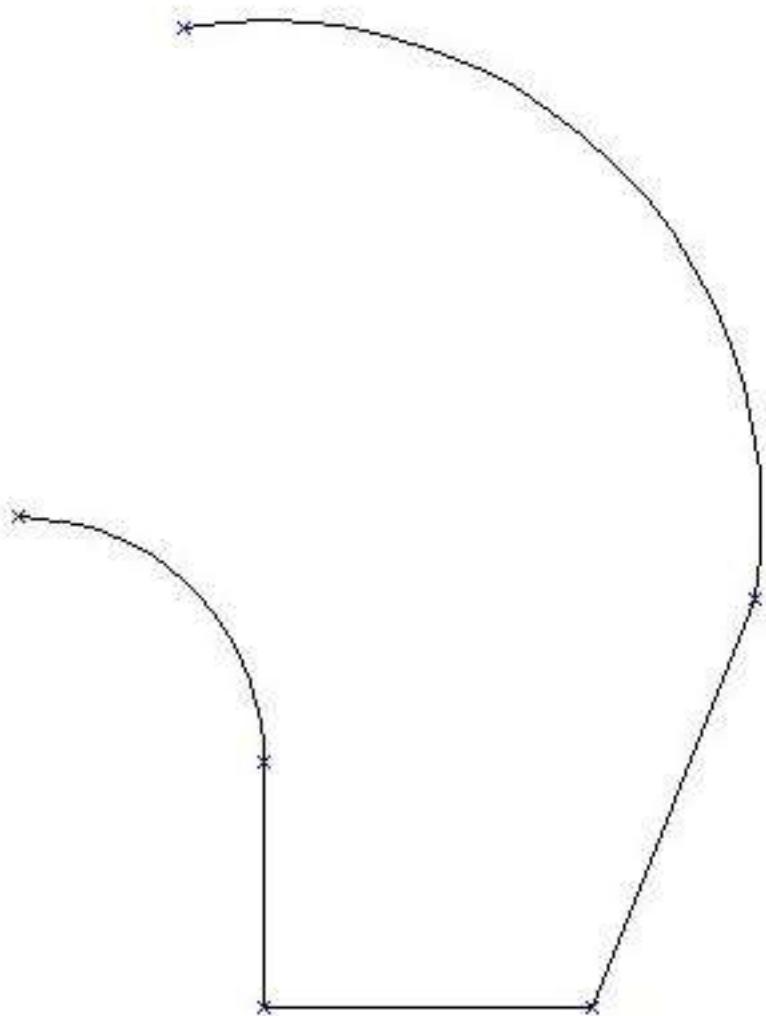
# **Construction of a Simple FE Model**



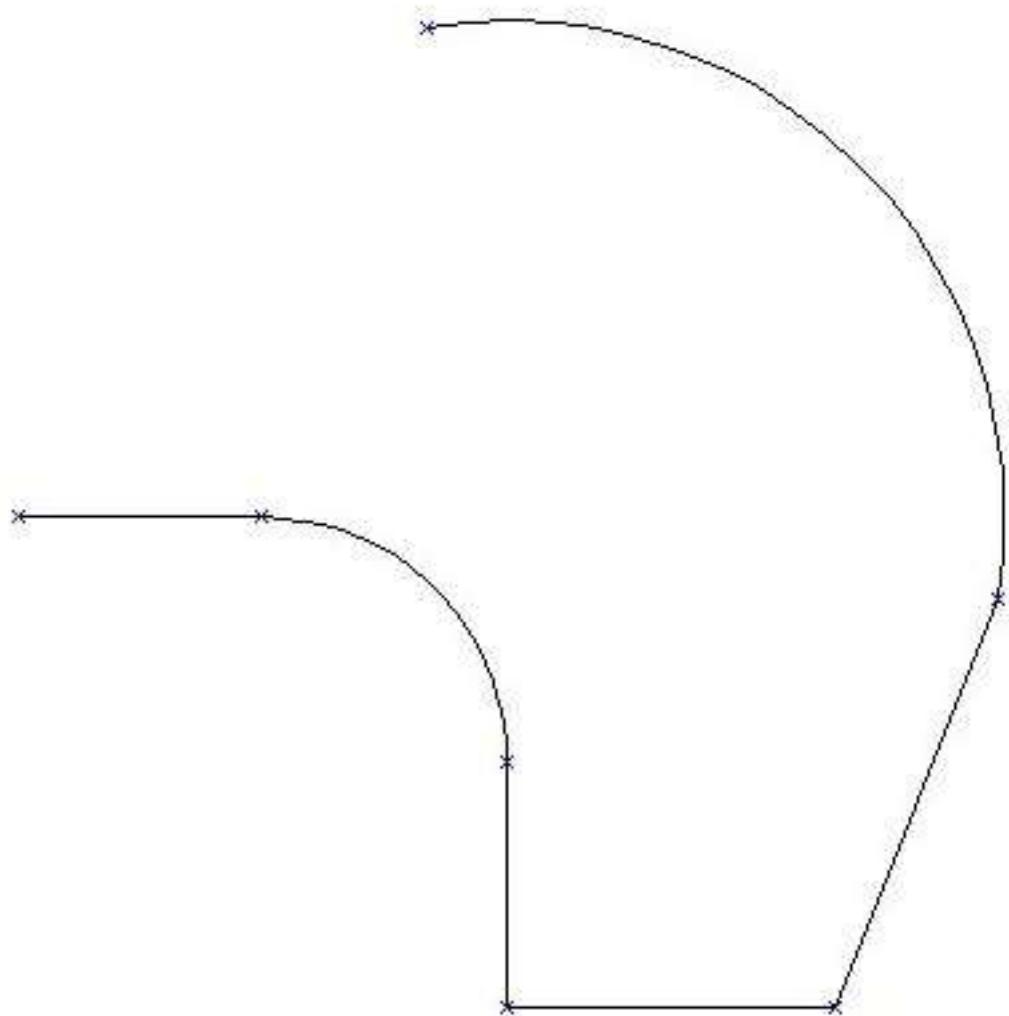
# **Construction of a Simple FE Model**



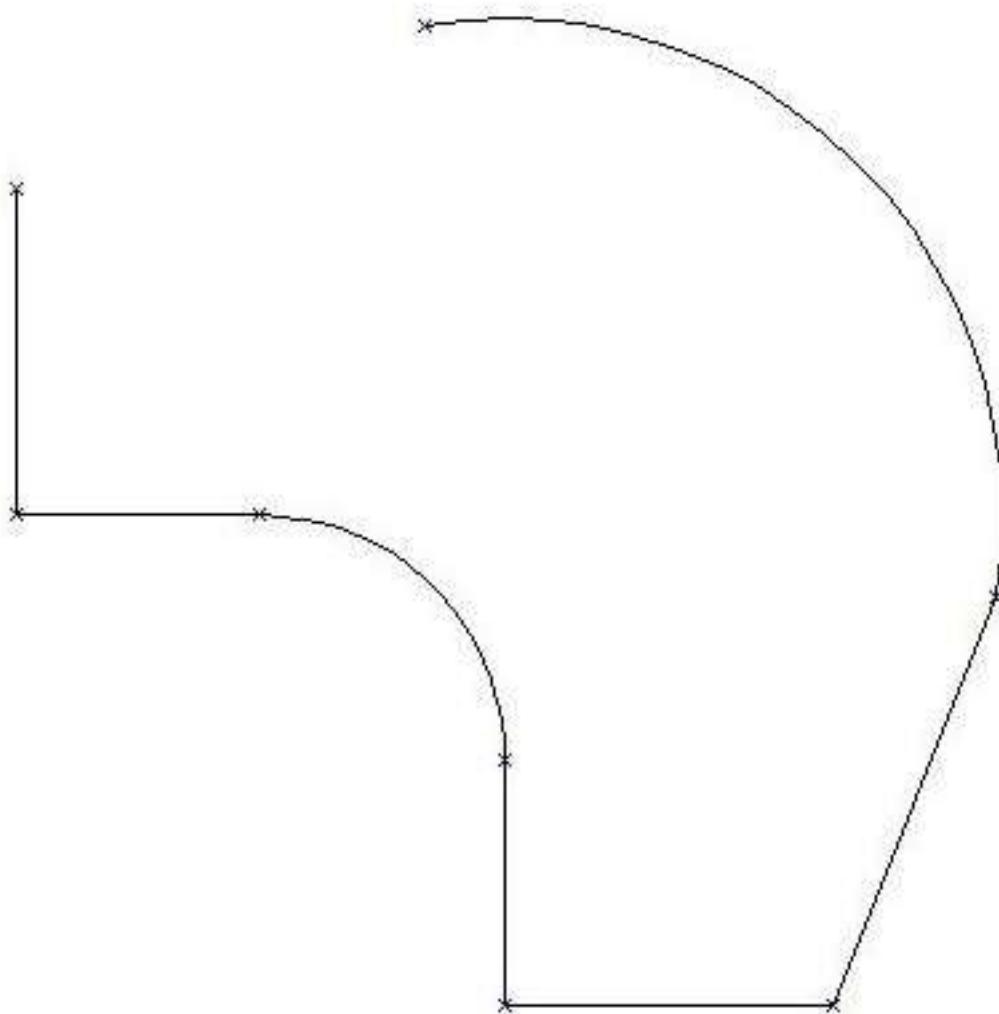
# **Construction of a Simple FE Model**



## **Construction of a Simple FE Model**

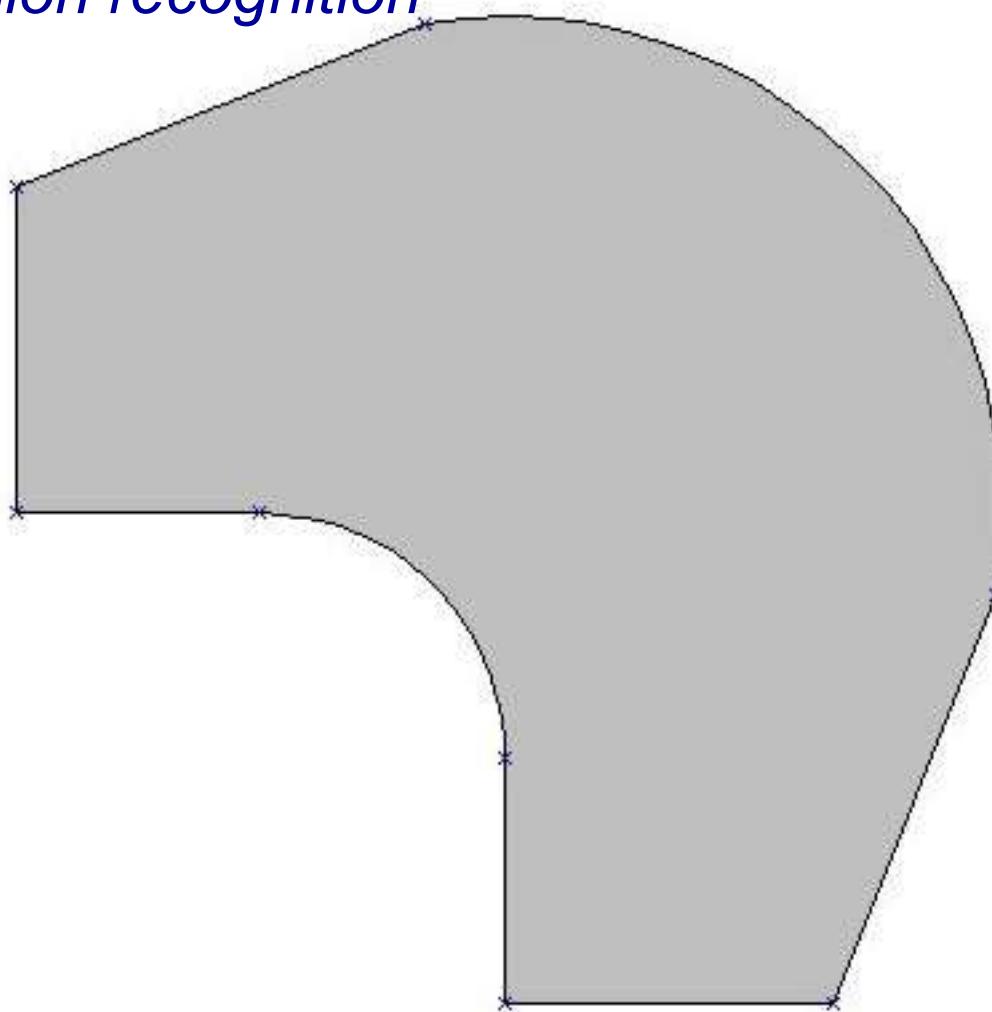


## **Construction of a Simple FE Model**

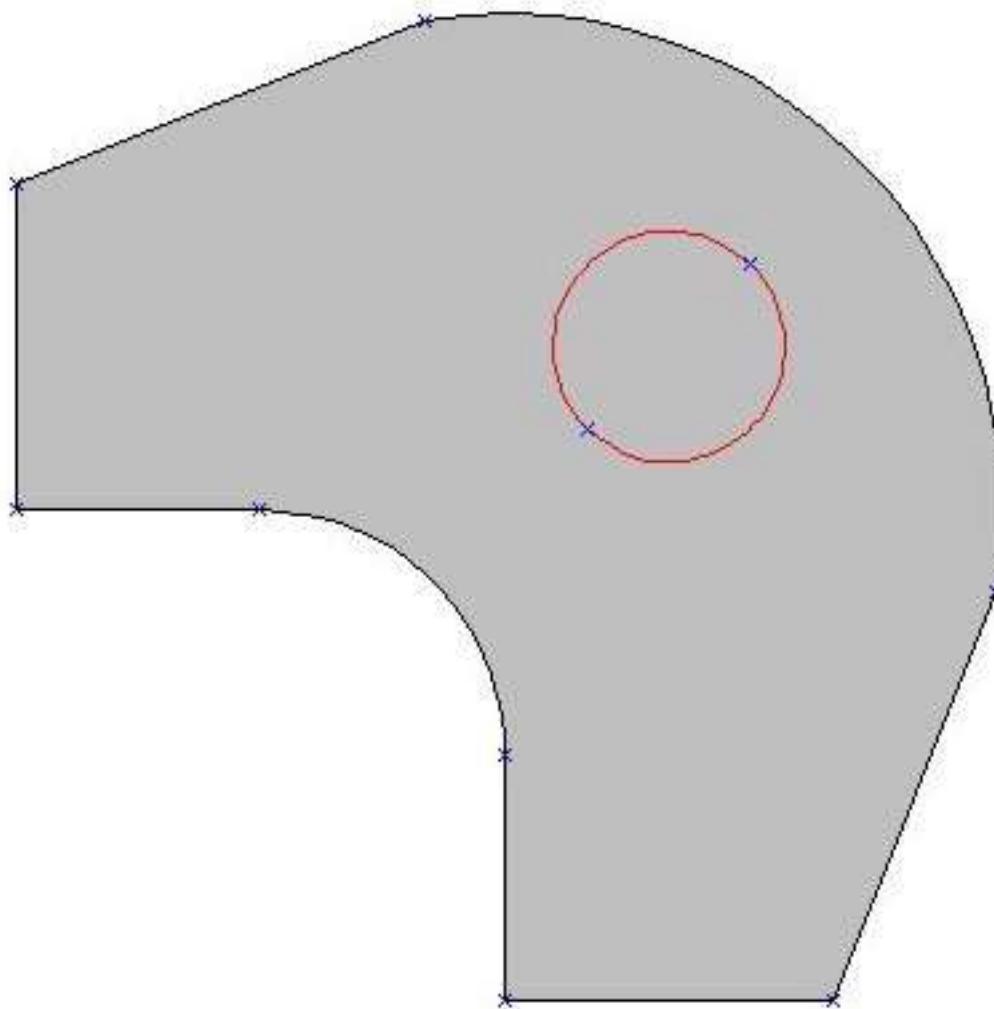


## **Construction of a Simple FE Model**

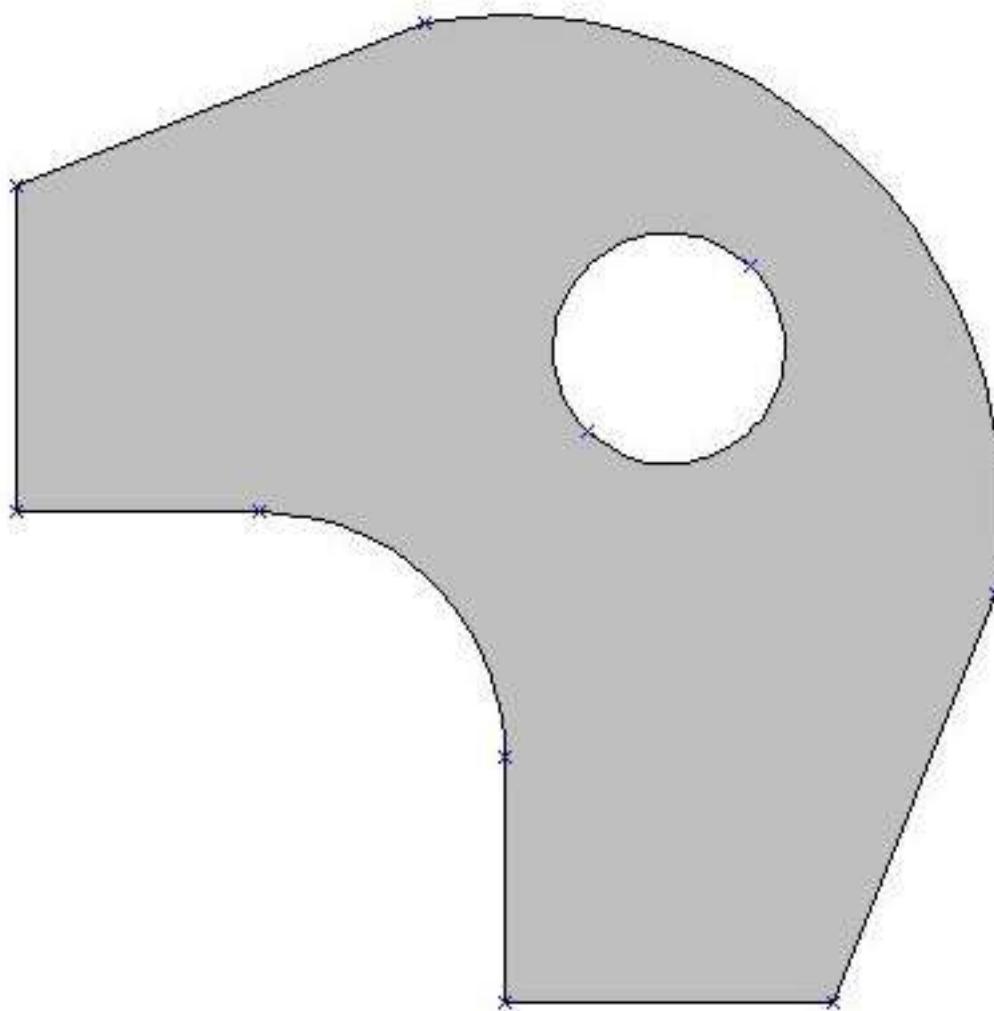
*Automatic region recognition*



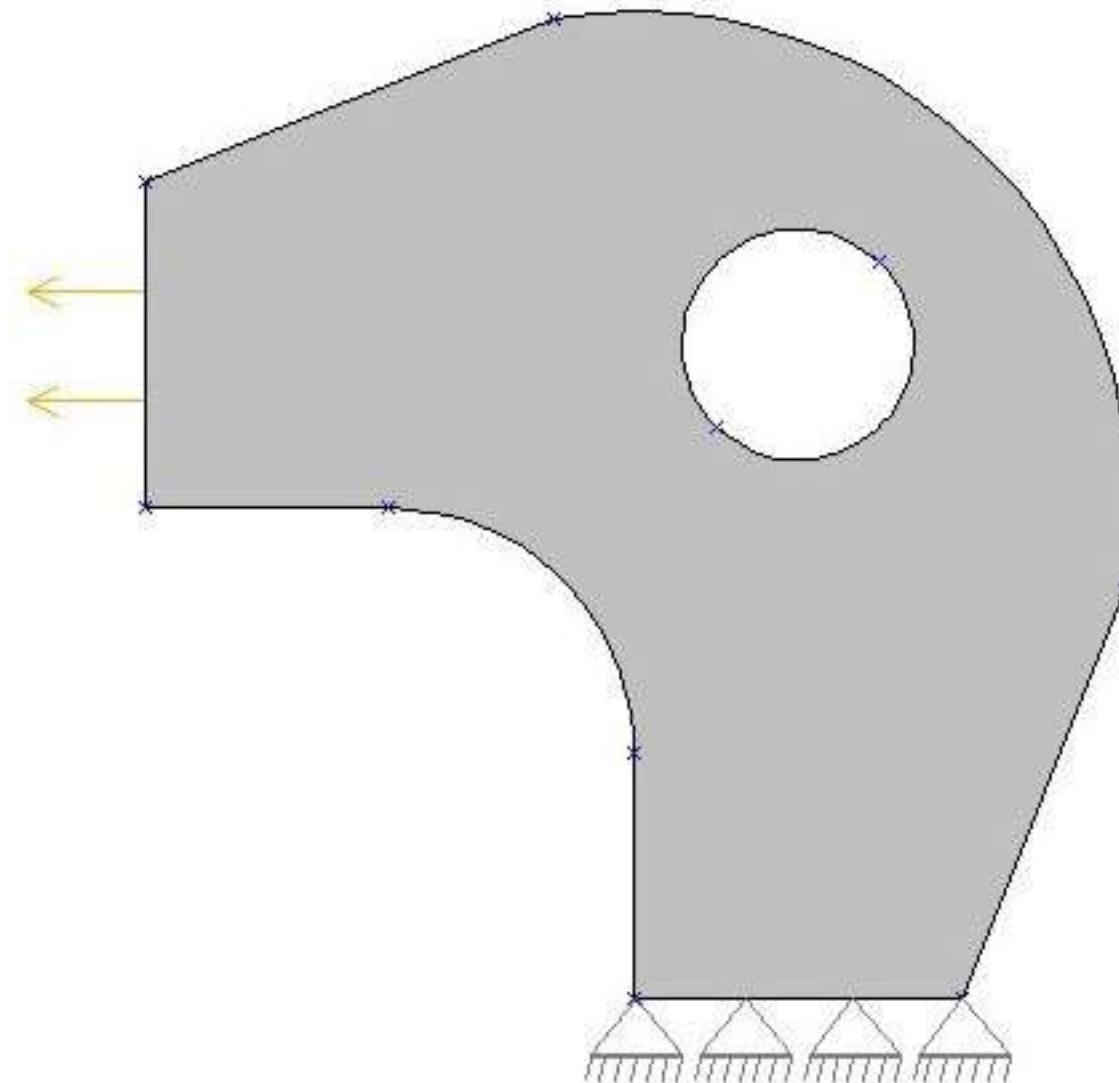
## *Creating a hole*



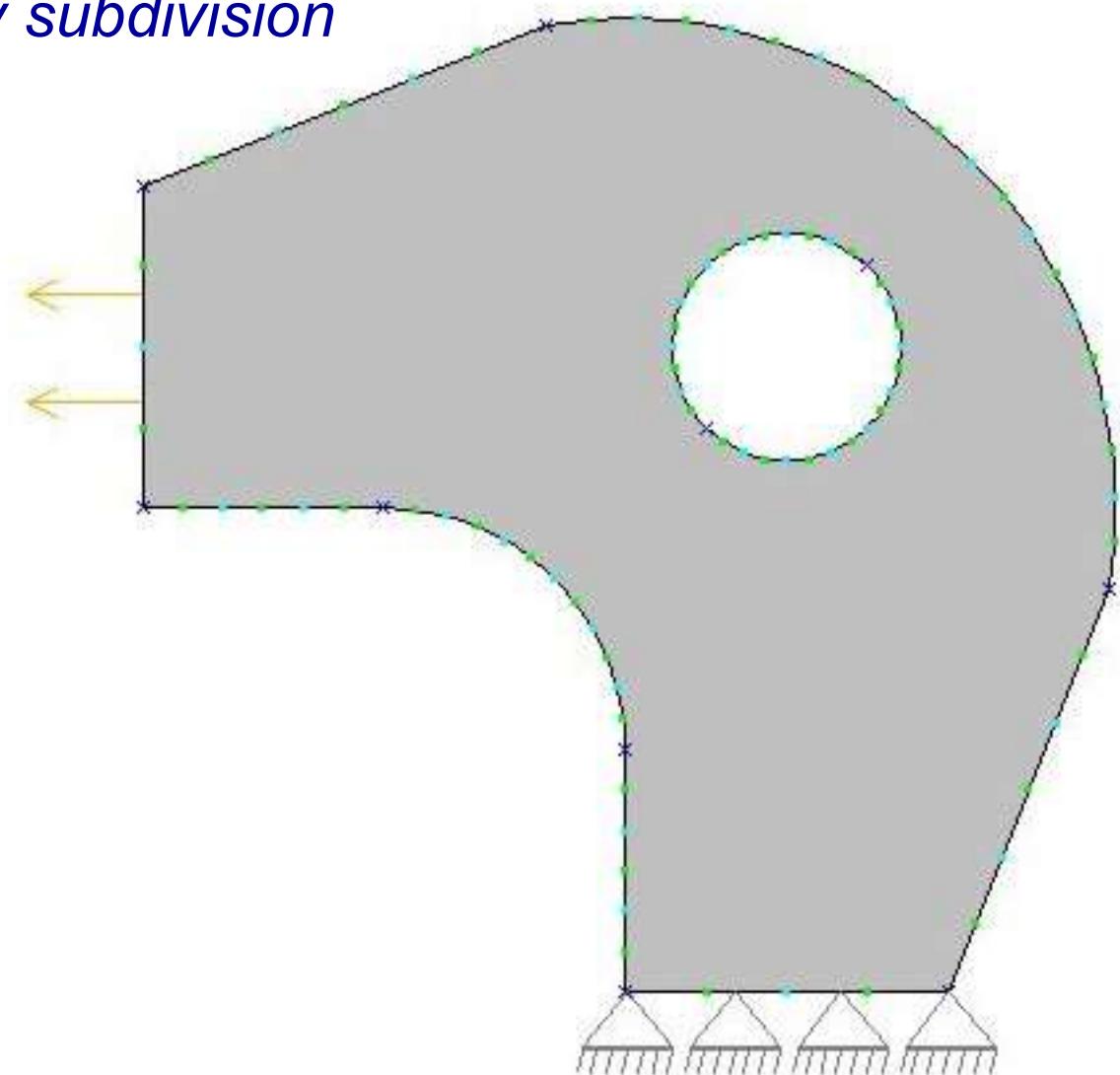
## *Assigning hole attribute*



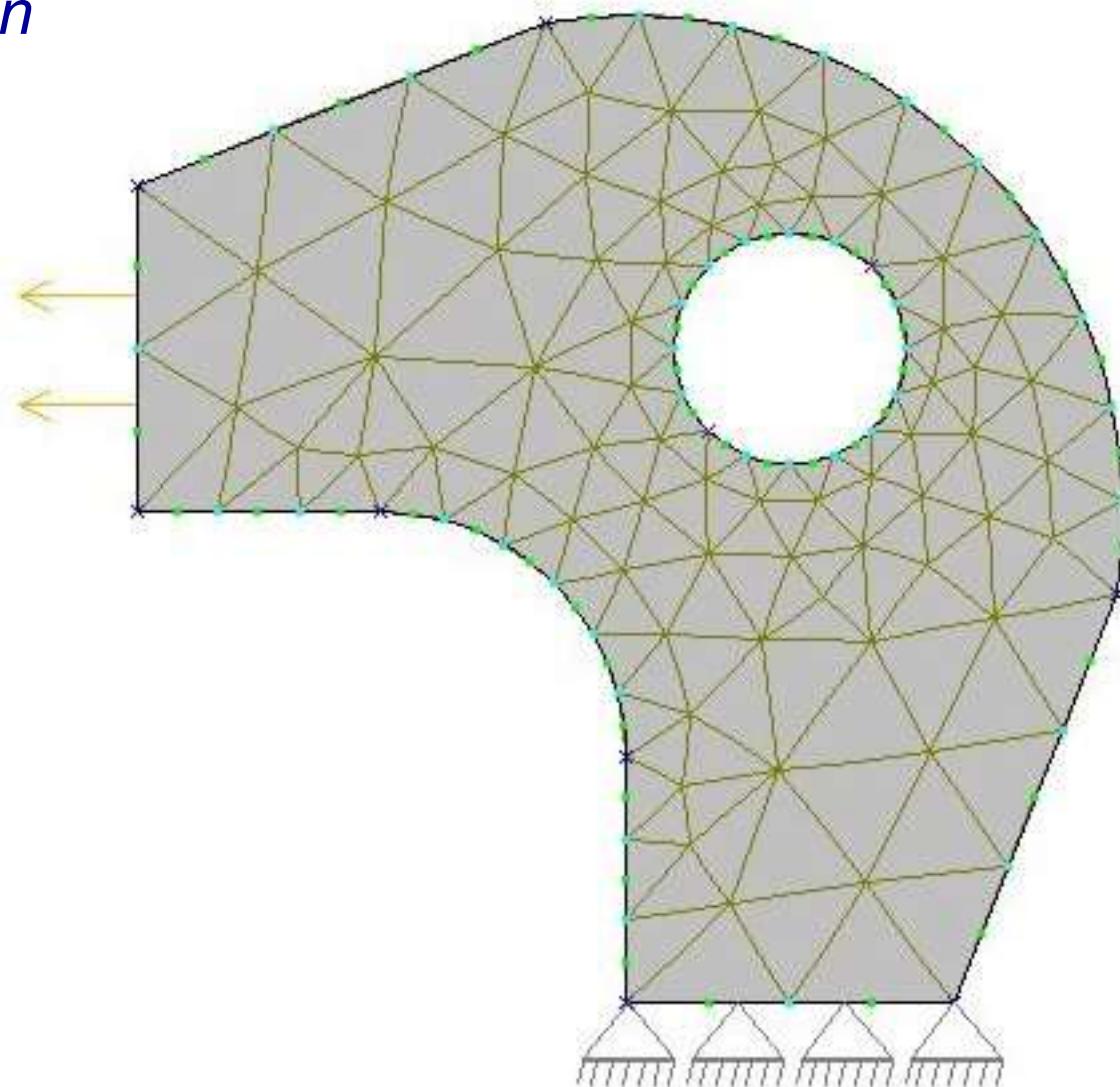
## *Applying attributes to geometry*



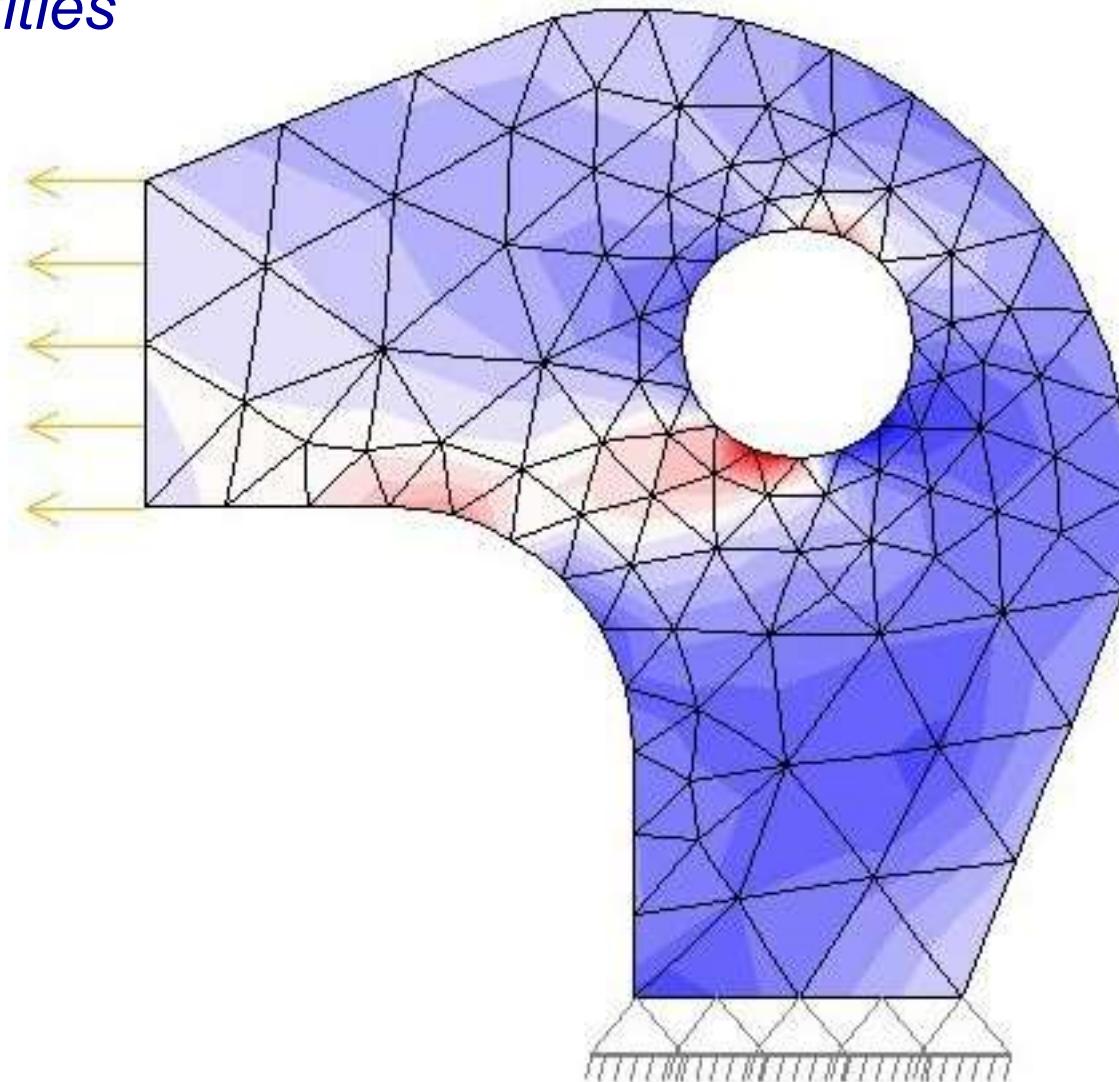
*Defining meshing refinement parameters:  
boundary subdivision*



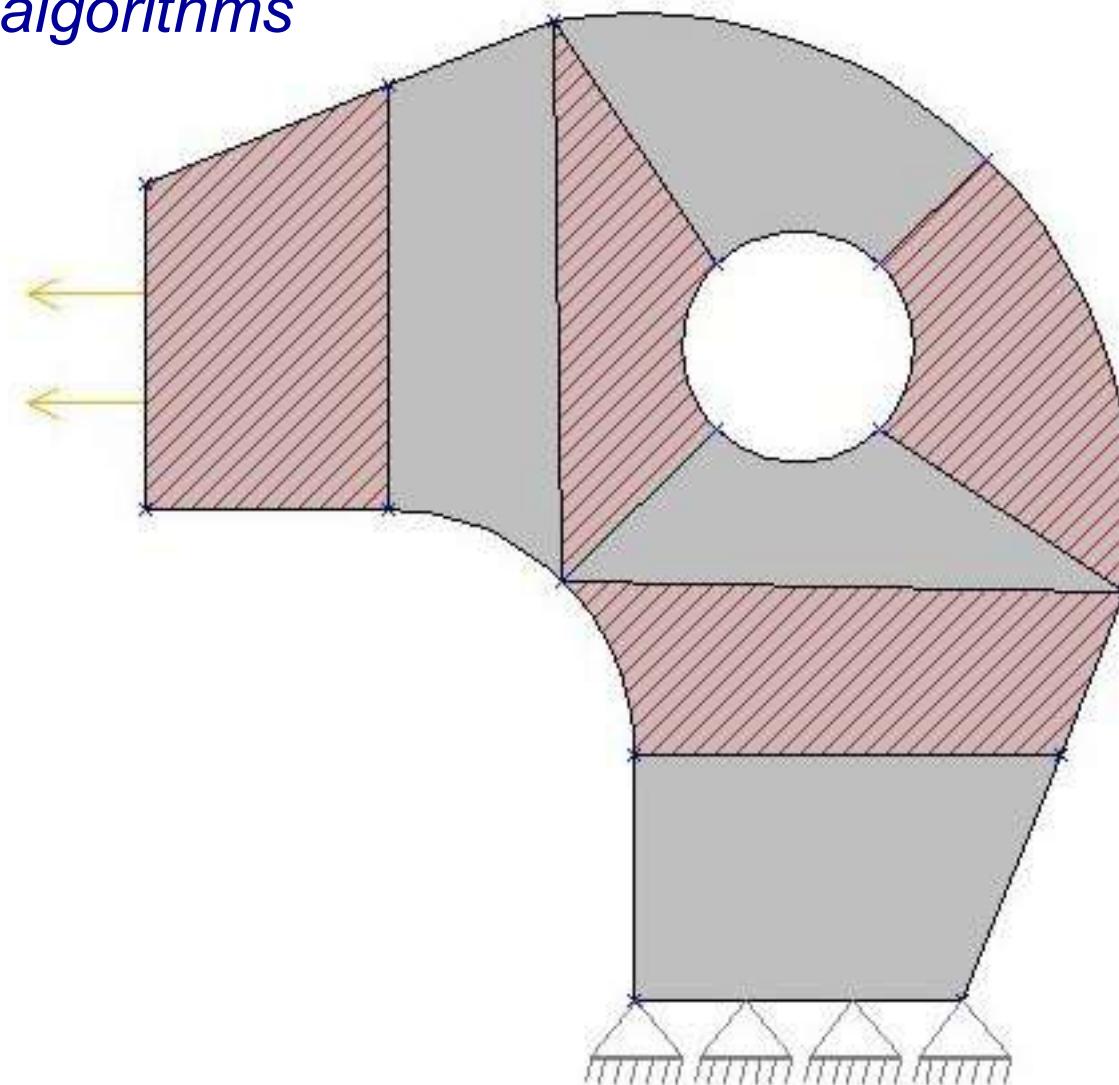
## *Automatic unstructured mesh generation*



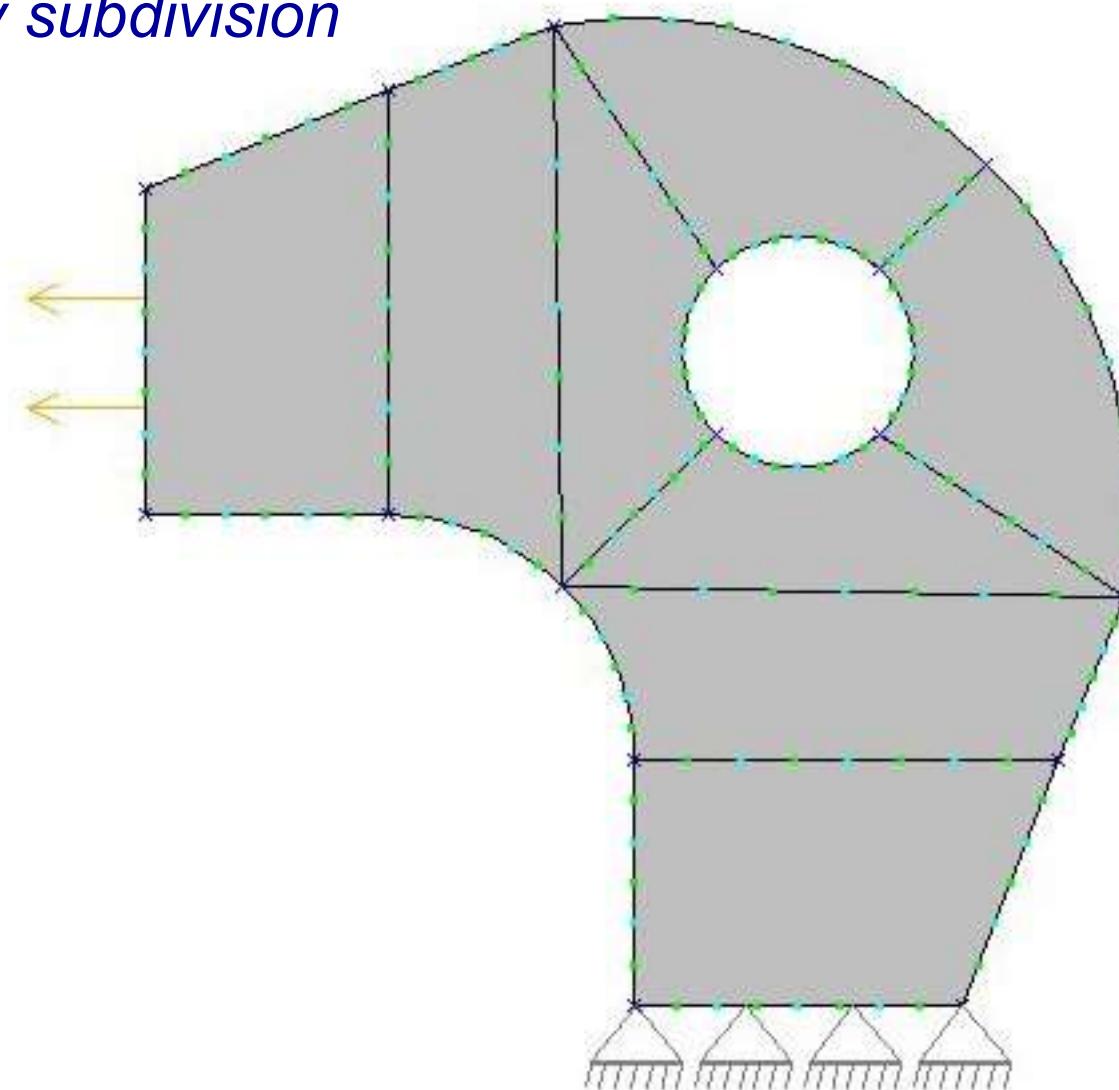
*Attributes automatically assigned to  
mesh entities*



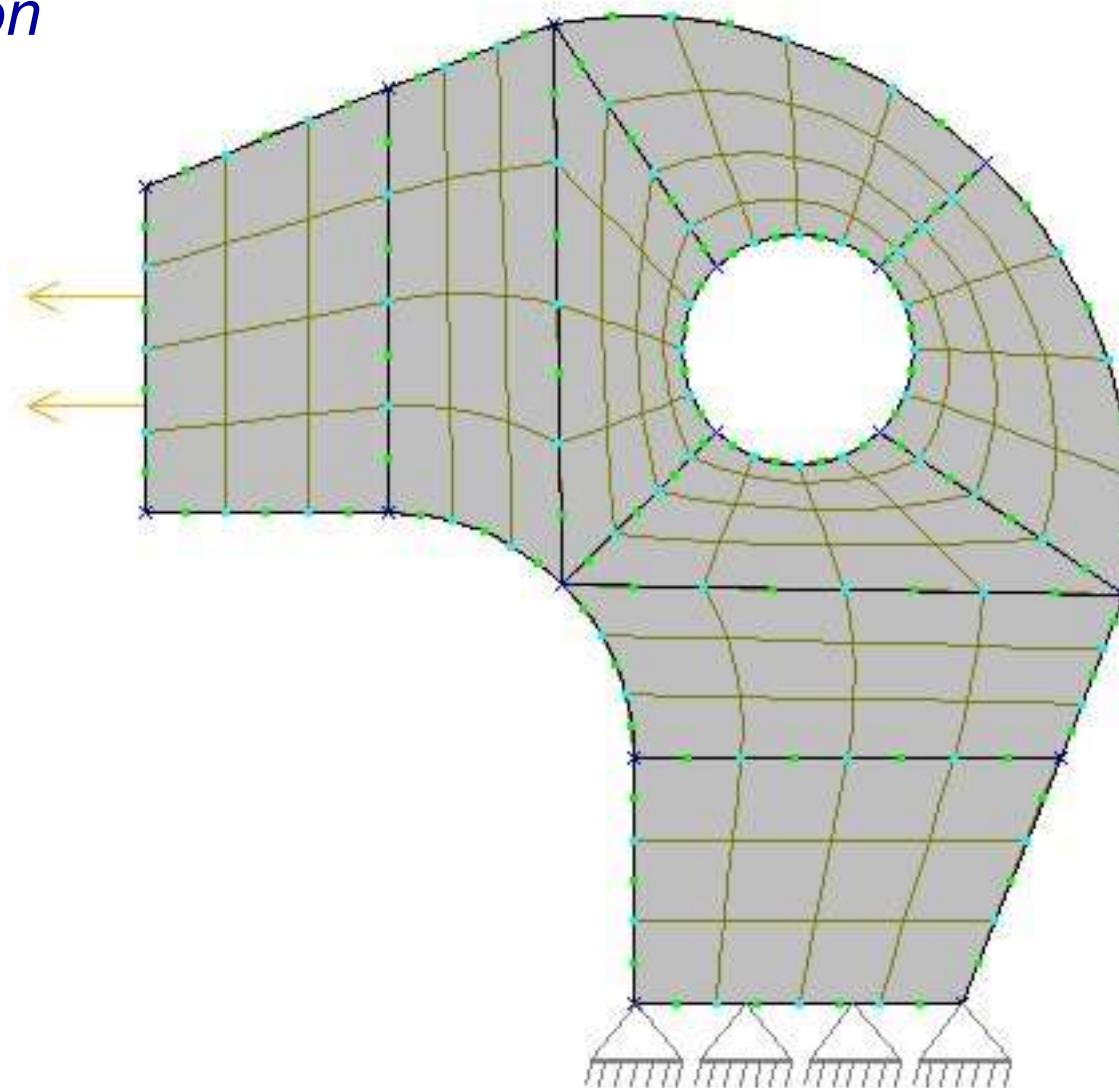
*Region decomposition to exploit structured meshing algorithms*



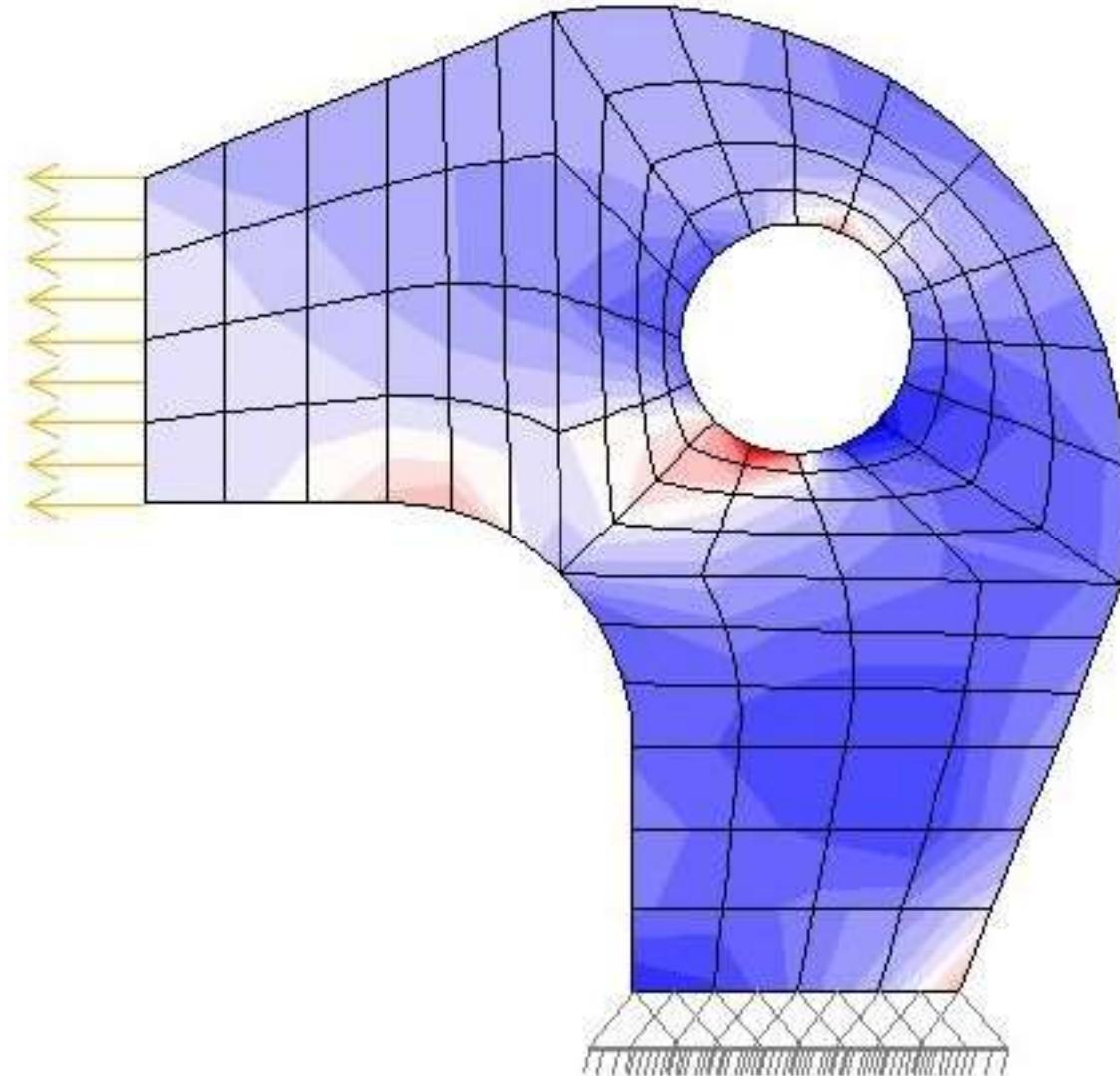
*Defining meshing refinement parameters:  
boundary subdivision*



## *Automatic unstructured mesh generation*

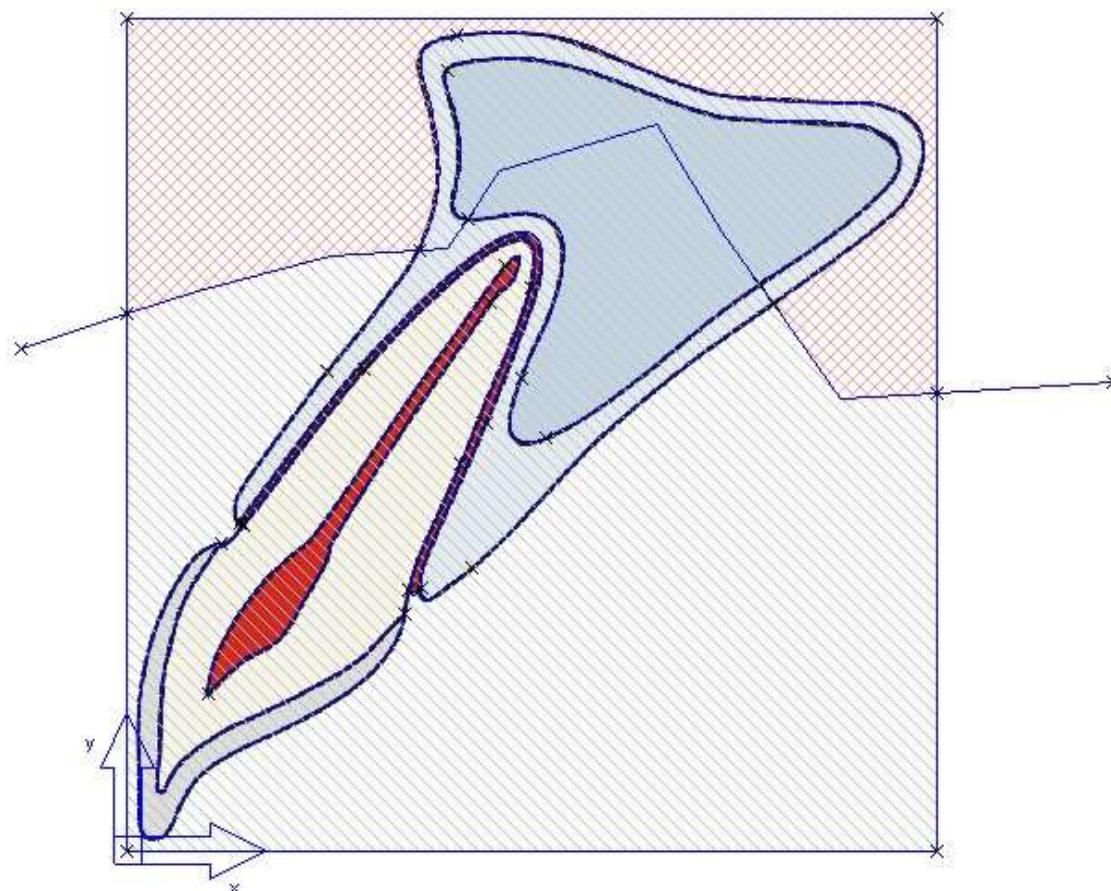


*What is the technology behind this?  
What issues we have to address?*



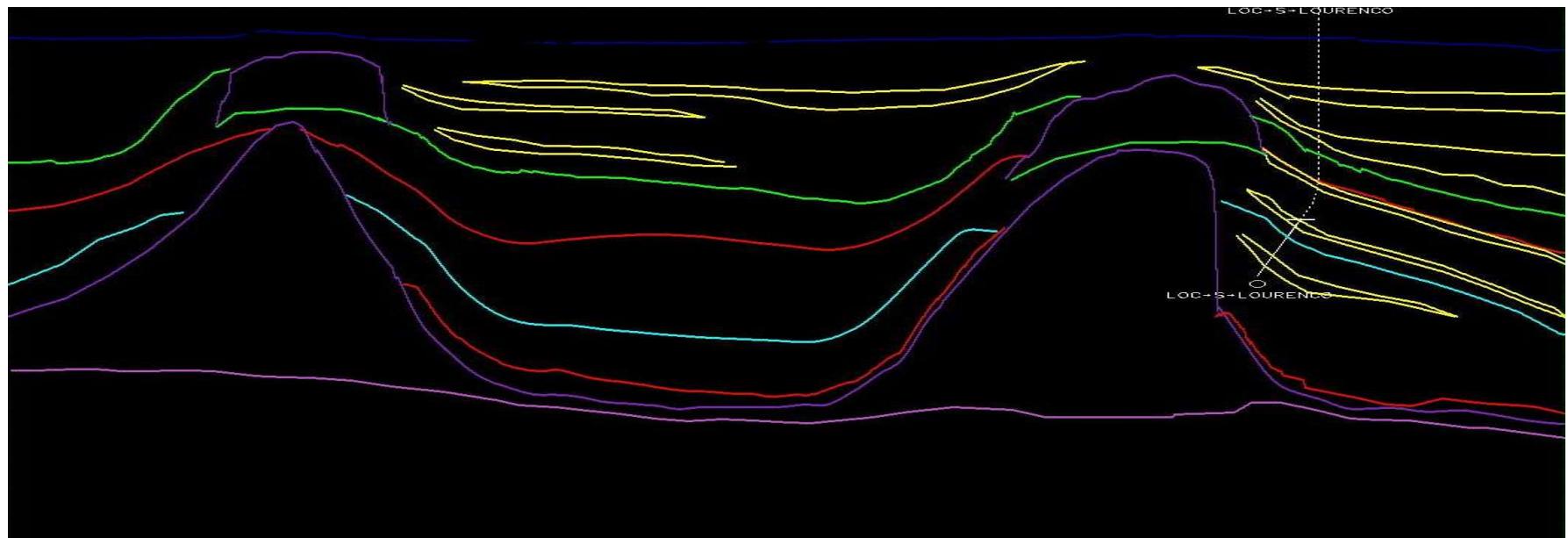
## **Generic Space Subdivision: Many Applications**

*An environment in which curves and surfaces are inserted randomly.  
Automatic region recognition and full adjacency information.*



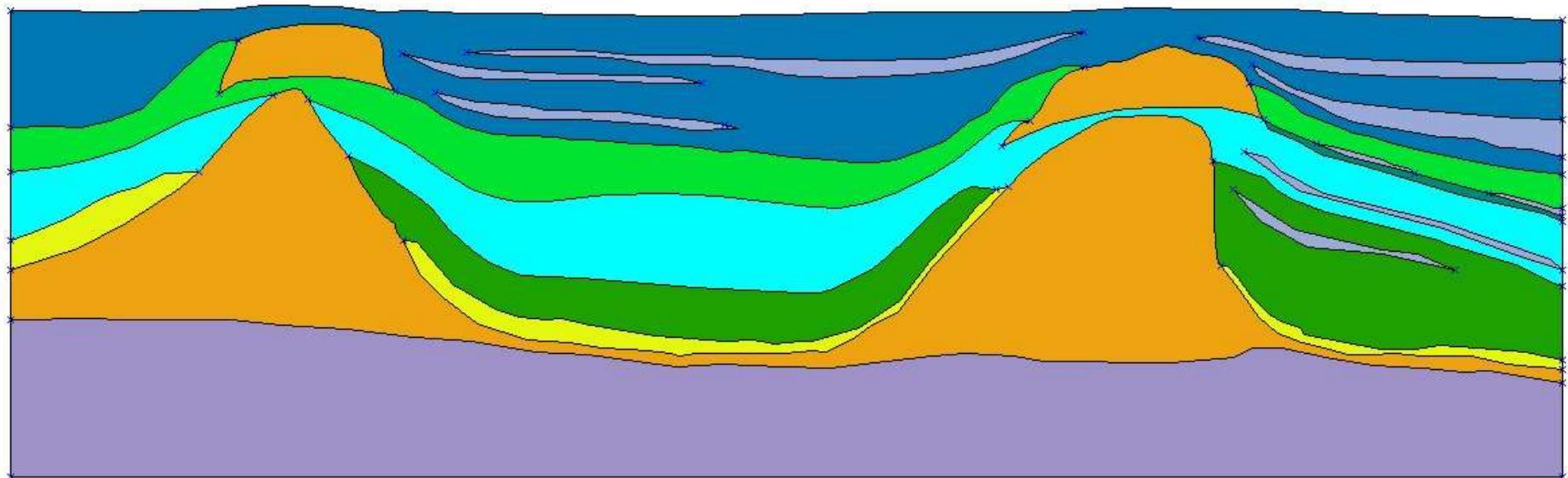
# 2D Subsurface Simulation Modeling

Sidon-Tiro



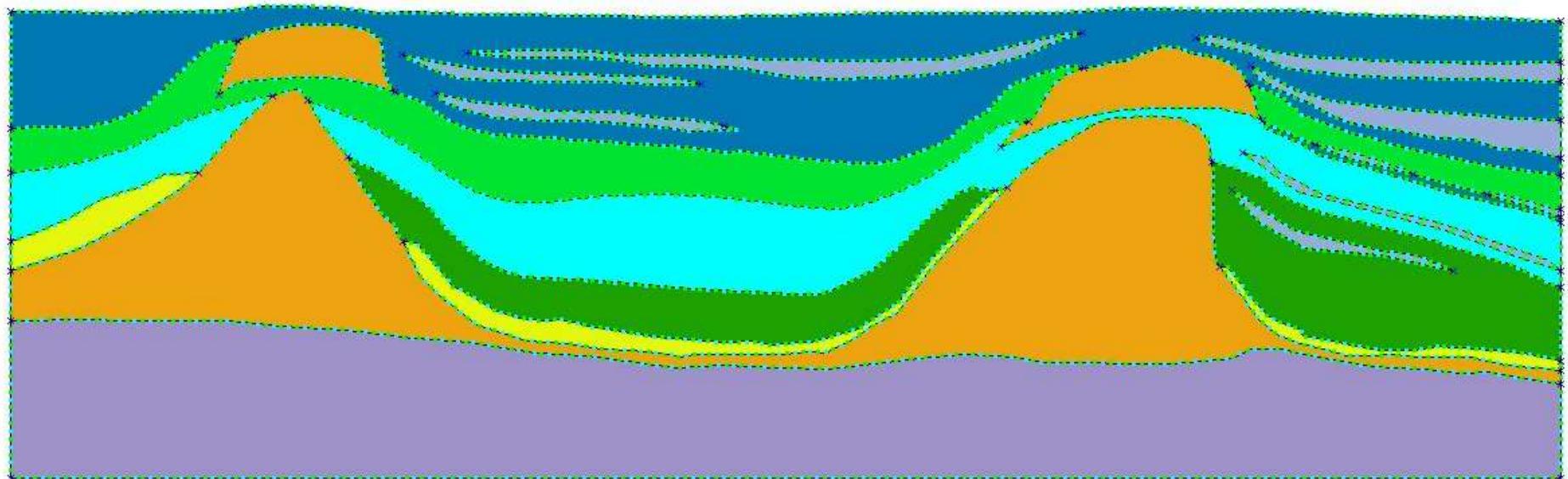
## 2D Subsurface Simulation Modeling

Curve digitalization



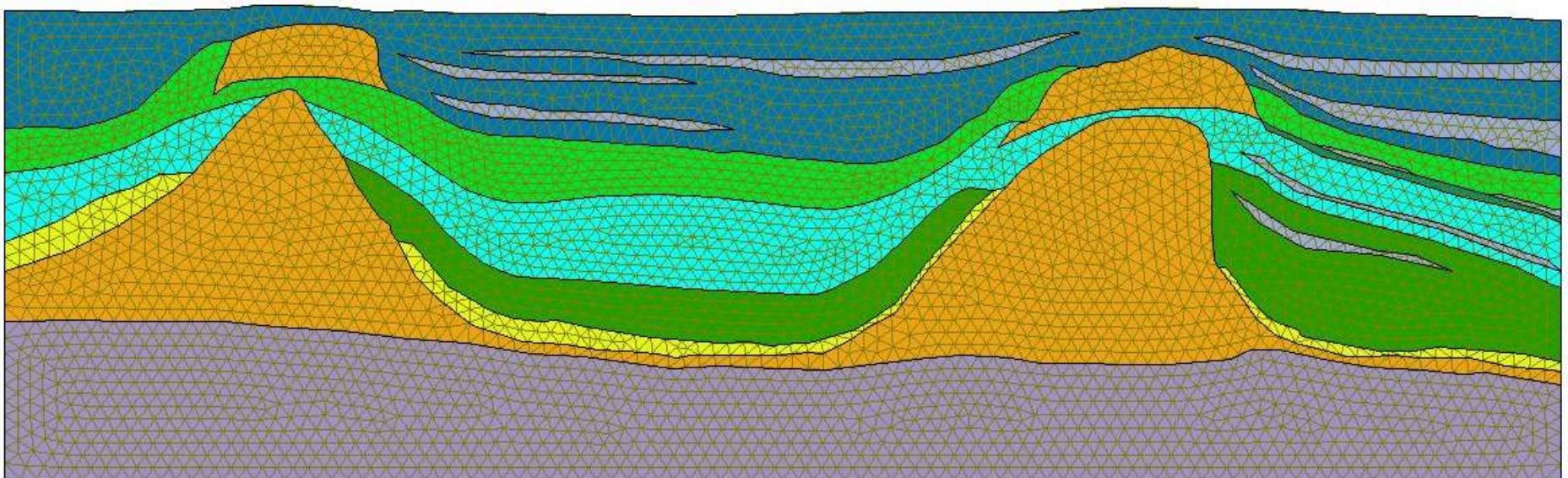
## 2D Subsurface Simulation Modeling

Curve subdivision



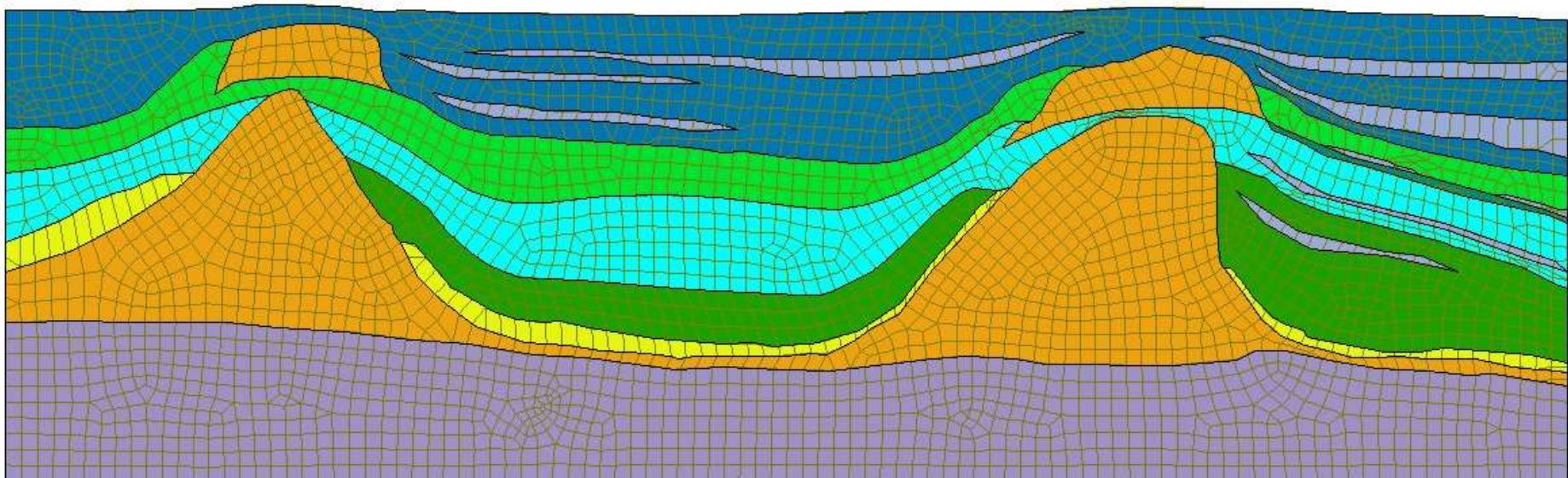
## 2D Subsurface Simulation Modeling

Mesh generation: triangular elements



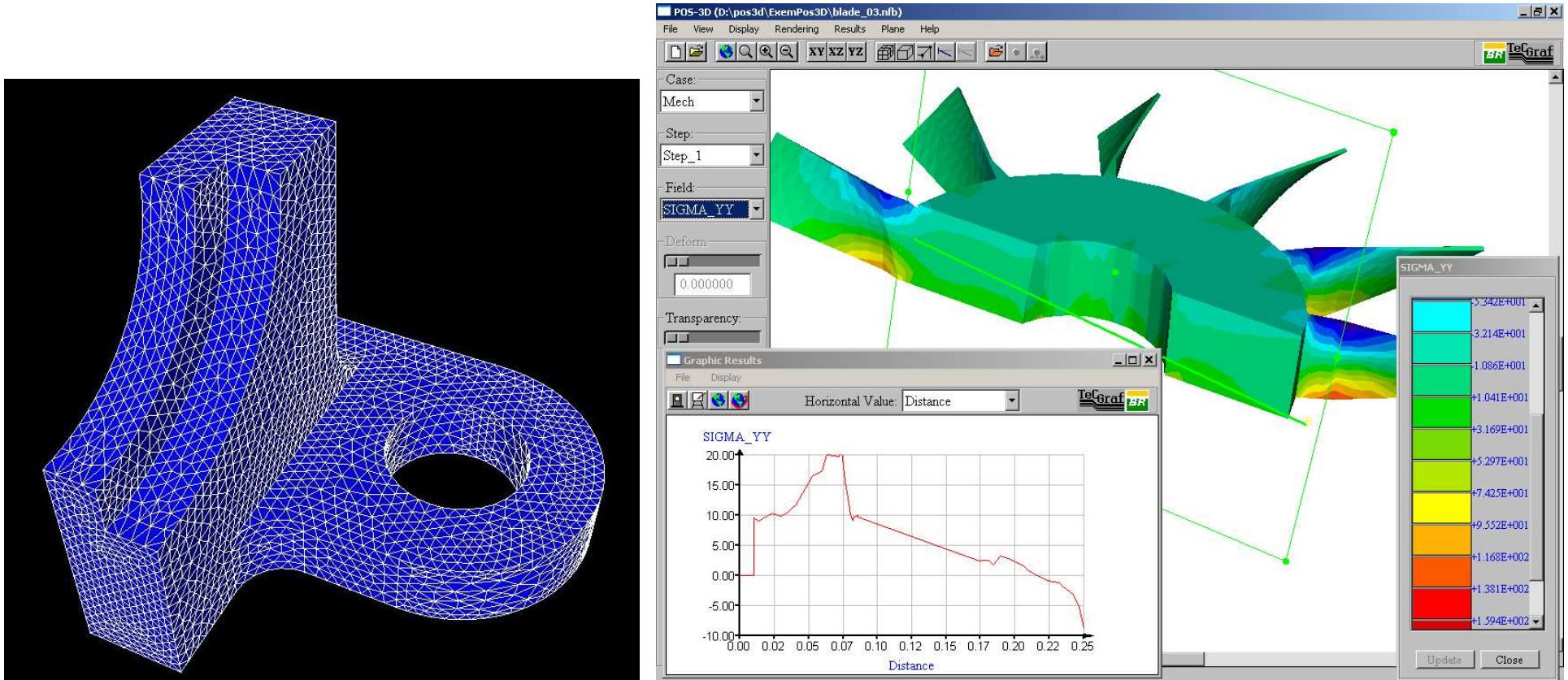
## 2D Subsurface Simulation Modeling

Mesh generation: quadrilateral elements



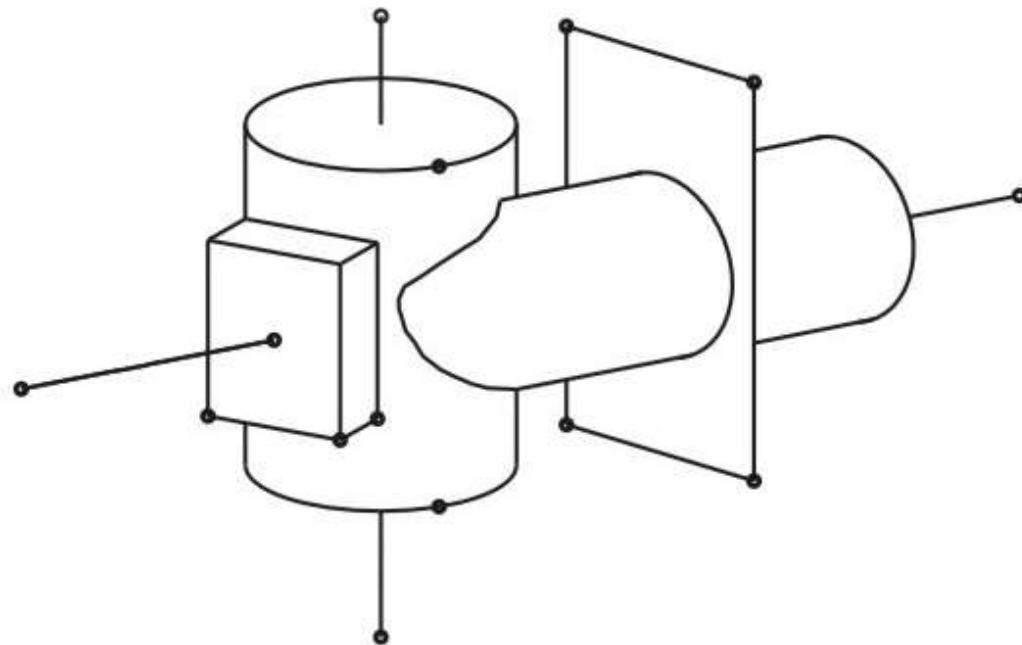
# Requirements for underlying data representation

*–The data structures must provide a natural navigation across all phases of a simulation: pre-processing (model creation), numerical analysis, and post-processing (model results visualization).*



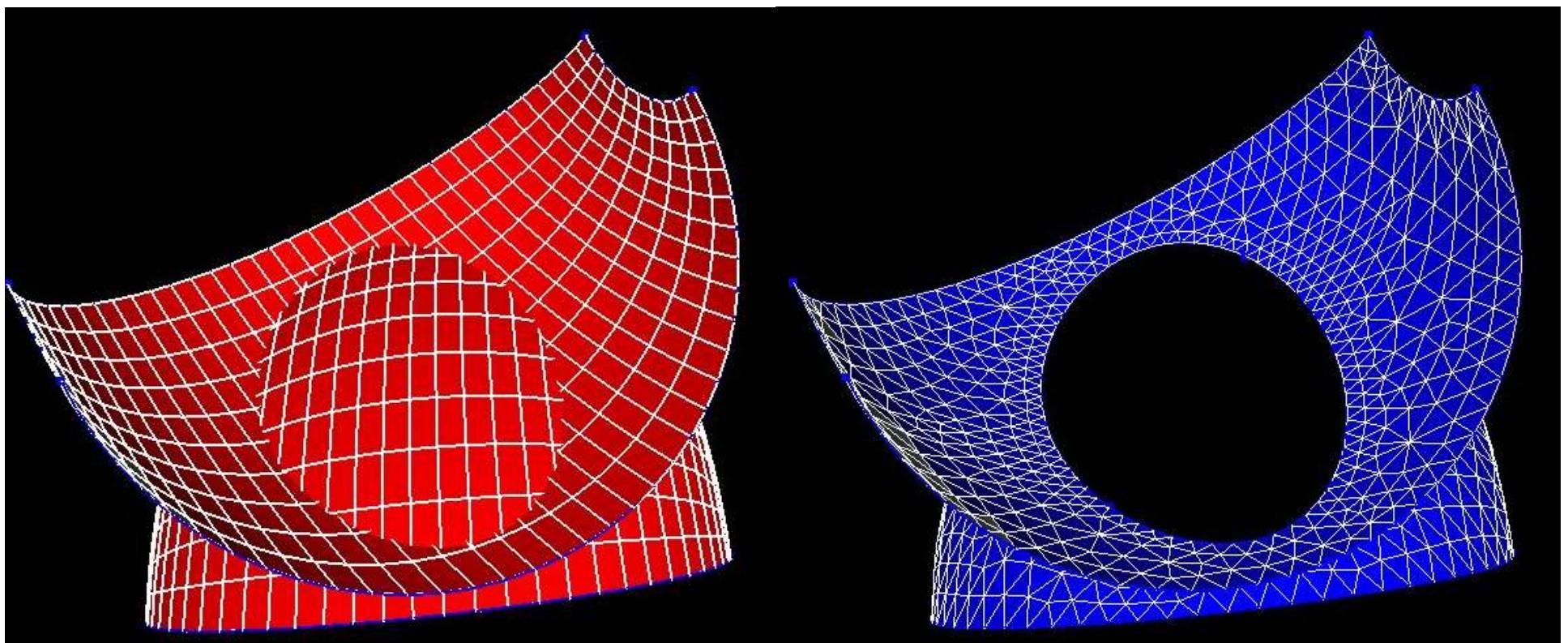
## Requirements for underlying data representation (cont.)

*–The data structures must take into account that the simulation may induce, at least temporarily during model creation, geometric objects (curves and surfaces) that are inconsistent with the target final model. This requires a non-manifold topology representation capability.*



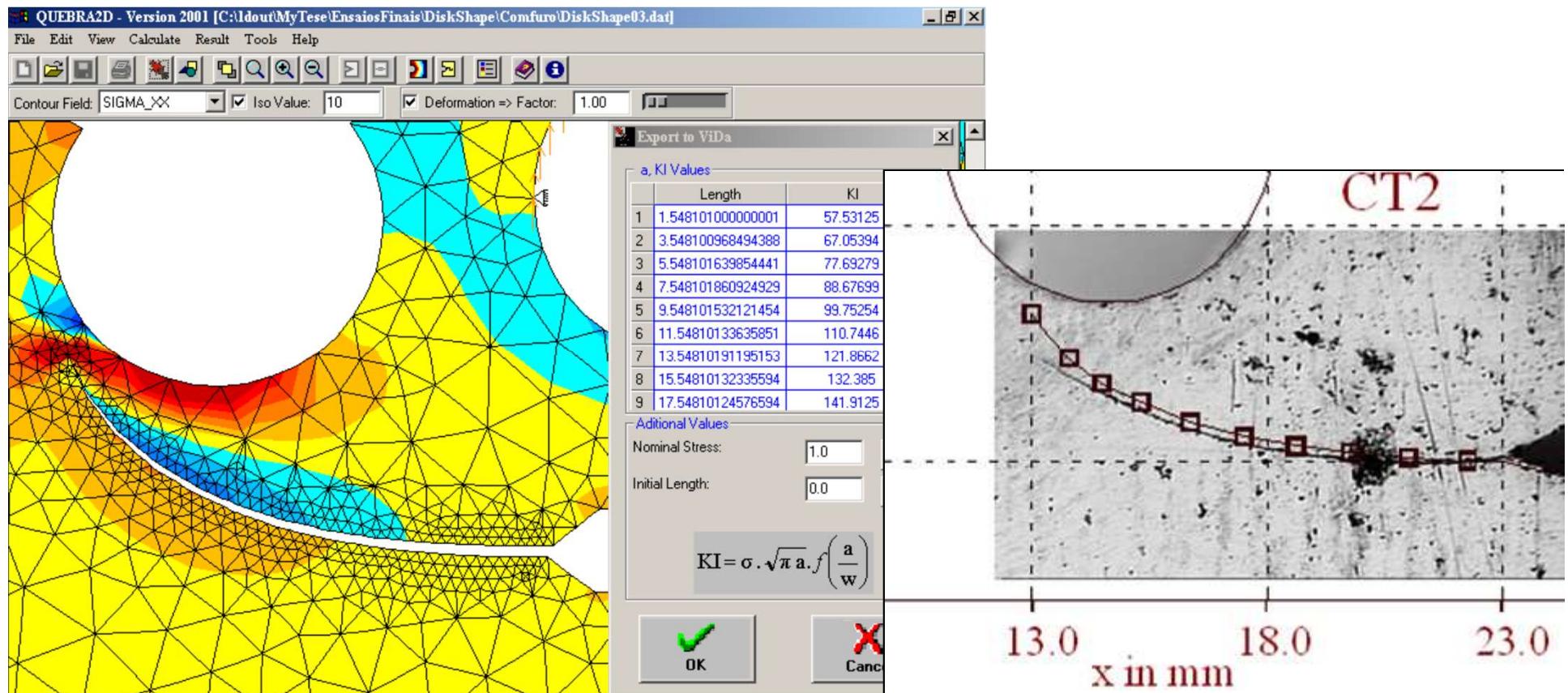
## Requirements for underlying data representation (cont.)

*–The data structure should aid in key aspects of geometric modeling, such as surface intersection and automatic region recognition, as well as in surface and solid finite element mesh generation in arbitrary domains.*



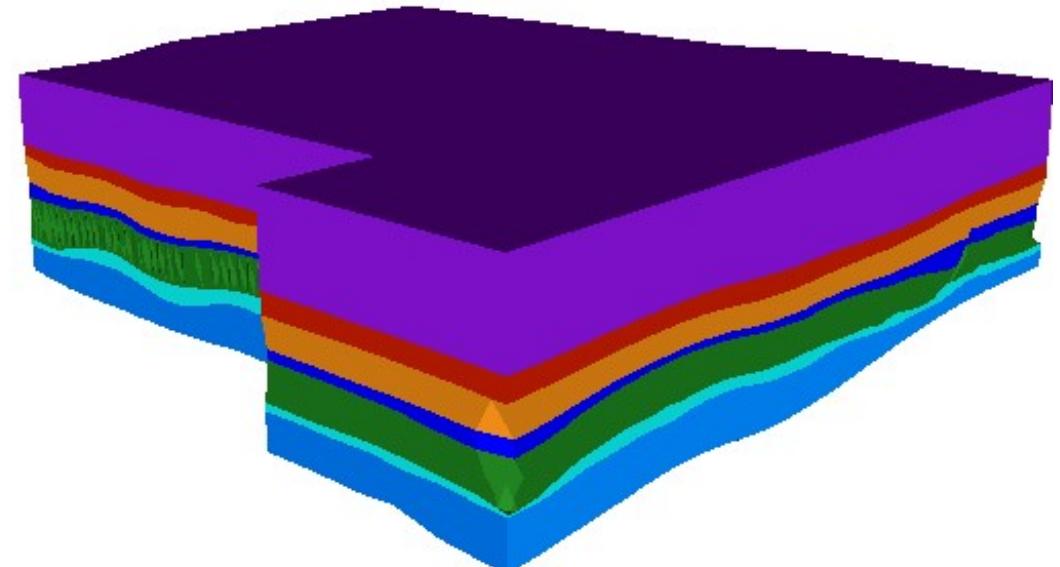
## Requirements for underlying data representation (cont.)

*–The data structure must provide for efficient geometric operators, including automatic intersection detection and processing.  
This is necessary in simulations with evolving topology and geometry.*

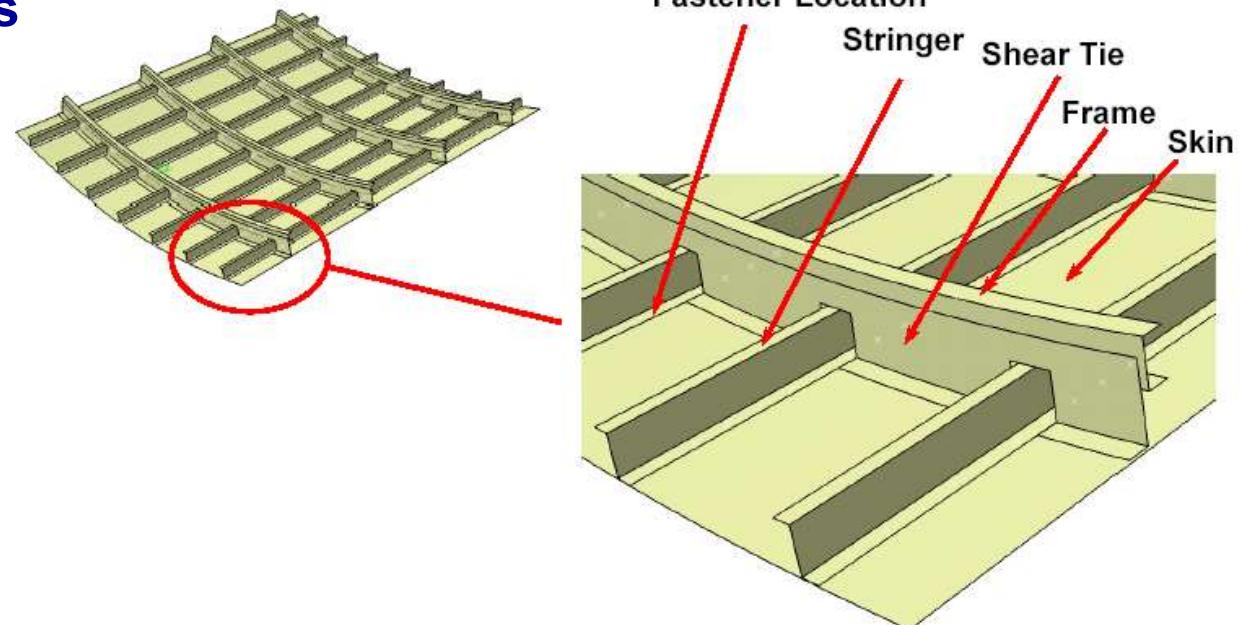


# The need for non-manifold modeling

## Multi-region modeling

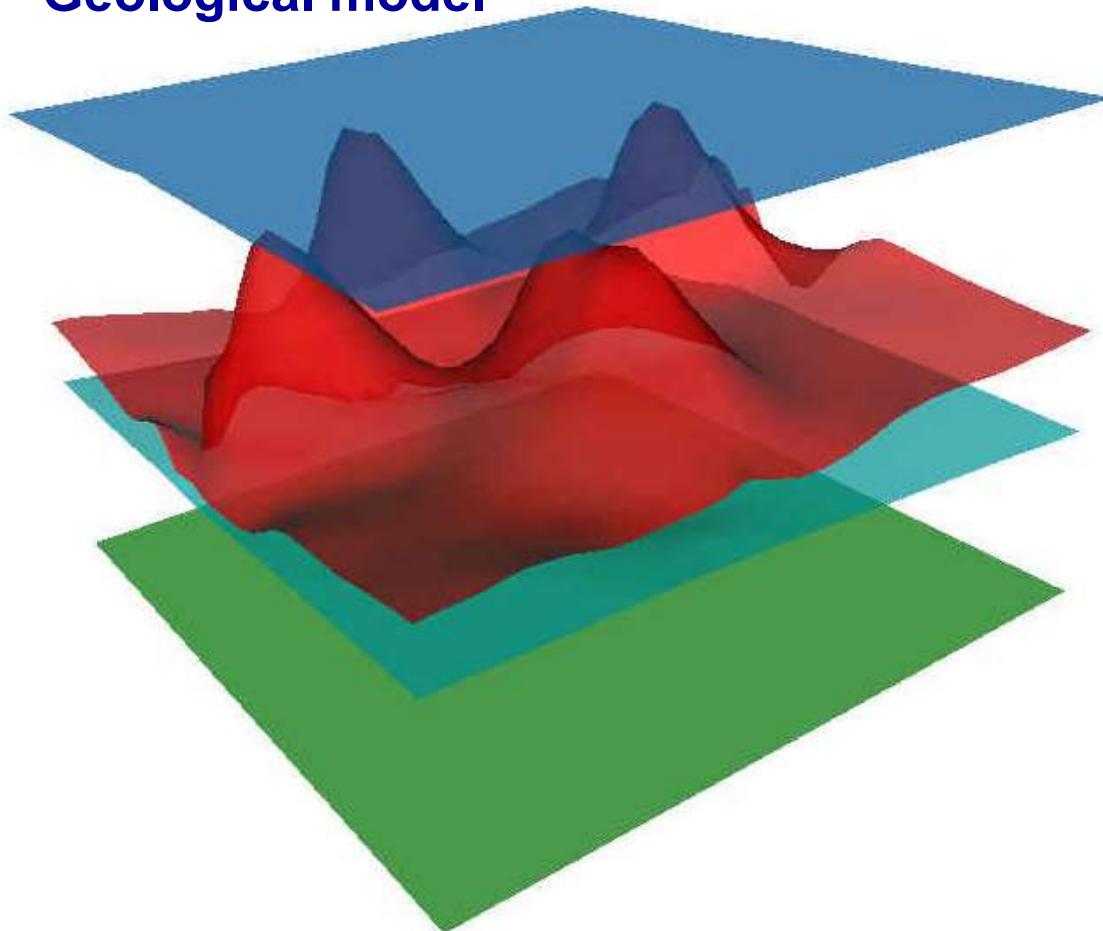


## Degenerated structures

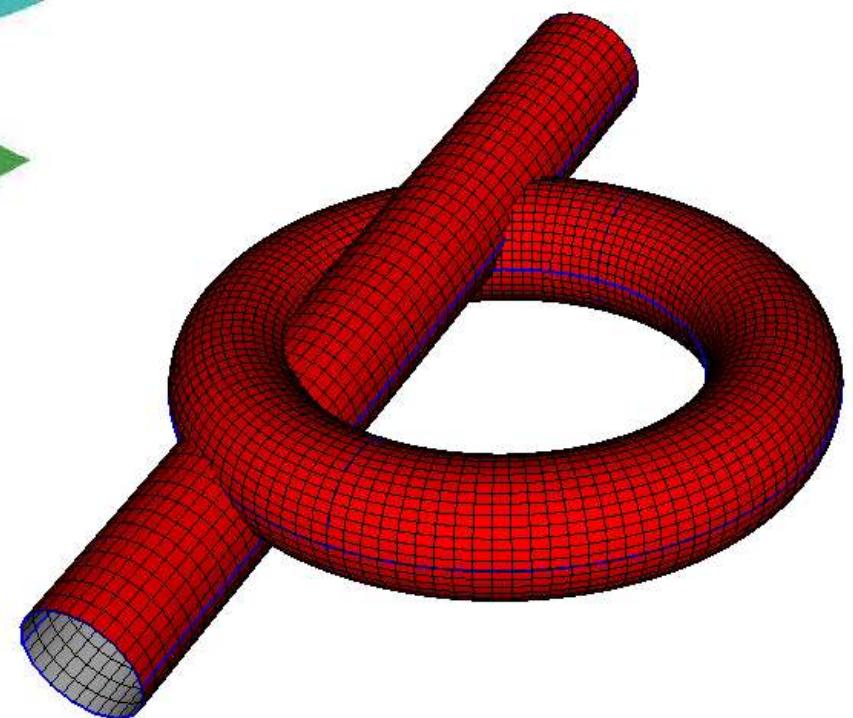


# Natural modeling: surface patches as primitives

Geological model

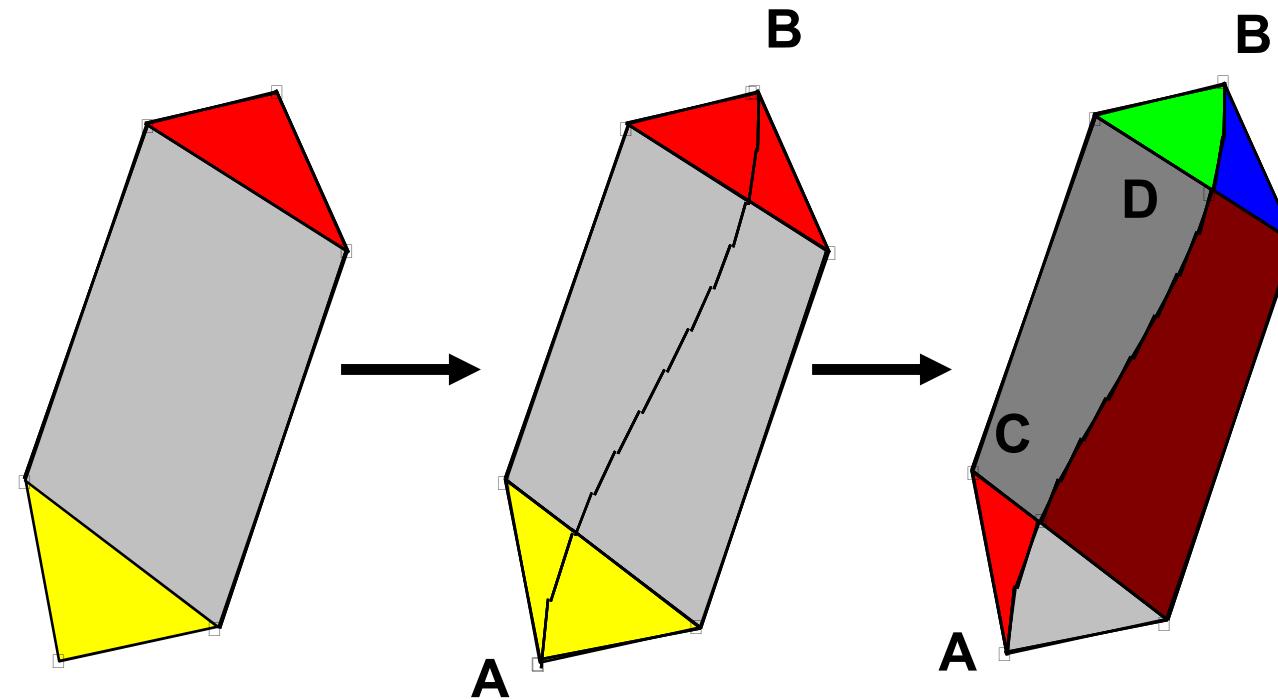


Manufactured model



# Ideal environment: complete space subdivision

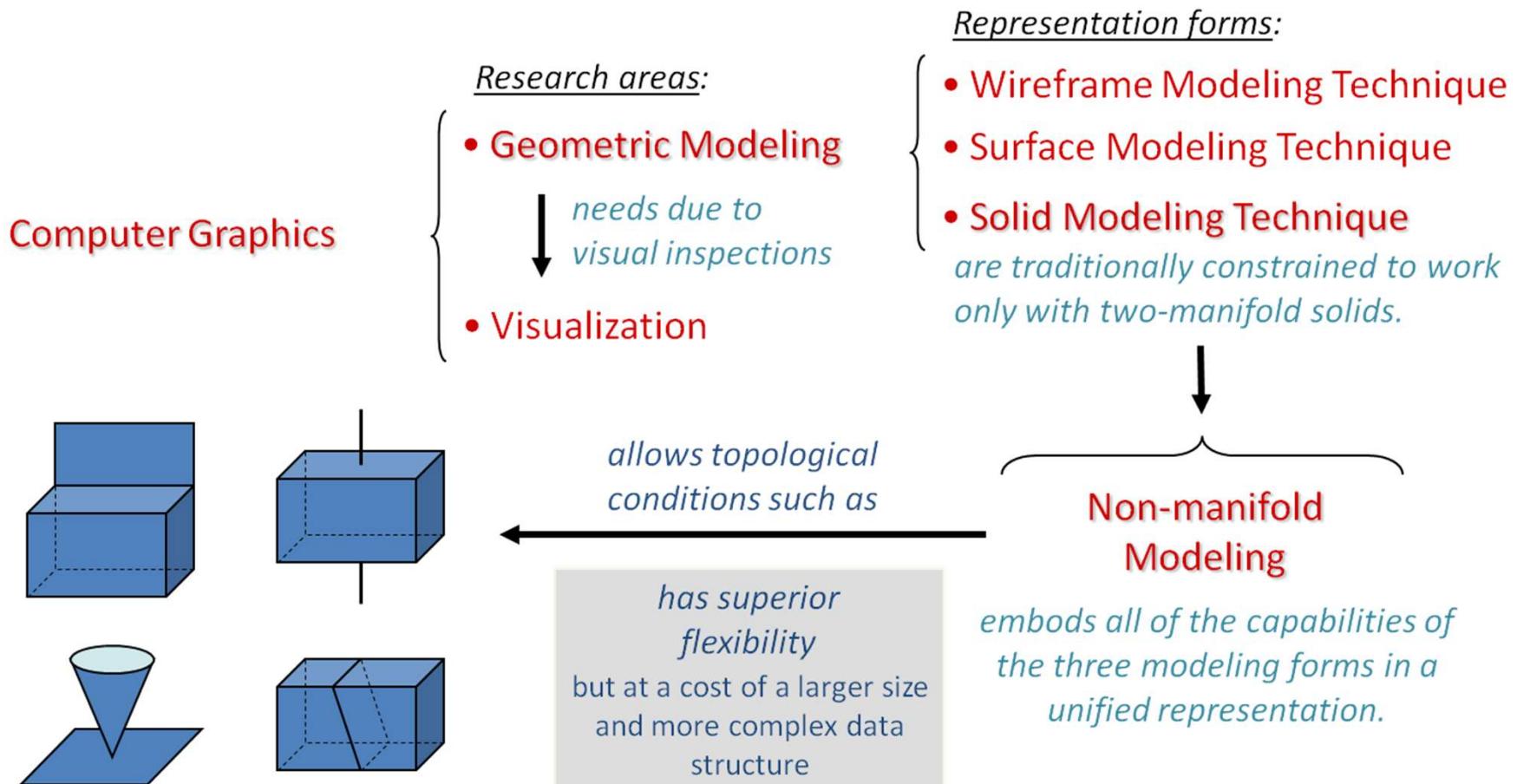
## Space subdivision in 2D: high level operations



**User action  
+ basic function**

**System  
response**

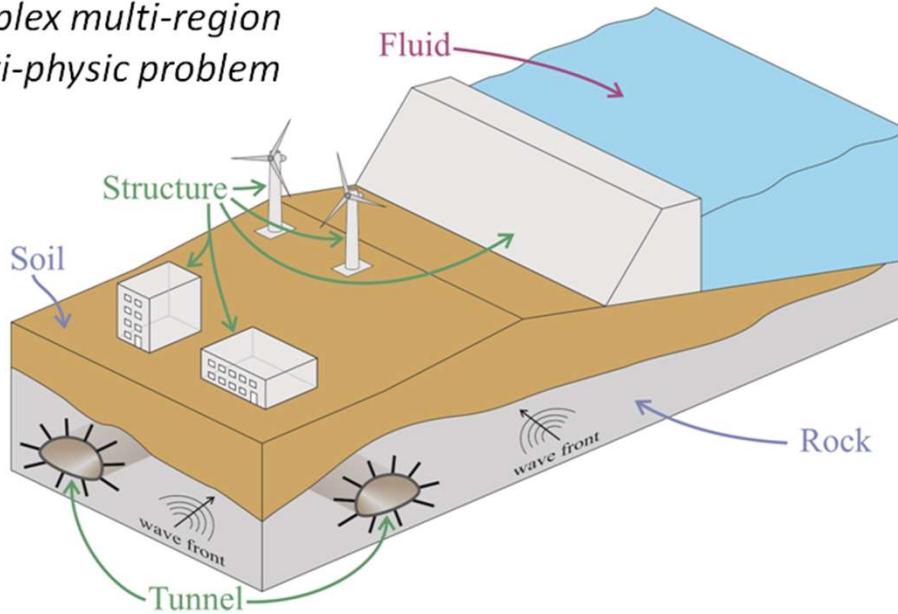
# Modelagem em Engenharia



# Modelagem em Engenharia

## Computer Graphics

complex multi-region  
multi-physics problem



### Research areas:

- Geometric Modeling
- Visualization

*needs due to visual inspections*

### Representation forms:

- Wireframe Modeling Technique
- Surface Modeling Technique
- Solid Modeling Technique

*are traditionally constrained to work only with two-manifold solids.*

## Non-manifold Modeling

*embodies all of the capabilities of the three modeling forms in a unified representation.*

# **Modelagem Geométrica**

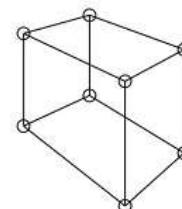
# Modelagem Geométrica

- Criação, manipulação, manutenção e análise das representações das formas geométricas de objetos bi e tridimensionais.
- Aplicação em diversas áreas, como na produção de filmes, design de peças mecânicas industriais, visualização científica e reprodução de objetos para análise em engenharia.

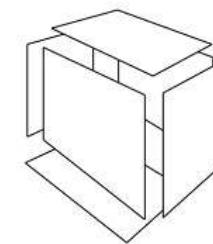
# Modelagem Geométrica

- **Evolução Histórica:**

- a) Modelagem por arames

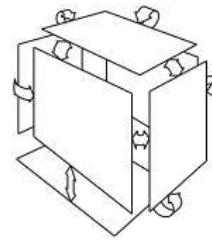


(a)



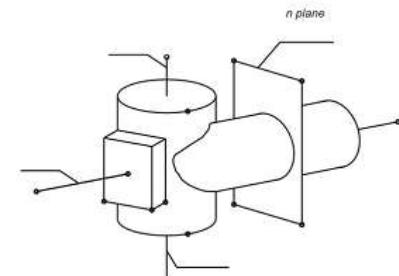
(b)

- a) Modelagem por superfícies



(c)

- b) Modelagem de sólidos



(d)

- a) Modelagem *non-manifold*

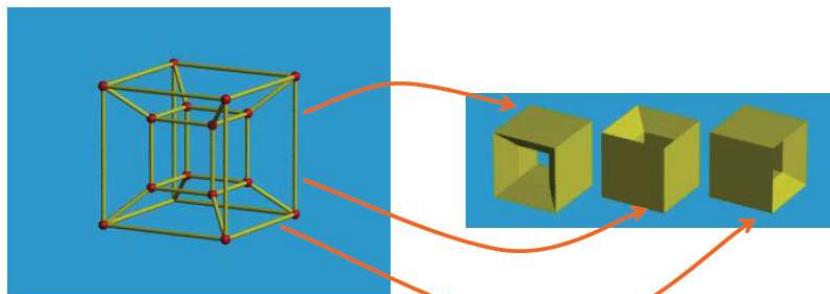
# Modelagem Geométrica

- **Formas de representação de sólidos**

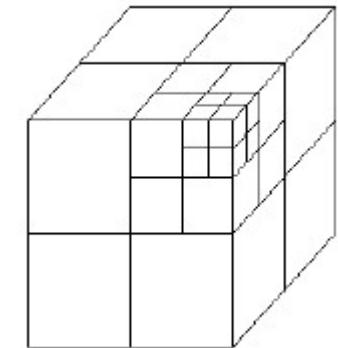
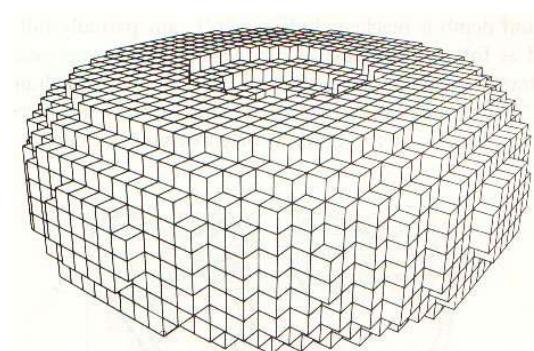
- Modelos de decomposição
- Modelos B-Rep
- Modelos construtivos (CSG)
- Modelos híbridos

# Modelagem de Sólidos

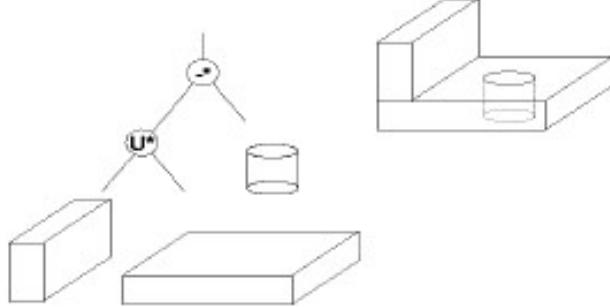
Wire Frame



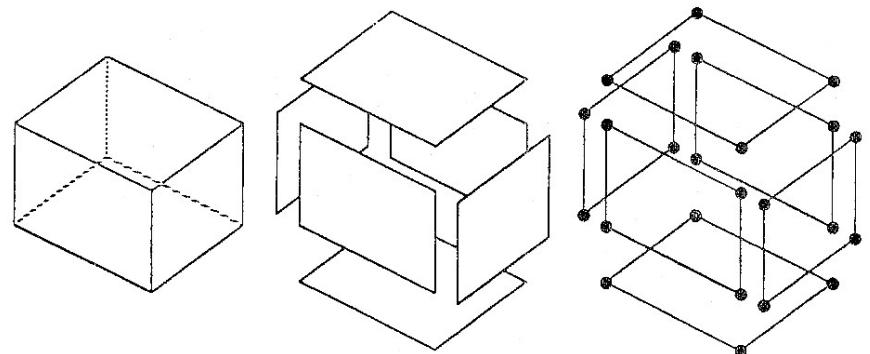
Cell Decomposition / Space Enumeration



Constructive Solid Geometry (CSG)

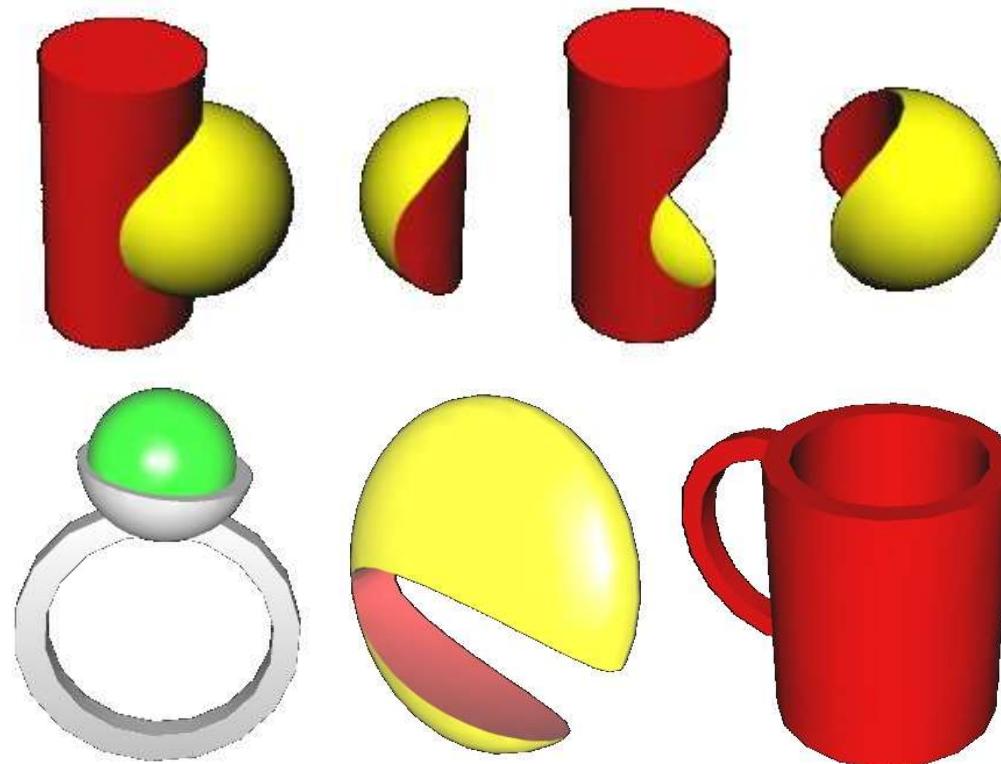


Boundary Representation (B-Rep)



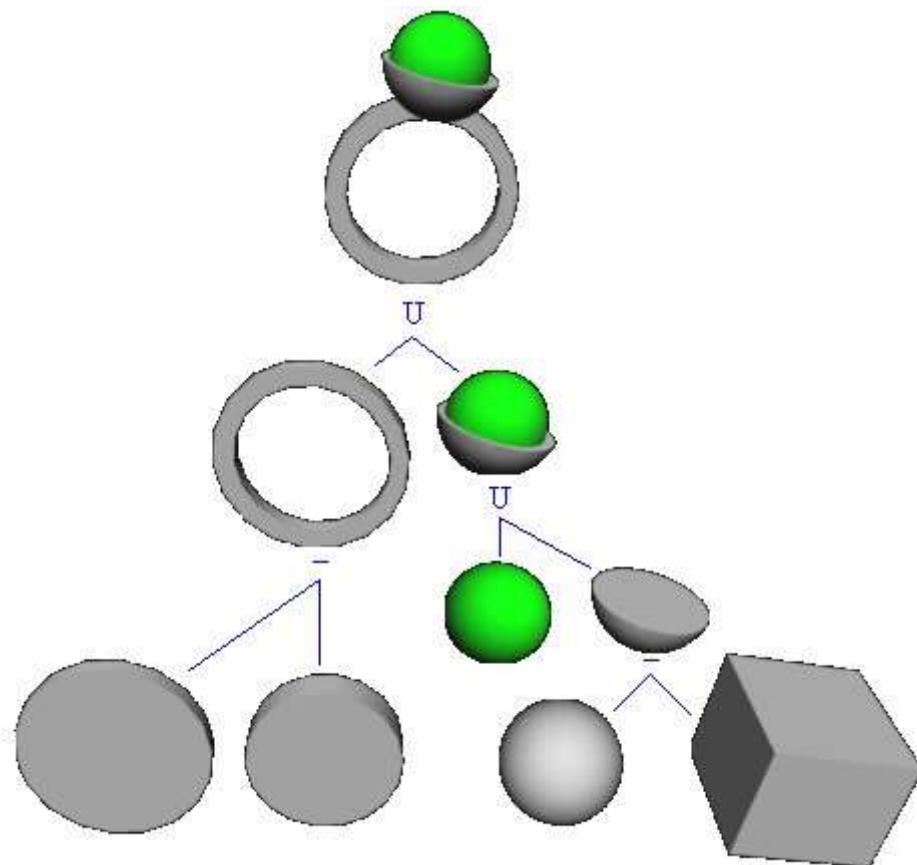
# Modelagem Geométrica

- A Geometria Construtiva de Sólidos (CSG) utiliza as operações booleanas e de movimentos rígidos em primitivas simples para construir objetos sólidos mais complexos.



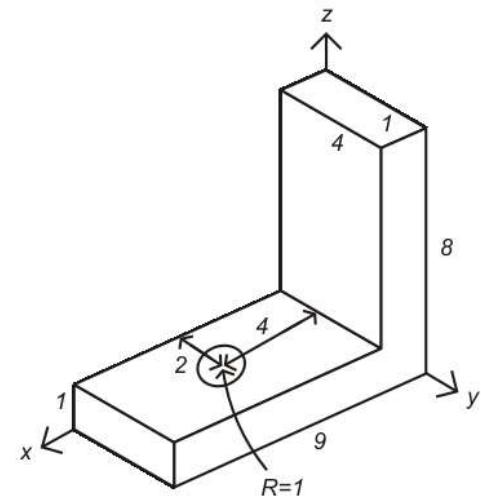
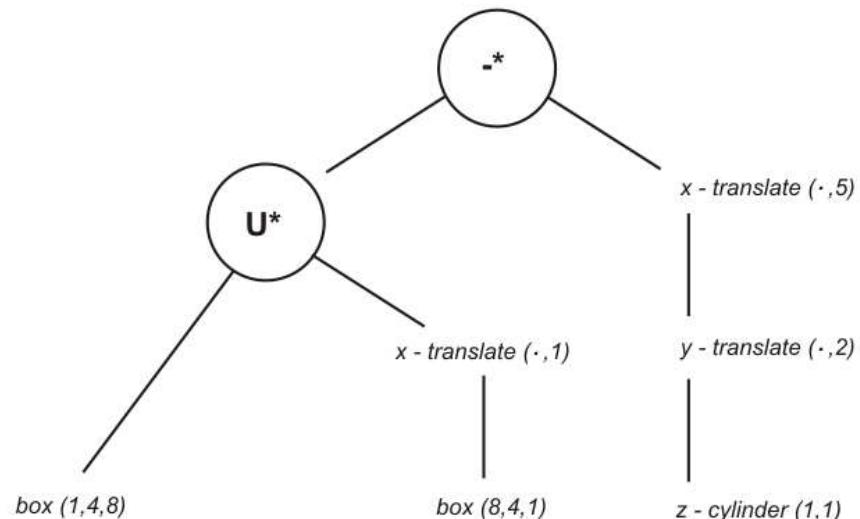
# Modelagem Geométrica

- Árvore CSG



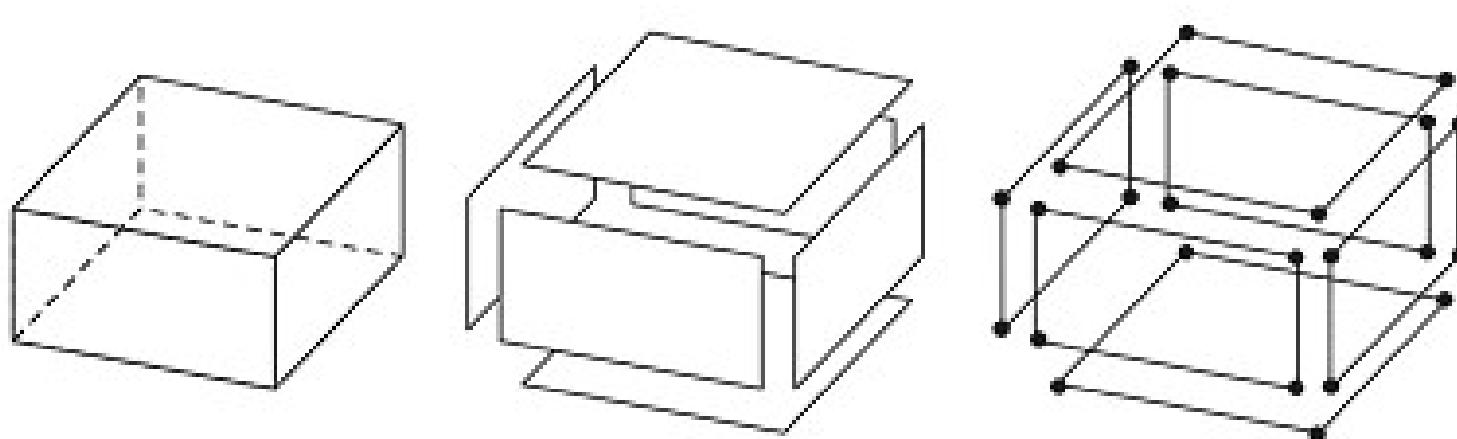
# Modelagem Geométrica

- Árvore CSG



# Modelagem Geométrica

- Modelos B-Rep utilizam explicitamente as relações de adjacência entre os elementos topológicos (vértices, arestas e faces) para definir a fronteira topológica dos objetos.

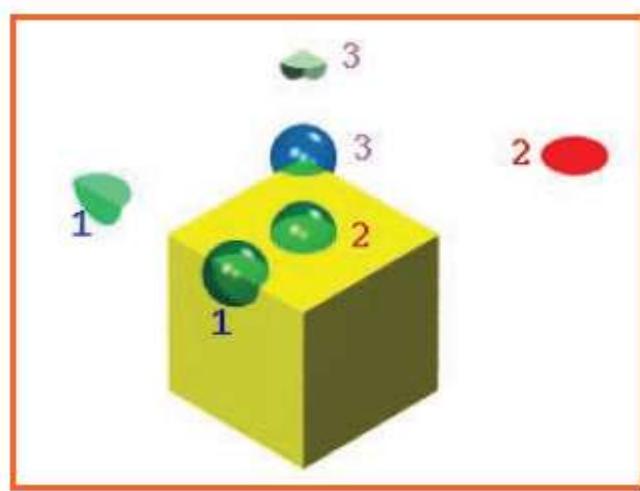


# Modelagem Geométrica

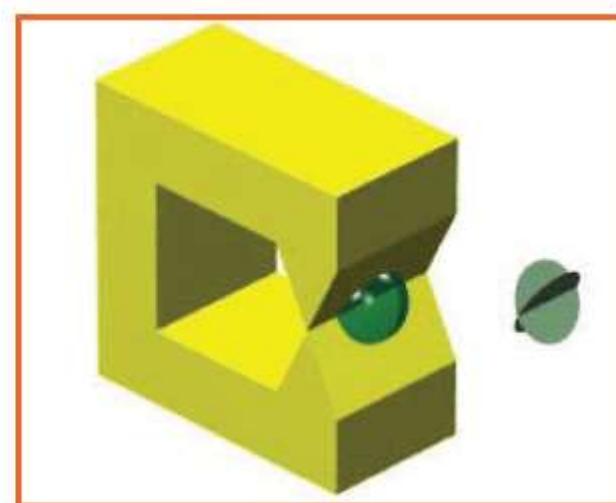
- **Modelagem *non-manifold***
  - Agrega todas as capacidades dos três tipos de modelagem anteriores.
  - Elimina as restrições ao domínio dos modelos analisados.
  - Permite a representação de estruturas internas ou pendentes de dimensão inferior.

# Modelagem Geométrica

Manifold



Non-manifold

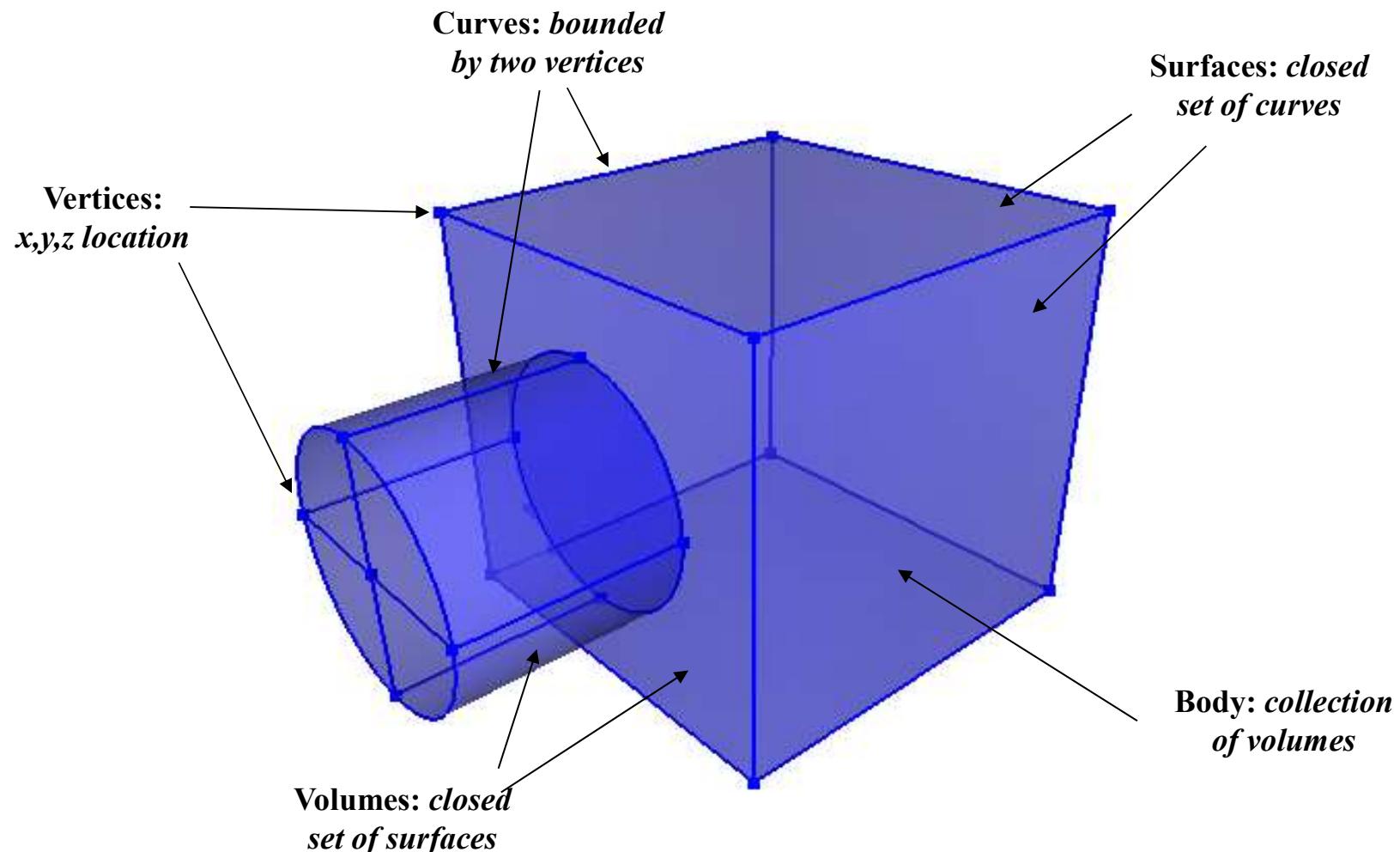


# Modelagem Geométrica

- **Topologia e Geometria**

- **Geometria** – conjunto de informações completas e essenciais para definir a forma e a localização espacial dos objetos.
- **Topologia** – subconjunto de informações obtidas a partir da geometria do objeto. Invariante após a aplicação de transformações geométricas no objeto.

# *Entidades Geométricas e Topológicas*



# Modelagem Geométrica

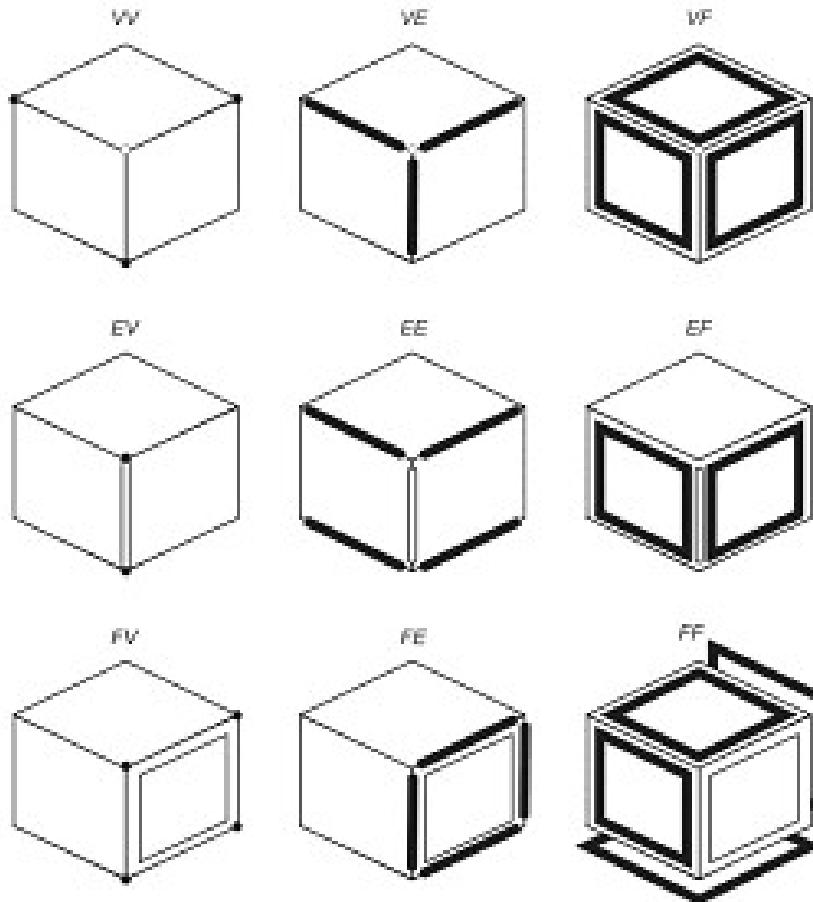
- **Uso da topologia como base de um sistema de modelagem:**
  - 1) Estabilidade do sistema
  - 2) Evitação de erros numéricos
  - 3) Separação das informações geométricas e topológicas

# Modelagem Geométrica

- **Relações de adjacência**

- Conectividade entre os elementos topológicos
- Extraídas das informações geométricas do modelo
- Utilização como base da estrutura de modelagem, garantindo a implementação de algoritmos mais simples e eficientes
- Determinação de um conjunto mínimo suficiente de relações de adjacência

# Modelagem Geométrica



**Relações de adjacência entre vértices, arestas e faces**

# Modelagem Geométrica

- **Estruturas de dados topológicas**
  - Sistematização e organização das informações topológicas de um modelo a partir do armazenamento de um conjunto suficiente de relações de adjacência.
  - Principais elementos topológicos: vértices, arestas e faces.
  - Elementos topológicos adicionais: *loops*, cascas, regiões, uso de vértices, semi-arestas, uso de arestas, uso de *loops*, uso de faces.

# Modelagem Geométrica

- **Estruturas de dados topológicas**
  - Exemplos de estruturas de dados consagradas em modelagem *manifold*:
    - *Winged-edge*
    - *Half-edge*
  - Estrutura de dados consagrada em modelagem *non-manifold*:
    - *Radial Edge*

# Topological Data Structure - Planar Subdivision

Induced by planar embedding of a graph.  
*Connected* if the underlying graph is.

$\text{Complexity} = \#\text{vertices} + \#\text{edges} + \#\text{faces}$

Typical operations:

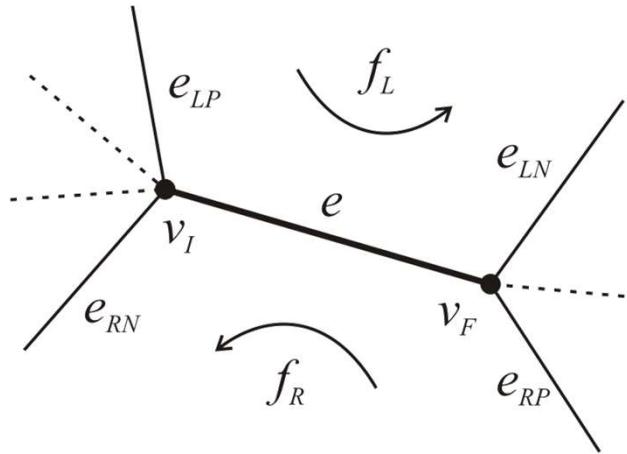
- ★ Walk around a face.
- ★ Access one face from an adjacent one via a common edge.
- ★ Visit all the edges adjacent to a vertex.

The diagram illustrates a planar subdivision graph. It features several green circular vertices connected by white edges. A specific face, labeled  $f$ , is highlighted with a light blue color. This face contains a smaller, nested pentagonal shape with its own edges and vertices, labeled "hole in  $f$ ". Labels "edge", "vertex", and "disconnected subdivision" are placed near the top left, middle left, and bottom left respectively. A green arrow points downwards from the word "edge".

# Estrutura de Dados Topológica

## *Winged-Edge*

# Winged-Edge (Baumgart, 1972)



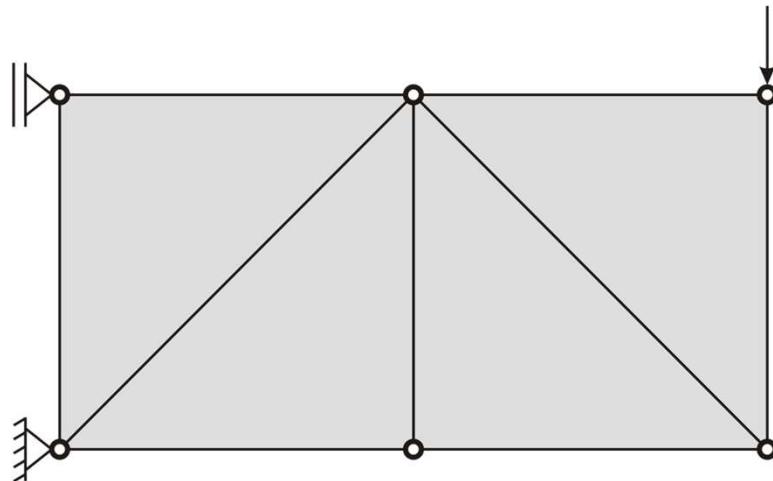
## Tabela de vértices

$v$	$x$	$y$	$z$	$e_I$

## Tabela de faces

$f$	$e_I$

## Tabela de arestas



geometria

ponto

curva

superfície

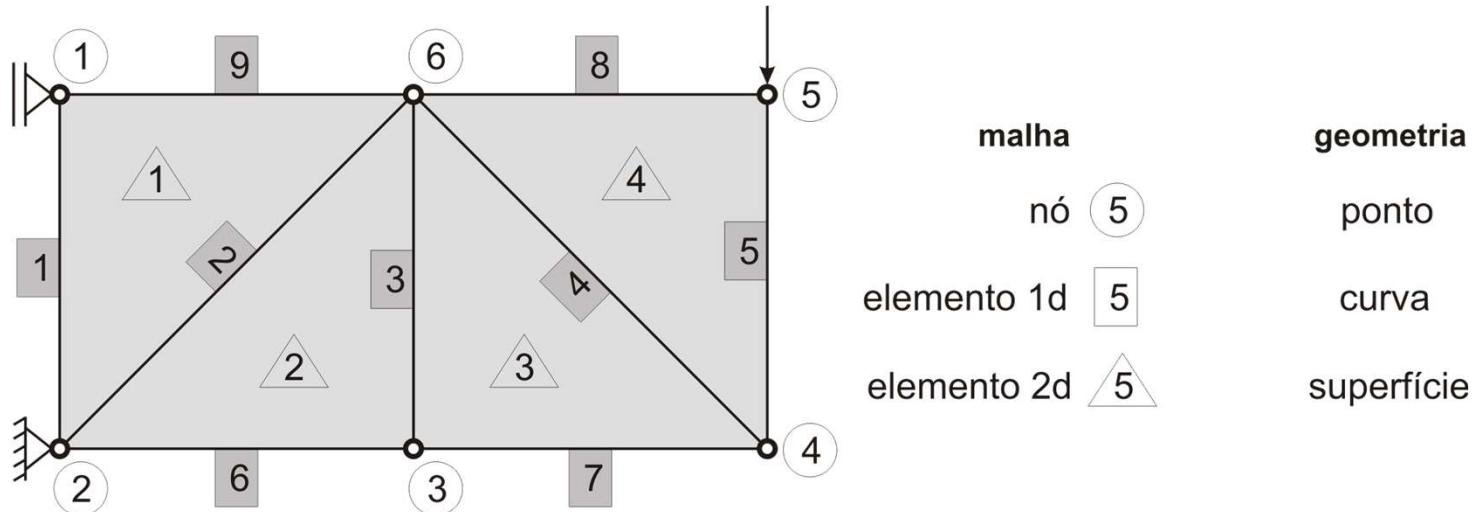


Tabela de nós

$N$	$x$	$y$	$z$
1	0	1	0
2	0	0	0
3	1	0	0
4	2	0	0
5	2	1	0
6	1	1	0

Tabela de conectividades

$E$	$N_1$	$N_2$	$N_3$
1	1	2	6
2	2	3	6
3	6	3	4
4	4	5	6

$E$	$N_1$	$N_2$
1	1	2
2	2	6
3	6	3
4	6	4
5	4	5
6	2	3
7	3	4
8	5	6
9	6	1

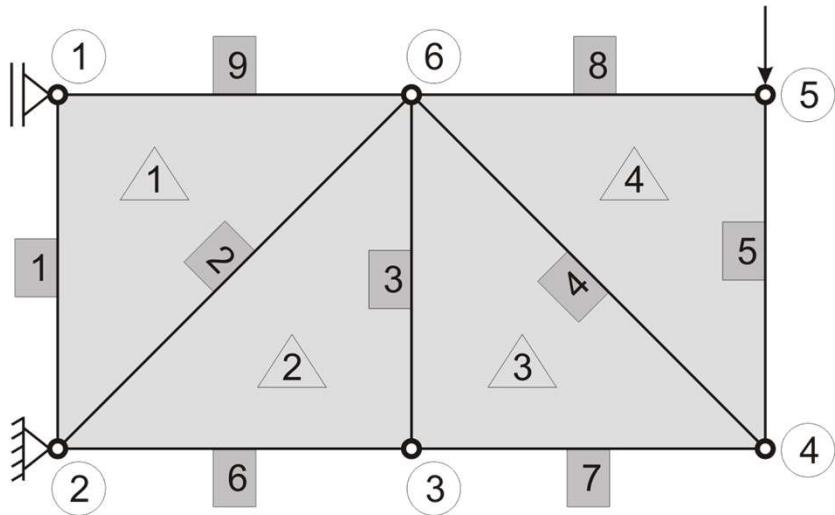


Tabela de nós

$N$	$x$	$y$	$z$
1	0	1	0
2	0	0	0
3	1	0	0
4	2	0	0
5	2	1	0
6	1	1	0

Tabela de conectividades

$E$	$N_1$	$N_2$	$N_3$
1	1	2	6
2	2	3	6
3	6	3	4
4	4	5	6

$E$	$N_1$	$N_2$
1	1	2
2	2	6
3	6	3
4	6	4
5	4	5
6	2	3
7	3	4
8	5	6
9	6	1

Tabela de vértices

$v$	$x$	$y$	$z$	$e_I$
1	0	1	0	1
2	0	0	0	6
3	1	0	0	7
4	2	0	0	4
5	2	1	0	8
6	1	1	0	2

Tabela de faces

$f$	$e_I$
0	1
1	2
2	6
3	4
4	4

Tabela de arestas

$e$	$v_I$	$v_F$	$f_L$	$f_R$	$e_{LP}$	$e_{LN}$	$e_{RP}$	$e_{RN}$
1	1	2	1	0	9	2	6	9
2	2	6	1	2	1	9	3	6
3	6	3	3	2	4	7	6	2
4	6	4	4	3	8	5	7	3
5	4	5	4	0	4	8	8	7
6	2	3	2	0	2	3	7	1
7	3	4	3	0	3	4	5	6
8	5	6	4	0	5	4	9	5
9	6	1	1	0	2	1	1	8

# Estrutura de Dados Topológica

## *Half-Edge*

# Half-Edge (Mäntylä, 1988)

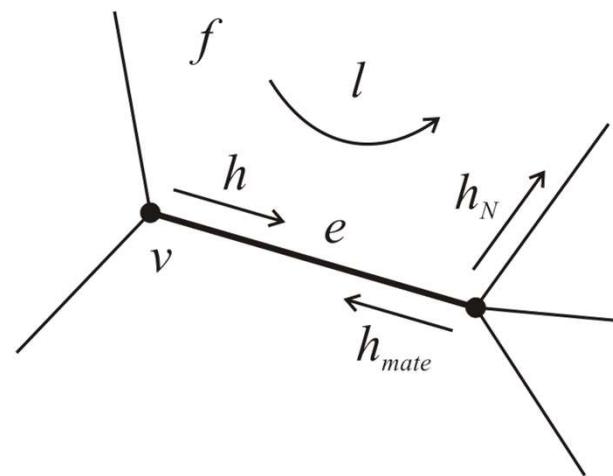


Tabela de vértices

$v$	$x$	$y$	$z$	$h$

Tabela de semi-arestas

$h$	$e$	$v$	$l$	$h_N$

Tabela de arestas

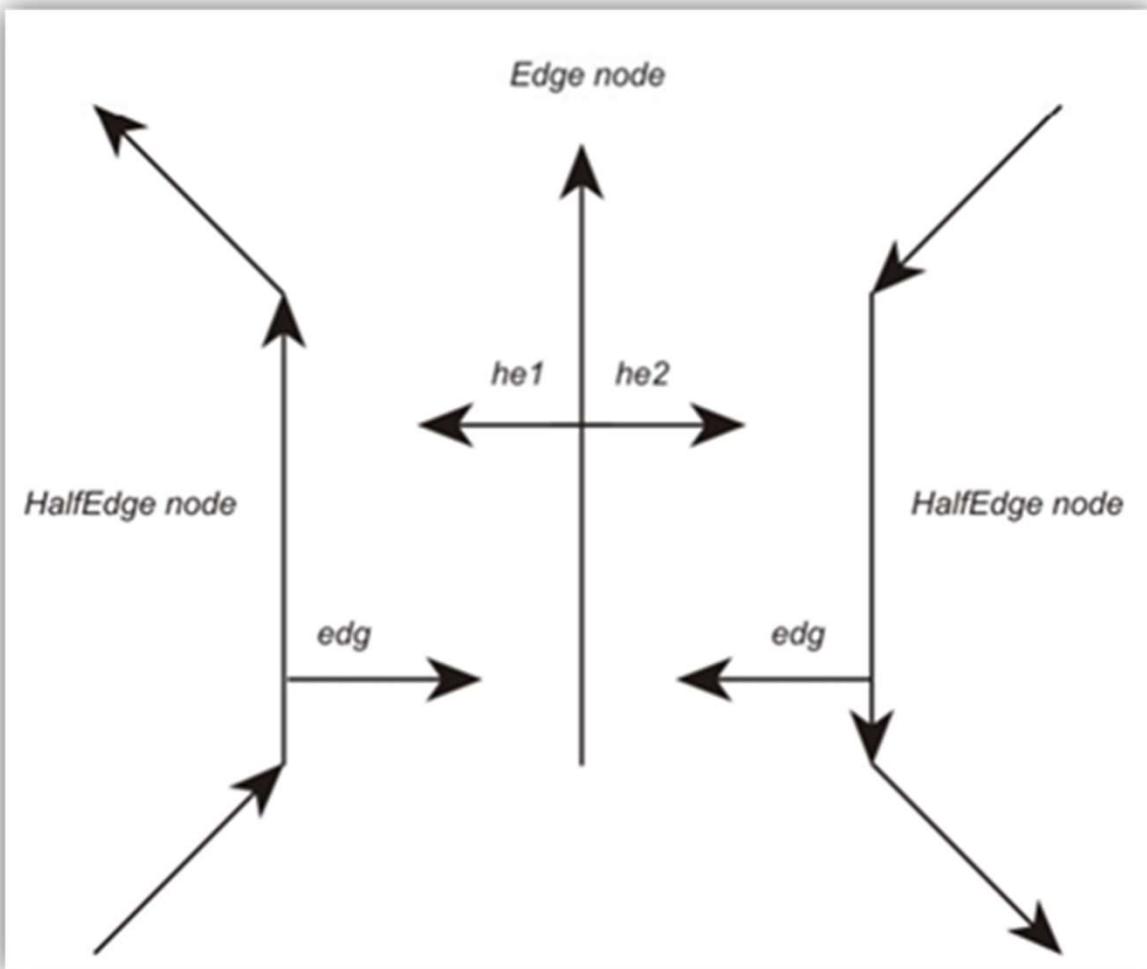
$e$	$h_1$	$h_2$

Tabela de laços

$l$	$h$	$f$	$l_N$

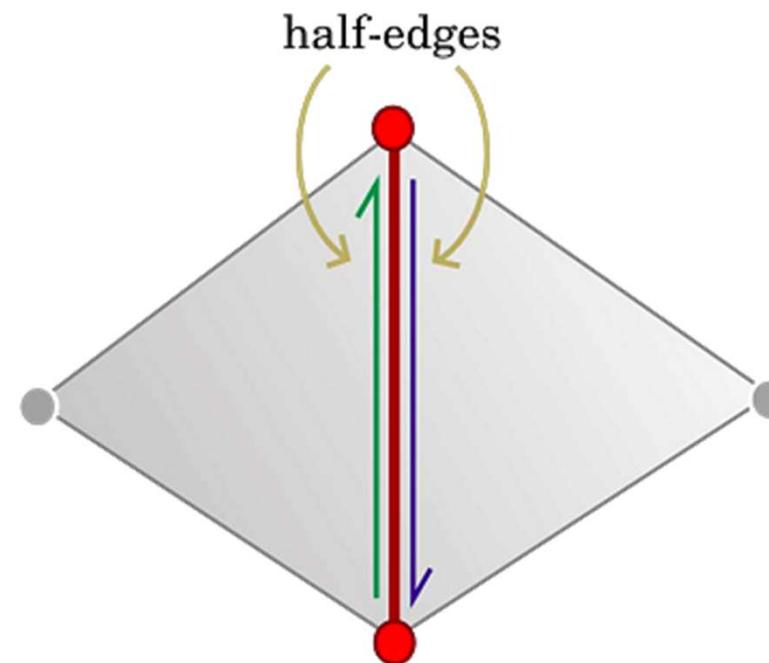
Tabela de faces

$f$	$l_{out}$	$l_{in}$

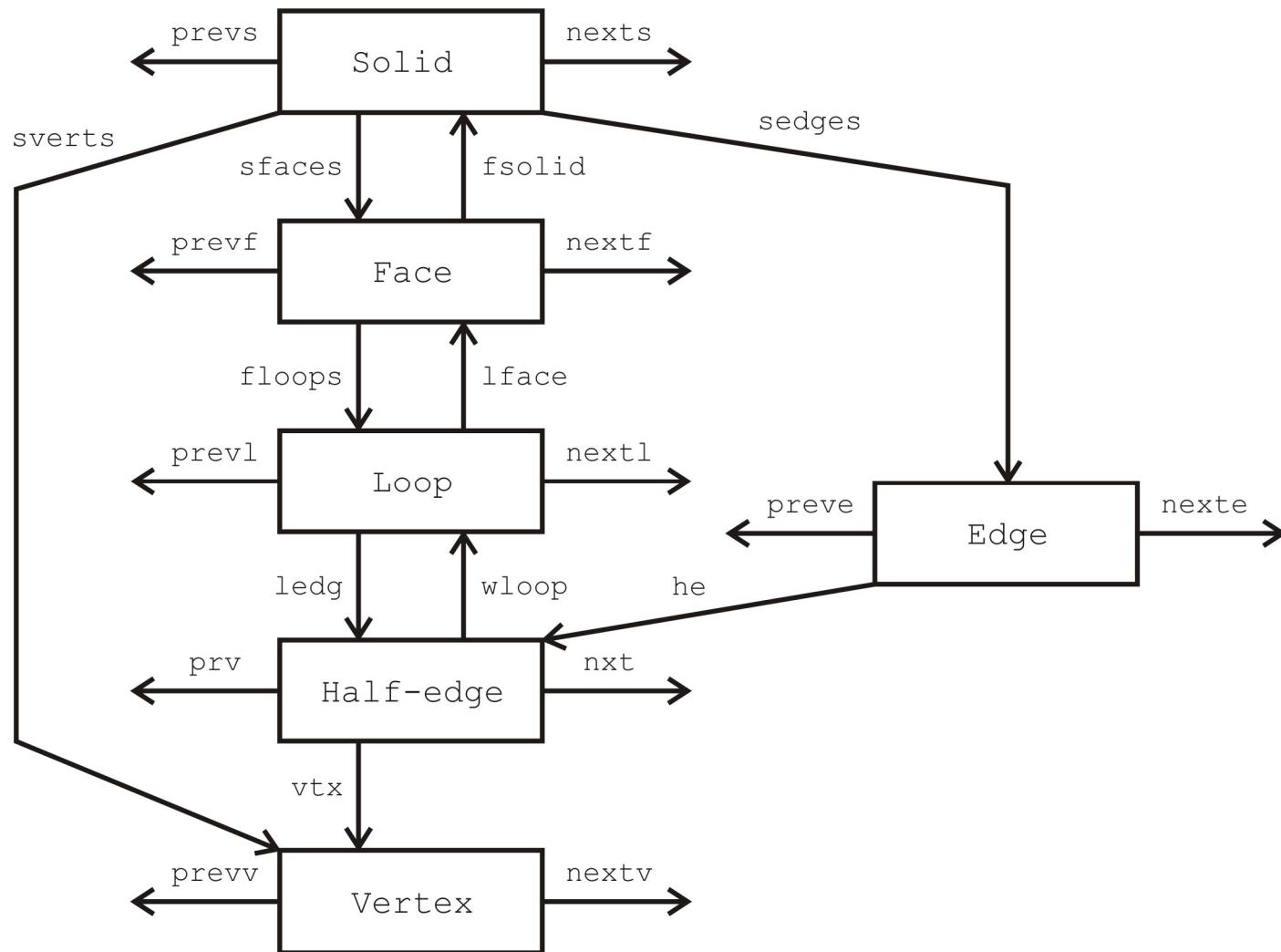


# Hierarchy of Topological Levels

- Solid
- Face
- Loop
- *Half-Edge*
  - Vertex
  - Edge\*



# Half-Edge Data Structure Entities



# Euler Operators

From a topological viewpoint, the simplest solids are those that have a closed orientable surface and no holes or interior voids. We assume that each face is bounded by a single loop of adjacent vertices; that is, the face is homeomorphic to a closed disk. Then the number of vertices  $V$ , edges  $E$ , and faces  $F$  of the solid satisfy the *Euler* formula:

$$V - E + F - 2 = 0$$

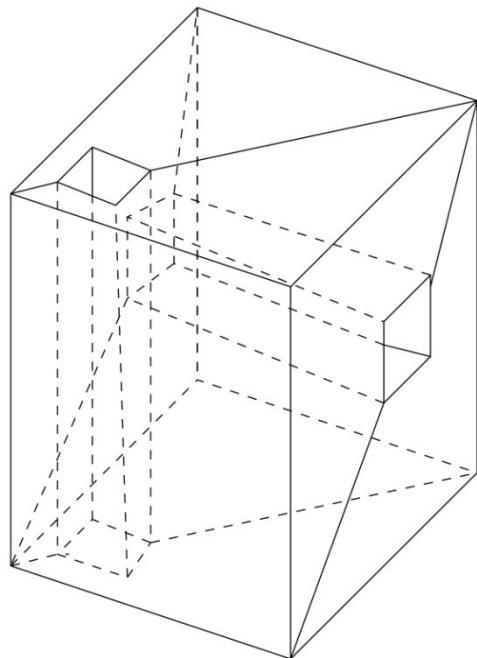
This fact is easily proved by induction on the surface structure. Extensions to this formula have been made that account for faces not being homeomorphic to closed disks, the solid surface not being without holes, and the solid having interior voids, as reviewed next.

[HOFFMANN1992]

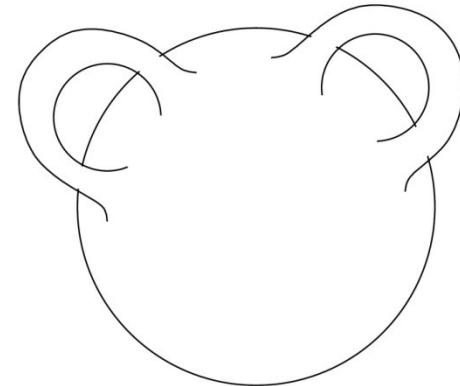
We consider the possibility that the solid has holes, but that it remains bounded by a single, connected surface. Moreover, each face is assumed to be homeomorphic to disk. For example, the torus has one hole, and the object in Figure **A** has two. It is a well-known fact that such solids are topologically equivalent, i.e., *homeomorphic*, to a sphere with zero or more handles. For example, the object of Figure **A** is homeomorphic to a sphere with two handles, the latter shown in Figure **B**. The number of handles is called the *genus* of the surface. In general, with a genus  $G$ , the numbers of vertices, edges, and faces obey the *Euler–Poincaré* formula:

$$V - E + F - 2(1 - G) = 0$$

[HOFFMANN1992]



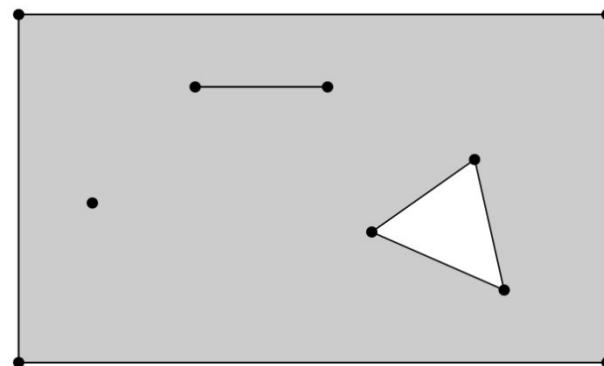
**Figure A** An Object with Two Holes and with Faces Homeomorphic to Disks



**Figure B** A Surface of Genus 2

Next, we further generalize by adding the possibility of internal voids. These voids are bounded by separate closed manifold surfaces, called *shells*. The number of shells will be denoted by  $S$ . Finally, we relax the requirement that a face is bounded by a single loop of vertices, but require that each face can be mapped to the plane. Thus, a sphere missing at least one point can be a face. In Figure C, a face is shown with four bounding loops. Note that one of these loops consists of a single vertex, and another one of two vertices connected by an edge. To account for faces of this complexity, we must count, for each face, the number of bounding vertex loops. For the face in Figure C, this number is four. With  $L$  the total number of loops, the relationship among the number of faces, edges, vertices, loops, and shells, and the sum  $G$  of each shell's genus, is then

$$V - E + F - (L - F) - 2(S - G) = 0$$



**Figure C** A Face with Four Bounding Loops

[HOFFMANN1992]

An example solid illustrating this relationship is shown in Figure D.

We may think of the quantities  $V$ ,  $E$ ,  $F$ ,  $L$ ,  $S$ , and  $G$  as existing in an abstract six-dimensional space. The relationship among them is then the equation of a hyperplane. Since the values of the variables must be non-negative integers, we might view the relation as defining a lattice on this hyperplane. For each solid with a given topological structure, there corresponds a point in this lattice.

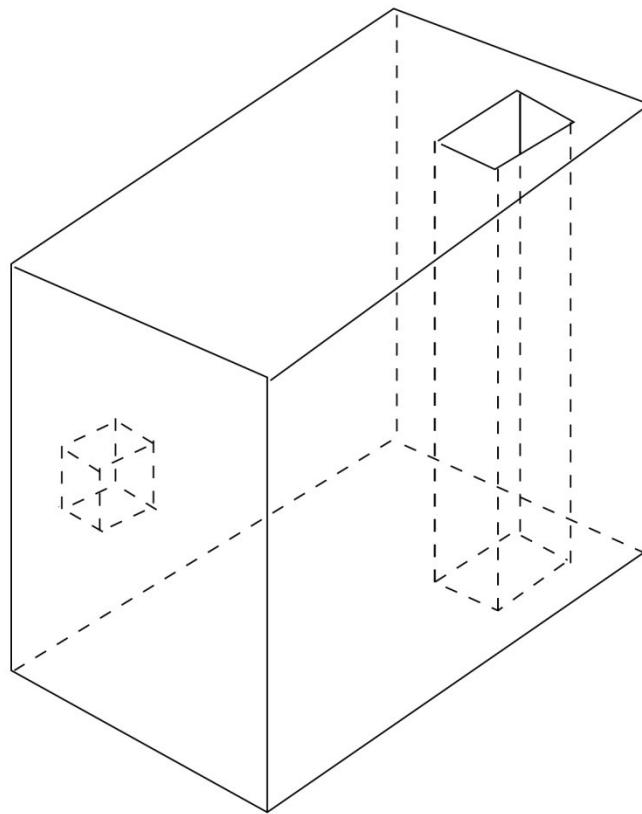


Figure D Solid with 24 Vertices, 36 Edges, 16 Faces, 18 Loops, 2 Shells, and Genus Sum 1

[HOFFMANN1992]

# Euler Operators

Operator Name	Meaning	V	E	F	L	S	G
MEV	Make an edge and a vertex	+1	+1				
MFE	Make a face and an edge		+1	+1	+1		
MSFV	Make a shell, a face and a vertex	+1		+1	+1	+1	
MSG	Make a shell and a hole					+1	+1
MEKL	Make an edge and kill a loop		+1		-1		

$$V - E + F - (L - F) - 2(S - G) = 0$$

# Euler Operators

Operator Name	Meaning	V	E	F	L	S	G
<b>MEV</b>	Make an edge and a vertex	+1	+1				
<b>MFE</b>	Make a face and an edge		+1	+1	+1		
<b>MSFV</b>	Make a shell, a face and a vertex	+1		+1	+1	+1	
<b>MSG</b>	Make a shell and a hole					+1	+1
<b>MEKL</b>	Make an edge and kill a loop		+1		-1		

Operator Name	Meaning	V	E	F	L	S	G	Result
MSFV	Make a shell, a face and a vertex	+1		+1	+1	+1		
MEV	Make an edge and a vertex	+1	+1					
MEV	Make an edge and a vertex	+1	+1					
MEV	Make an edge and a vertex	+1	+1					
MFE	Make a face and an edge		+1	+1		+1		
MFE	Make a face and an edge		+1	+1		+1		
MFE	Make a face and an edge		+1	+1		+1		

**MVFS**

$V = 1$  ( $H = 1$ )  $N = 0$   $P = 0$

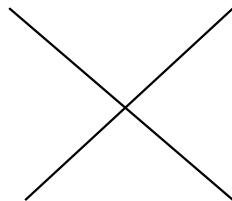
$H = 1$  ( $V = 1, E = 0, L = 1$ )  $N = 0$   $P = 0$

$E = 0$  ( $H1 = 0, H2 = 0$ )  $N = 0$   $P = 0$

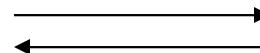
$L = 1$  ( $H = 1, F = 1$ )  $N = 0$   $P = 0$

$F = 1$  ( $S = 1, LOUT = 0 / LOOPS = 1$ )  $N = 0$   $P = 0$

$S = 1$  ( $V = 1, F = 1, E = 0$ )  $N = 0$   $P = 0$



**MVFS**



**KVFS**

**MVFS**

$V = 1$  ( $H = 1$ )  $N = 0$   $P = 0$

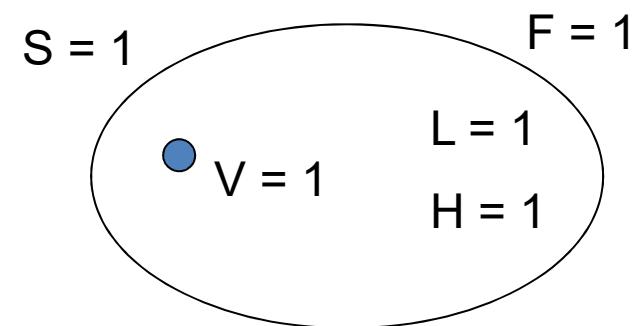
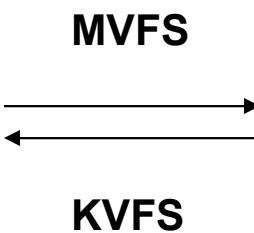
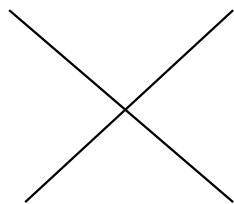
$H = 1$  ( $V = 1, E = 0, L = 1$ )  $N = 0$   $P = 0$

$E = 0$  ( $H1 = 0, H2 = 0$ )  $N = 0$   $P = 0$

$L = 1$  ( $H = 1, F = 1$ )  $N = 0$   $P = 0$

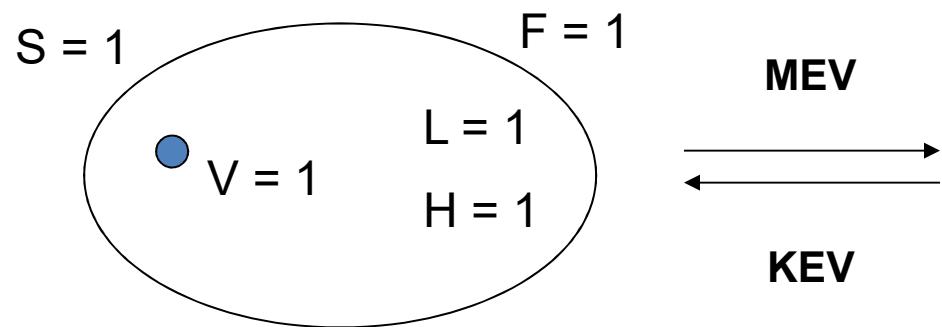
$F = 1$  ( $S = 1, LOUT = 0 / LOOPS = 1$ )  $N = 0$   $P = 0$

$S = 1$  ( $V = 1, F = 1, E = 0$ )  $N = 0$   $P = 0$



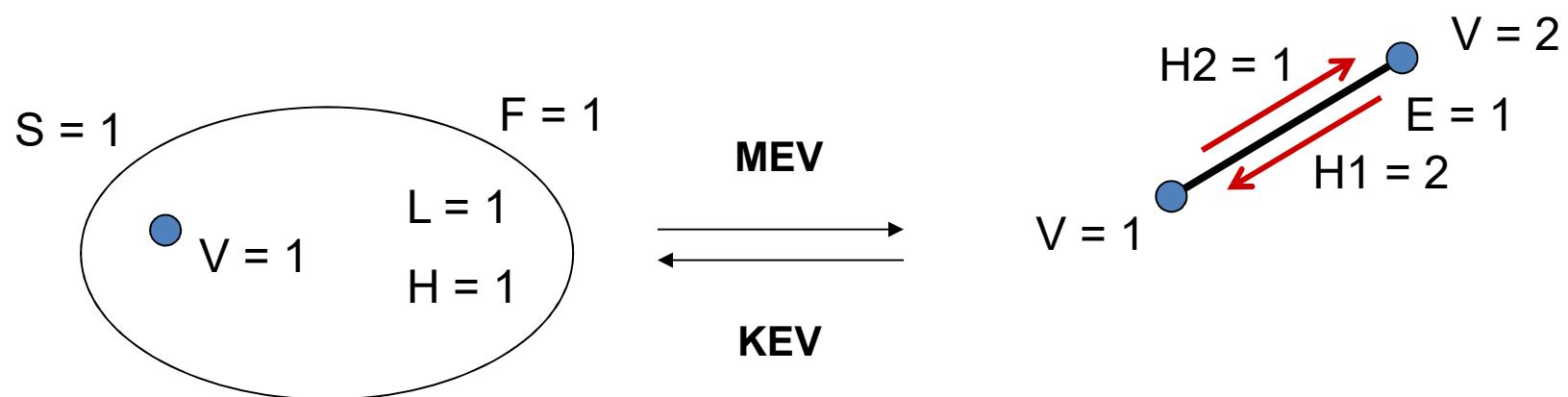
**MEV**

$V = 1 (H = 1) N = 0 P = 2$   
 $V = 2 (H = 2) N = 1 P = 0$   
 $H = 1 (V = 1, E = 1, L = 1) N = 2 P = 2$   
 $H = 2 (V = 2, E = 1, L = 1) N = 1 P = 1$   
 $E = 1 (H1 = 2, H2 = 1) N = 0 P = 0$   
 $L = 1 (H = 2, F = 1) N = 0 P = 0$   
 $F = 1 (S = 1, LOUT = 0 / LOOPS = 1) N = 0 P = 0$   
 $S = 1 (V = 1, F = 1, E = 1) N = 0 P = 0$



**MEV**

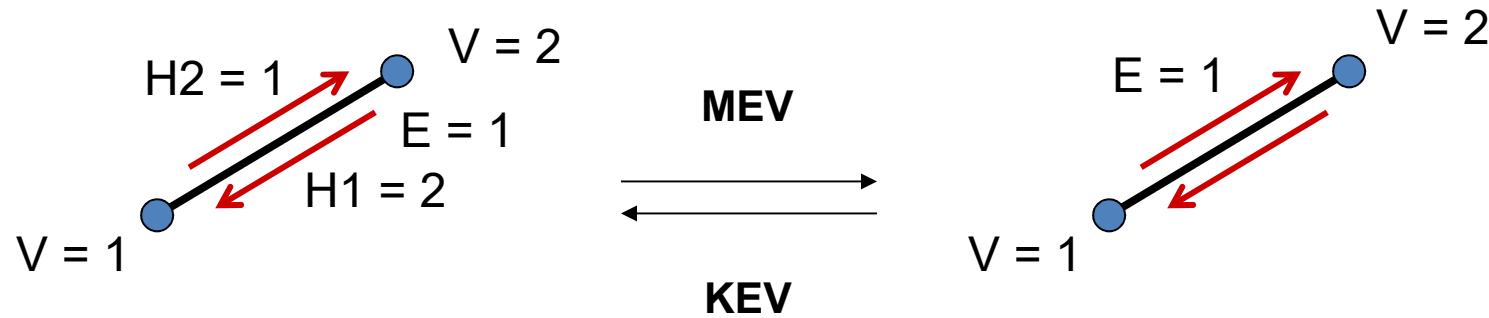
$V = 1 (H = 1) N = 0 P = 2$   
 $V = 2 (H = 2) N = 1 P = 0$   
 $H = 1 (V = 1, E = 1, L = 1) N = 2 P = 2$   
 $H = 2 (V = 2, E = 1, L = 1) N = 1 P = 1$   
 $E = 1 (H1 = 2, H2 = 1) N = 0 P = 0$   
 $L = 1 (H = 2, F = 1) N = 0 P = 0$   
 $F = 1 (S = 1, LOUT = 0 / LOOPS = 1) N = 0 P = 0$   
 $S = 1 (V = 1, F = 1, E = 1) N = 0 P = 0$



**MEV**

For a single strip there  
is no definition of the  
sequence (ccw nor ucw)

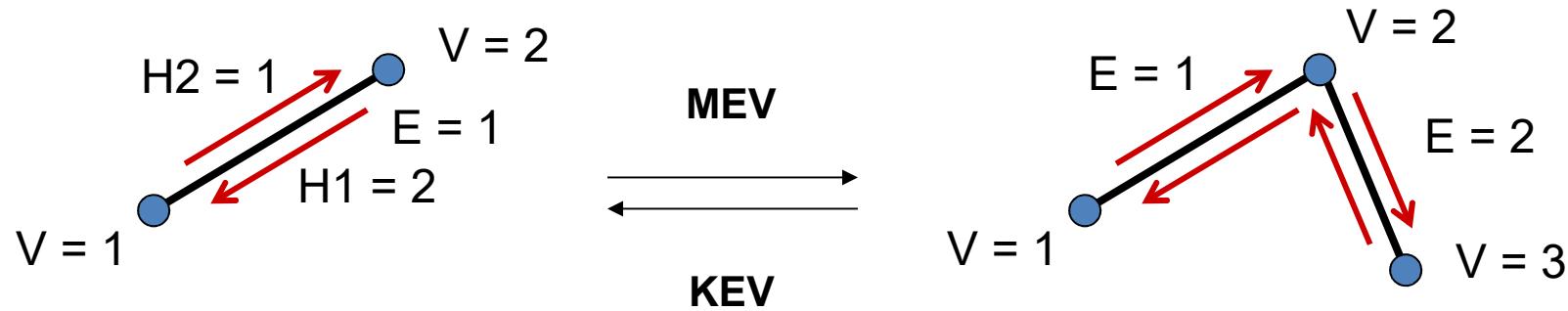
$V = 1 \ (H = 1) N = 0 P = 2$   
 $V = 2 \ (H = 3) N = 1 P = 3$   
 $V = 3 \ (H = 4) N = 2 P = 0$   
 $H = 1 (V = 1, E = 1, L = 1) N = 3 P = 2$   
 $H = 2 (V = 2, E = 1, L = 1) N = 1 P = 4$   
 $H = 3 (V = 2, E = 2, L = 1) N = 4 P = 1$   
 $H = 4 (V = 3, E = 2, L = 1) N = 2 P = 3$   
 $E = 1 (H1 = 2, H2 = 1) N = 0 P = 2$   
 $E = 2 (H1 = 3, H2 = 4) N = 1 P = 0$   
 $L = 1 (H = 2, F = 1) N = 0 P = 0$   
 $F = 1 (S = 1, LOUT = 0 / LOOPS = 1) N = 0 P = 0$   
 $S = 1 (V = 1, F = 1, E = 1) N = 0 P = 0$



**MEV**

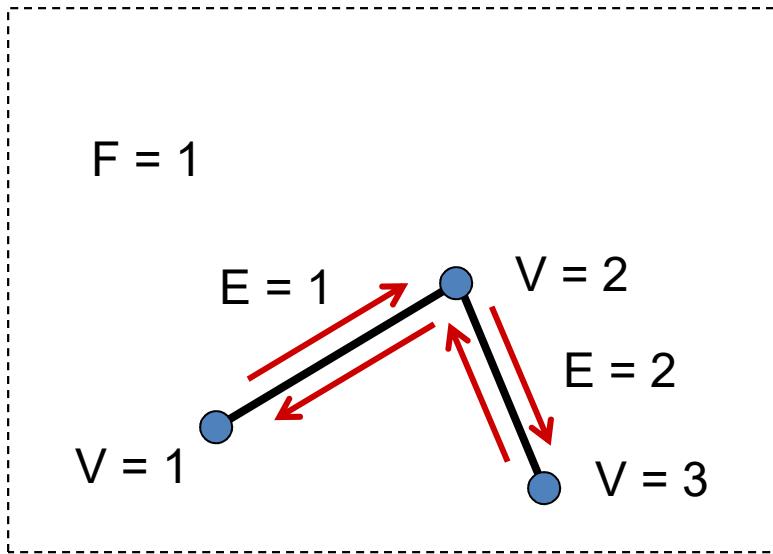
For a single strip there  
is no definition of the  
sequence (ccw nor ucw)

$V = 1 \ (H = 1) N = 0 P = 2$   
 $V = 2 \ (H = 3) N = 1 P = 3$   
 $V = 3 \ (H = 4) N = 2 P = 0$   
 $H = 1 (V = 1, E = 1, L = 1) N = 3 P = 2$   
 $H = 2 (V = 2, E = 1, L = 1) N = 1 P = 4$   
 $H = 3 (V = 2, E = 2, L = 1) N = 4 P = 1$   
 $H = 4 (V = 3, E = 2, L = 1) N = 2 P = 3$   
 $E = 1 (H1 = 2, H2 = 1) N = 0 P = 2$   
 $E = 2 (H1 = 3, H2 = 4) N = 1 P = 0$   
 $L = 1 (H = 2, F = 1) N = 0 P = 0$   
 $F = 1 (S = 1, LOUT = 0 / LOOPS = 1) N = 0 P = 0$   
 $S = 1 (V = 1, F = 1, E = 1) N = 0 P = 0$

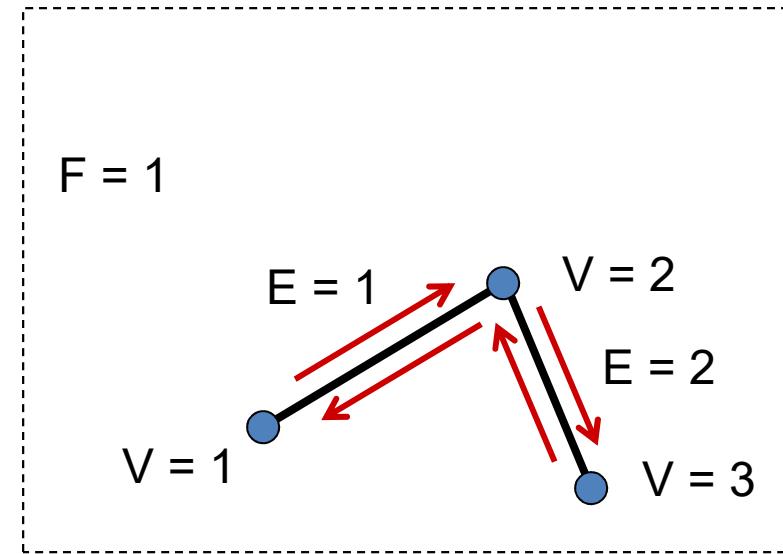


Defines the sequence if occurs two situations:

MEV

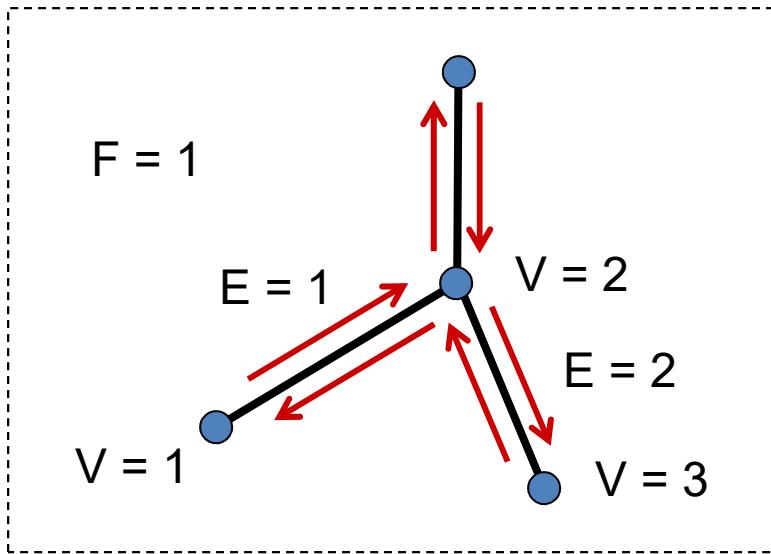


MEF

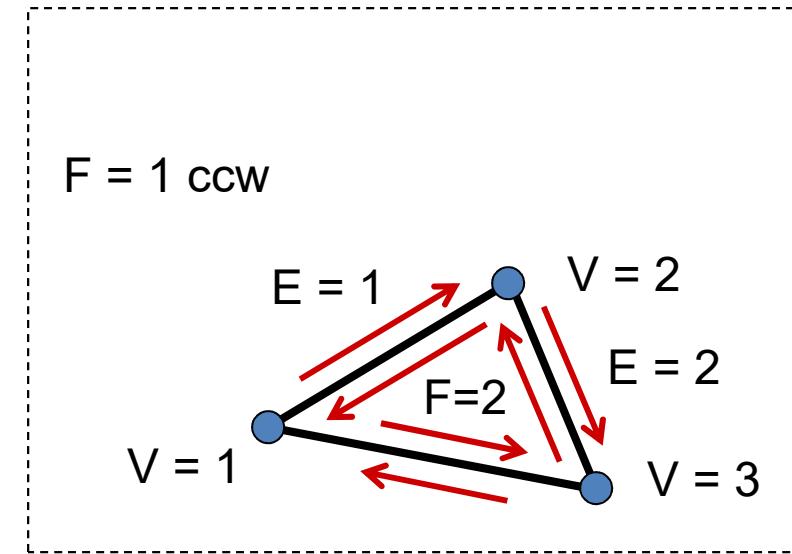


Defines the sequence if occurs two situations:

MEV

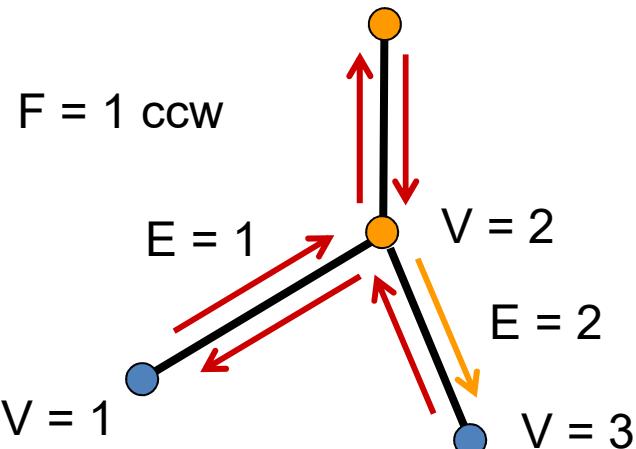


MEF



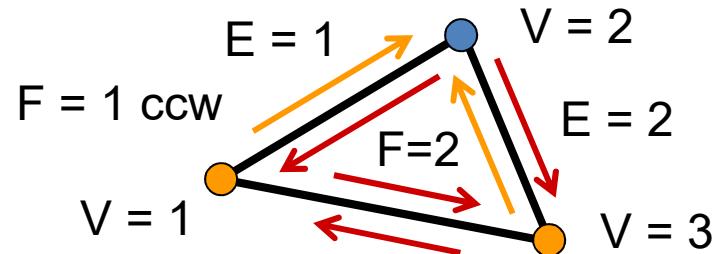
Which are the parameter to define each situation?

MEV

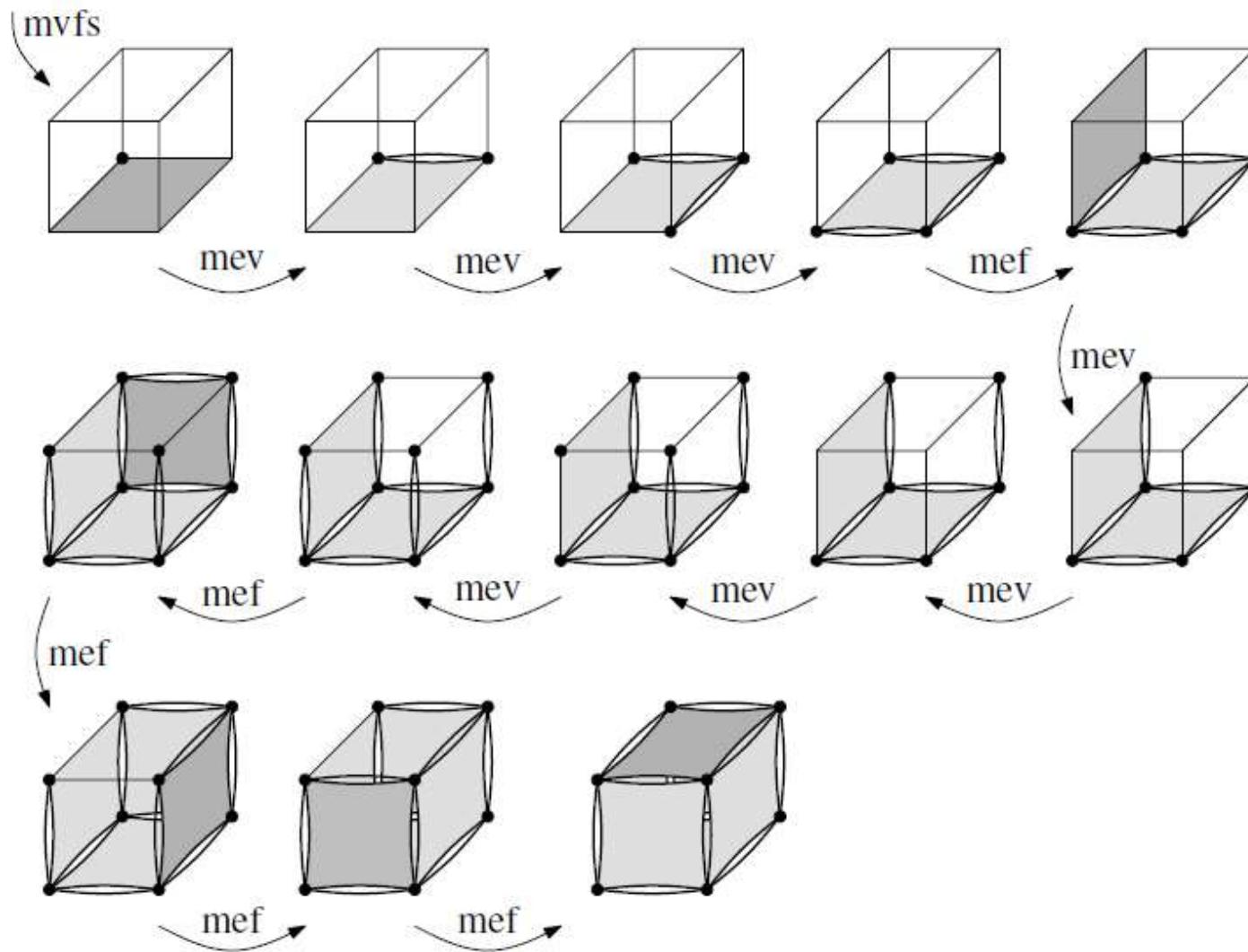


MEF

In this case, the half-edge of edge 2 (if it is the first parameter of MEF) receives the new face/loop. It is decided if the new loop area is positive! TIP: Always keep the first face with negative area (as the outside face).



# Using Euler Operators to Construct a Solid



# **Modelagem Geométrica Non-manifold**

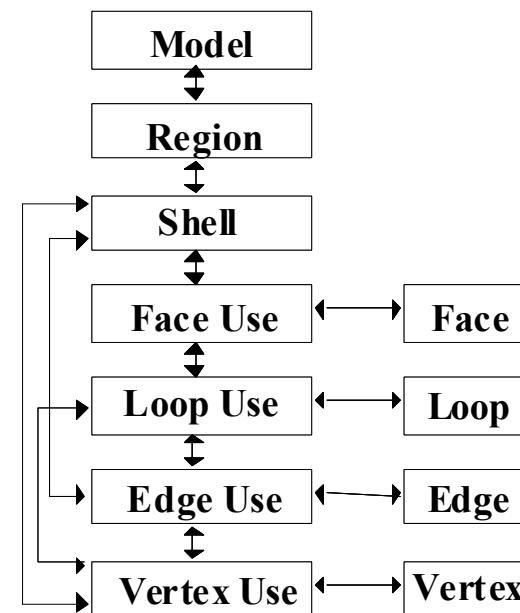
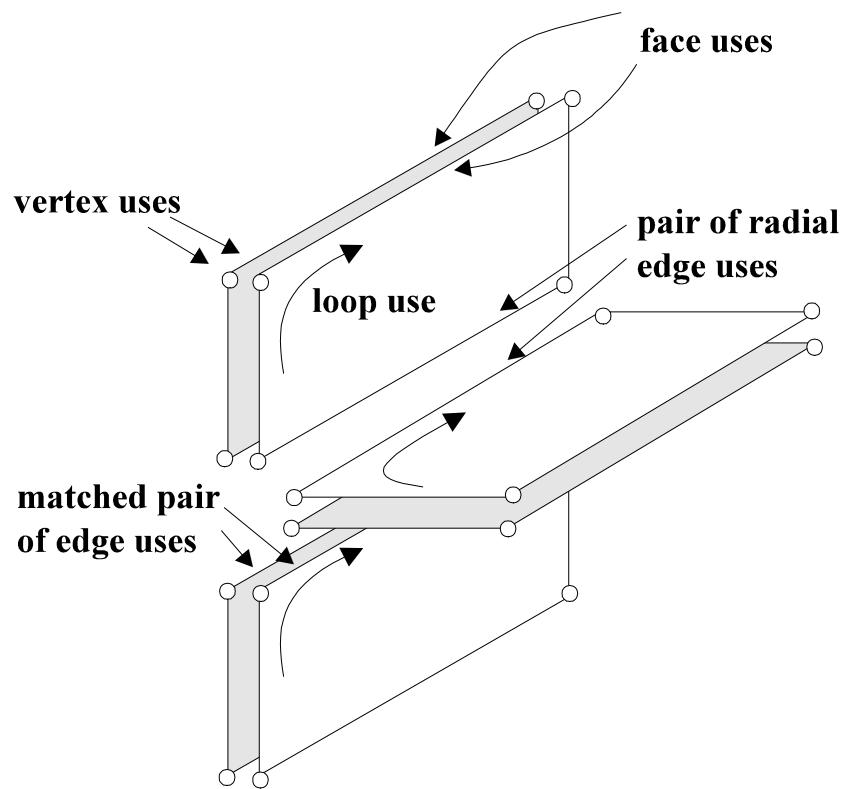
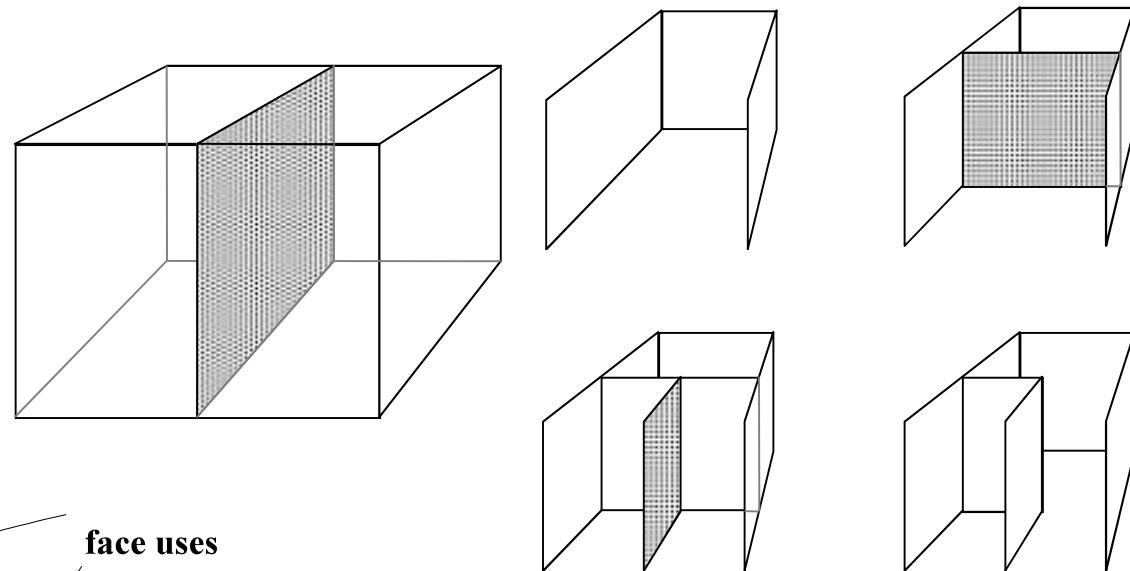
# Modelagem Geométrica

- **Topologia em representações *non-manifold***

➤ Áreas de aplicação da modelagem geométrica que usufruem das vantagens adicionais da representação *non-manifold*

- **Modelagem** – transição entre modelos, detecção de regiões, armazenamento de informações geométricas arbitrárias
- **Análise** – implementação de ferramentas de criação e análise simultâneas do modelo
- **Representação de objetos heterogêneos** – regiões com volumes comuns, faces coincidentes, estruturas internas, sólidos constituídos de materiais diferentes

## Radial-Edge (Weiler 1986)



# **Modelagem Paramétrica**

# Modelagem Paramétrica

**MCAD** (*Mechanical Computer Aided Design*)

Tecnologia relativamente nova.

# Modelagem Paramétrica

**MCAD (*Mechanical Computer Aided Design*)**

Tecnologia relativamente nova.

**Seu desenvolvimento vem ocorrendo desde +40 anos  
em paralelo ao desenvolvimento da tecnologia de hardware.**

Foi primeiramente apresentada no final de 1980, e recentemente se tornou o novo paradigma da projetos CAD mecânicos.

# Modelagem Paramétrica

**MCAD** (*Mechanical Computer Aided Design*)

Tecnologia relativamente nova.

Seu desenvolvimento vem ocorrendo desde +40 anos em paralelo ao desenvolvimento da tecnologia de hardware.

Foi primeiramente apresentada no final de 1980, e recentemente se tornou o novo paradigma da projetos CAD mecânicos.

**Tem elevado as tecnologias de CAD ao nível de ser uma ferramenta de projetos muito poderosa.**

Ela automatiza o projeto e os procedimentos de revisão pelo uso de *parametric features*.

# Modelagem Paramétrica

A palavra *paramétrico* significa que as definições da geometria do projeto, tal como dimensões, podem ser mudadas em qualquer momento no processo de projeto

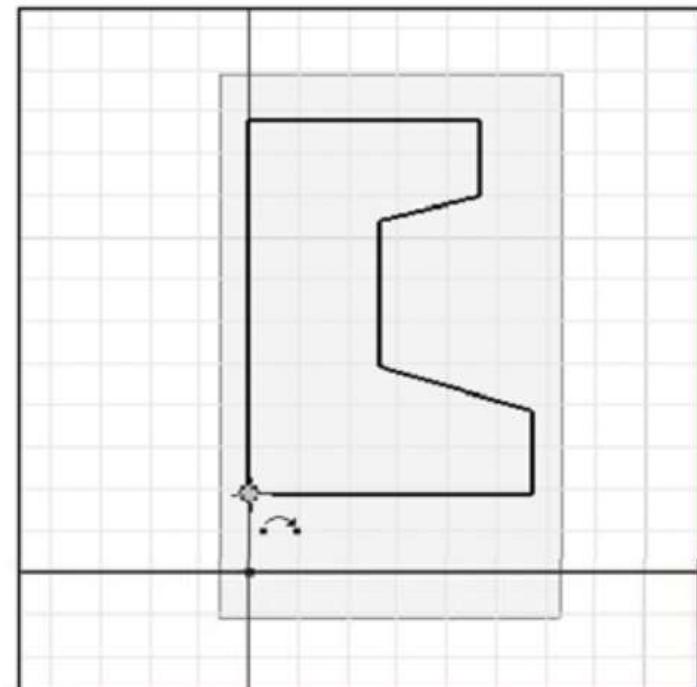
*Modelagem paramétrica* recebe esse nome por causa do projeto de parâmetros ou variáveis que são modificados durante o processo de simulação do projeto.

Vocabulário e Formalização:

- *Features*
- *Part* (Parte)
- *Constrains* (Restrições)
- *Assembly* (Montagem)
- *Sketch* (Esboço)

# Modelagem Paramétrica

*Sketcher*

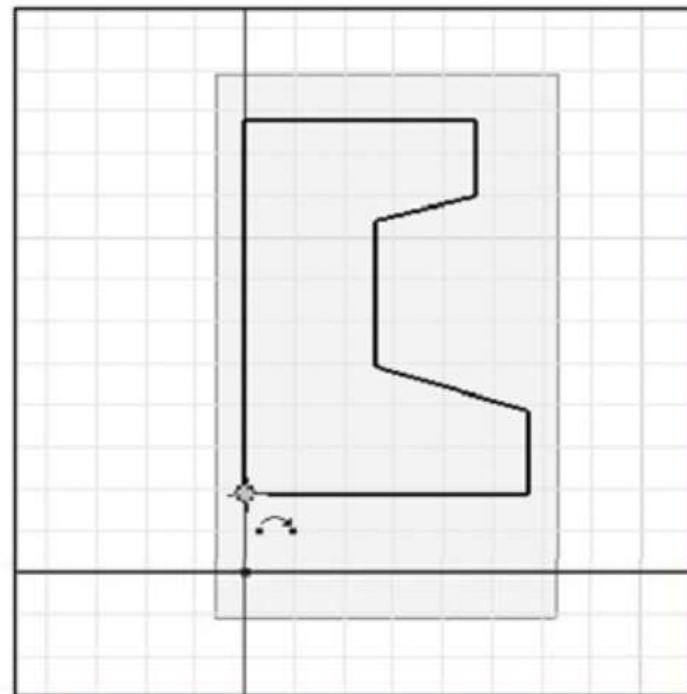


# Modelagem Paramétrica

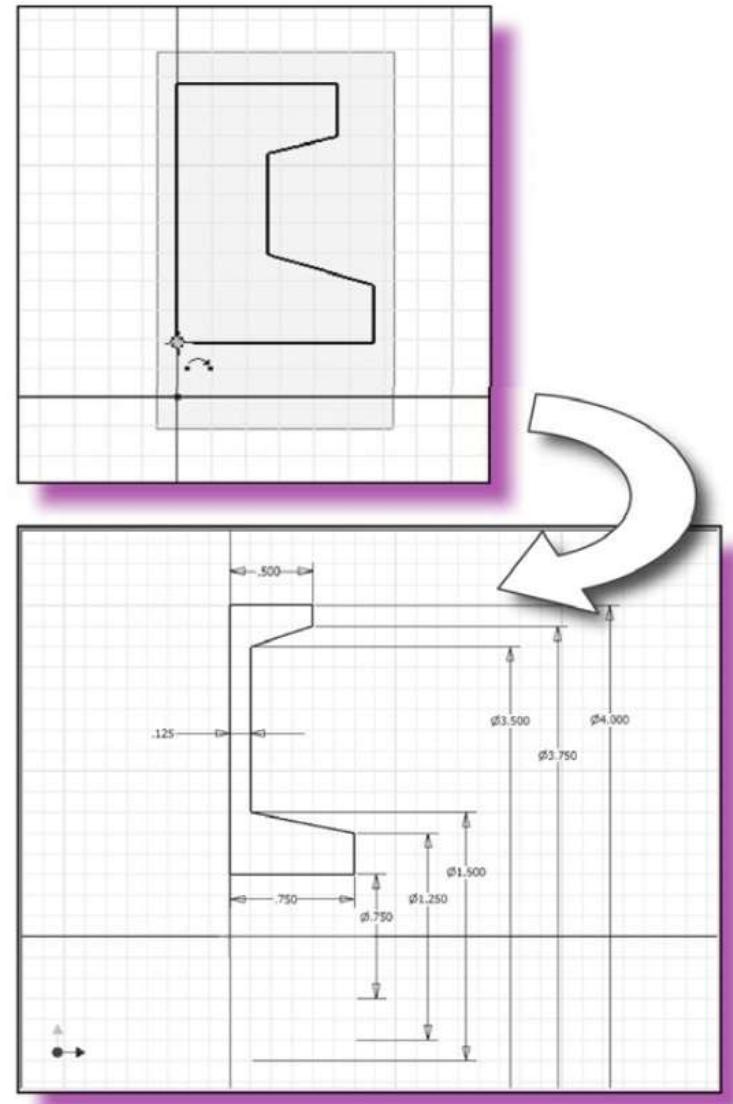
## Ferramentas Geométricas

- **Point:** Draws a point
- **Arc:** Draws an arc segment from center, radius, start angle and end angle
- **Circle:** Draws a circle from center and radius
- **2-point Line:** Draws a line segment from 2 points
- **Polyline (multiple-point line):** Draws a line made of multiple line segments
- **Rectangle:** Draws a rectangle from 2 opposite points
- **Fillet:** Makes a fillet between two lines joined at one point. Select both lines or click on the corner point, then activate the tool.
- **Trimming:** Trims a line, circle or arc with respect to the clicked point.
- **External Geometry:** Creates an edge linked to external geometry.
- **Construction Mode:** Toggles an element to/from construction mode. A construction object will not be used in a 3D geometry operation.

## *Sketcher*



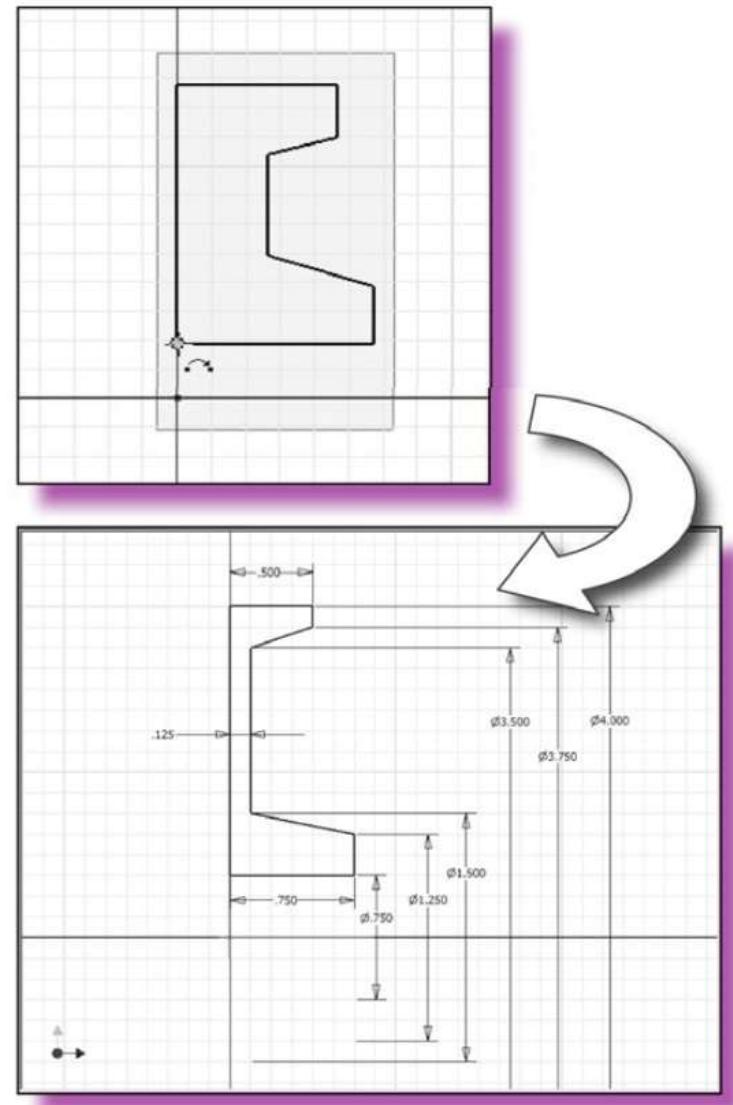
# Modelagem Paramétrica



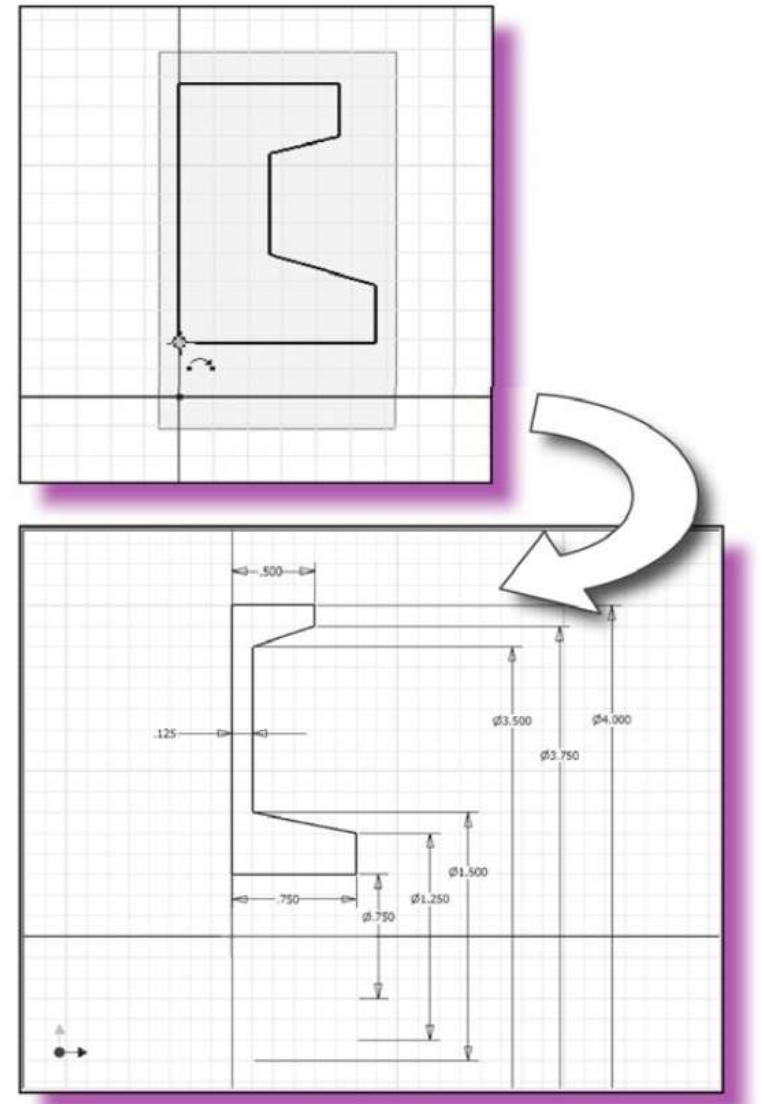
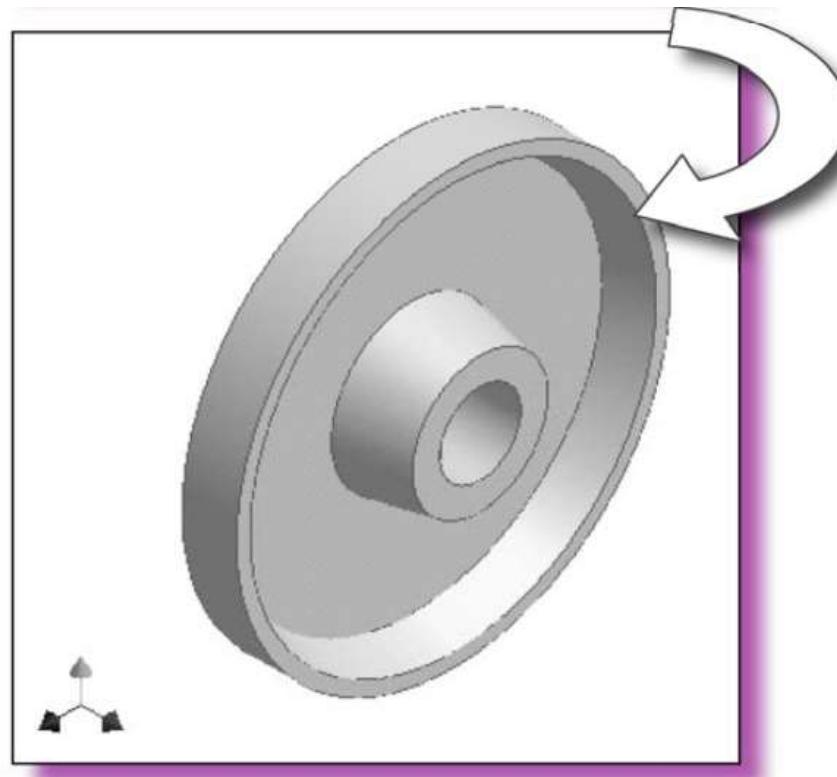
# Modelagem Paramétrica

## Aplicação das Restrições

- **Lock:** Creates a lock constraint on the selected item by setting vertical and horizontal dimensions relative to the origin (dimensions can be edited afterwards).
- **Coincident:** Creates a coincident (point-on-point) constraint between two selected points.
- **Point On Object:** Creates a point-on-object constraint on selected items.
- **Horizontal Distance:** Fixes the horizontal distance between 2 points or line ends. If only one item is selected, the distance is set to the origin.
- **Vertical Distance:** Fixes the vertical distance between 2 points or line ends. If only one item is selected, the distance is set to the origin.
- **Vertical:** Creates a vertical constraint to the selected lines or polylines elements. More than one object can be selected.
- **Horizontal:** Creates a horizontal constraint to the selected lines or polylines elements. More than one object can be selected.
- **Length:** Creates a length constraint on a selected line.
- **Radius:** Creates a radius constraint on a selected arc or circle.
- **Parallel:** Creates a parallel constraint between two selected lines.
- **Perpendicular:** Creates a perpendicular constraint between two selected lines.
- **InternalAngle:** Creates an internal angle constraint between two selected lines.
- **Tangent:** Creates a tangent constraint between two selected entities, or a colinear constraint between two line segments.
- **Equal Length:** Creates an equality constraint between two selected entities. If used on circle or arcs, the radius will be set equal.
- **Symmetric:** Creates a symmetric constraint between 2 points with respect to a line.



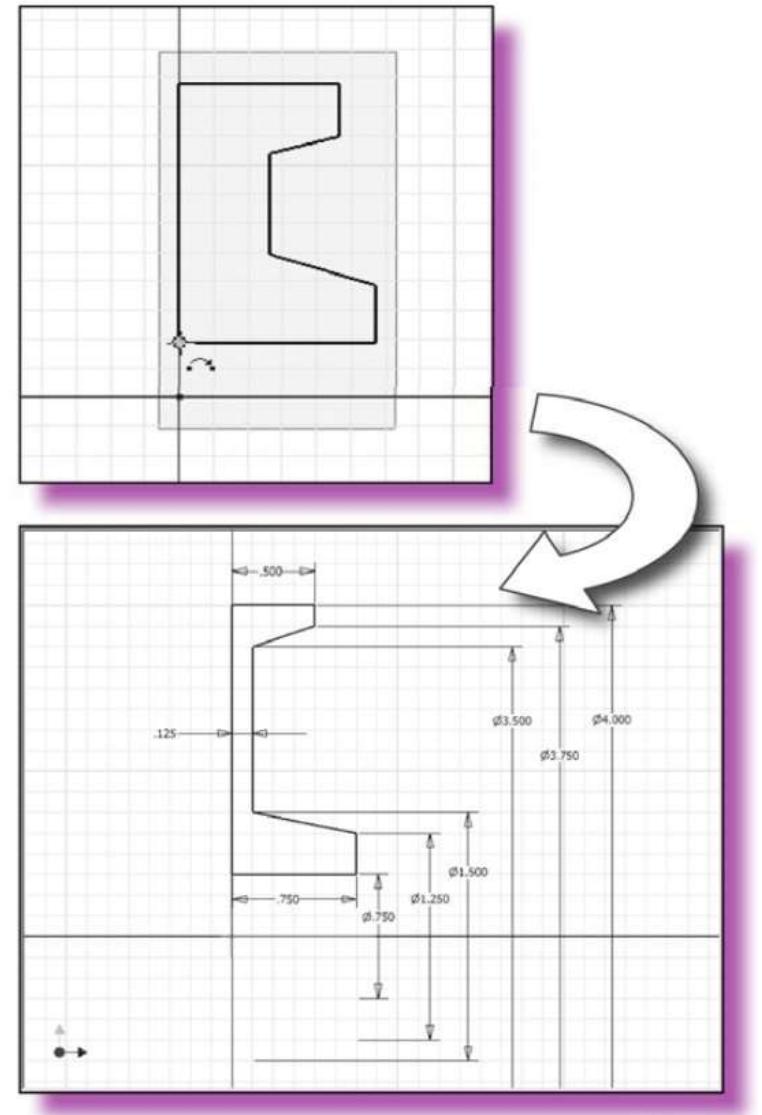
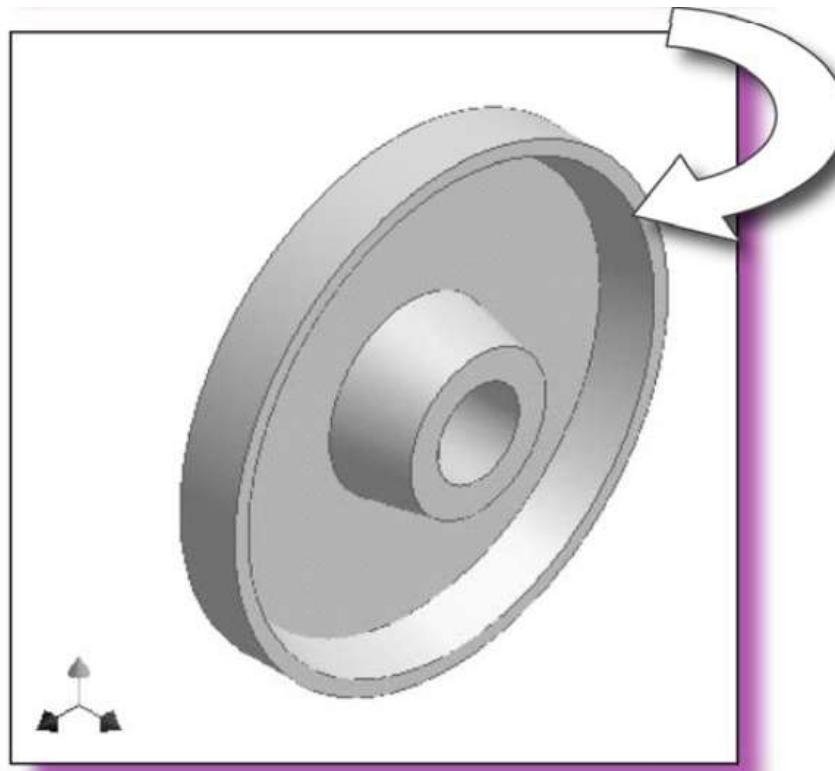
# Modelagem Paramétrica



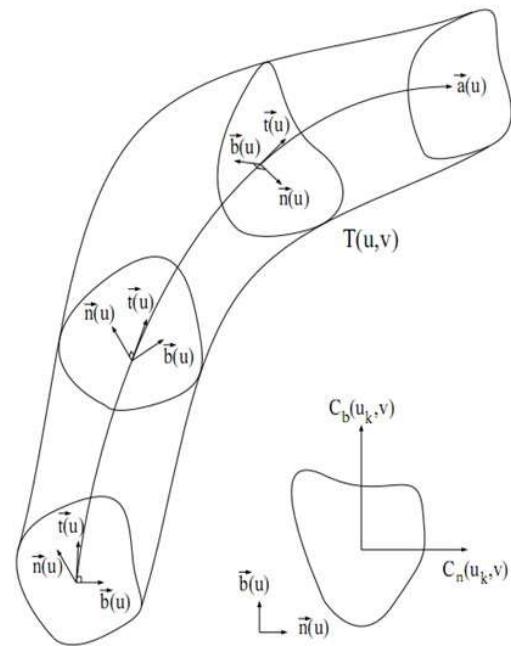
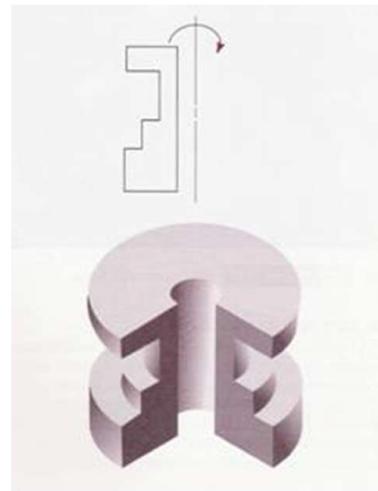
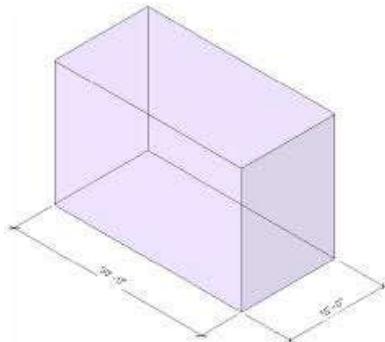
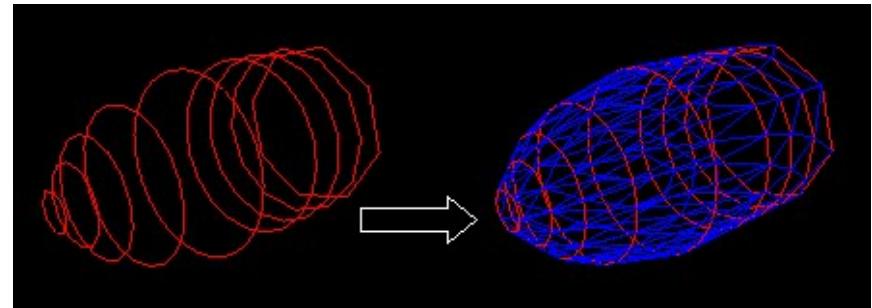
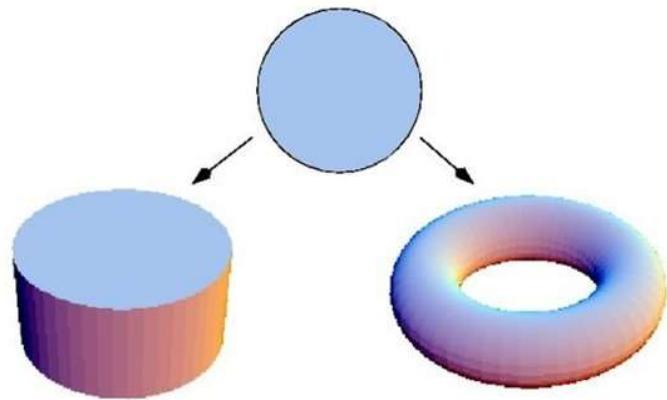
# Modelagem Paramétrica

*Features:*

- **Extrude** (Extrusão)
- **Revolute** (Revolução)
- **Sweep** (Varredura)
- **Loft**



# Modelagem Paramétrica



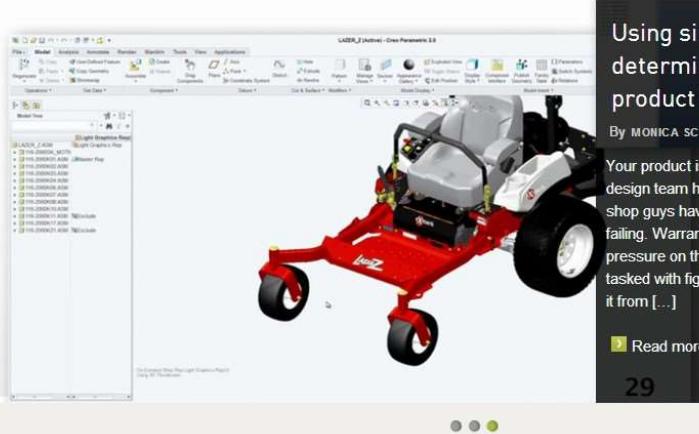
# Modelagem Paramétrica

PTC Creo®

ENGLISH

PRODUCT & SERVICE  
ADVANTAGE® PTC®

HOME REINVENTING DESIGN SEE CREO CREO REACTIONS BEHIND THE SCENES NEW HERE? Search



Using simulation to determine the root cause of product failure

By MONICA SCHNITGER | Published: APR 7, 2014 29

Your product is out in the marketplace. Your design team has done the best job it can. The shop guys have put their all into making it. But it's failing. Warranty claims are escalating and putting pressure on the bottom line and you, the person tasked with figuring out what's wrong and keeping it from [...]

[Read more](#)

29

Stay up to date. Subscribe.

Enter your email here

Submit

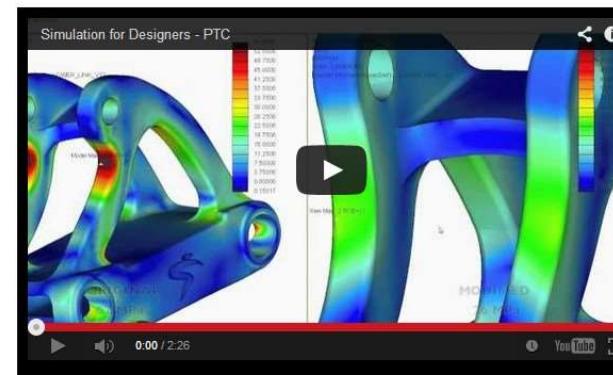
Connect with PTC

PTC Creo®

ENGLISH

PRODUCT & SERVICE  
ADVANTAGE® PTC®

HOME REINVENTING DESIGN SEE CREO CREO REACTIONS BEHIND THE SCENES NEW HERE? Search



Free Webinar Series: Learn the Benefits of PTC Simulation Solutions

By MARK BRUNELLI | Published: APR 16, 2014

Problems found earlier in the design process reduce development costs and save time. See how simulating the performance of your design early and often can reduce physical prototyping and enable you to make better design decisions. In just 25 minutes, see how PTC's simulation solutions can help you accurately: Predict product performance while you design [...]

[Read more](#)

[Leave a comment](#)

...

Stay up to date. Subscribe.

Enter your email here

Submit

Connect with PTC

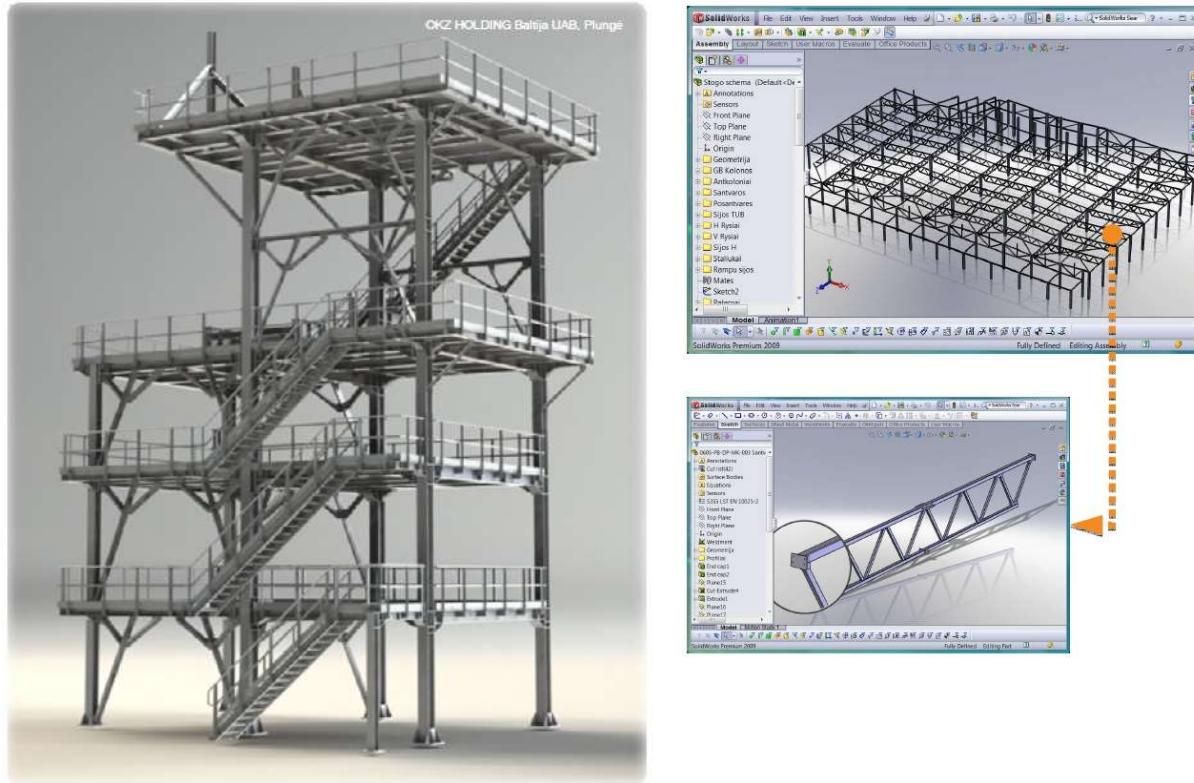


# Modelagem Paramétrica



[POPOV2009]

# Modelagem Paramétrica

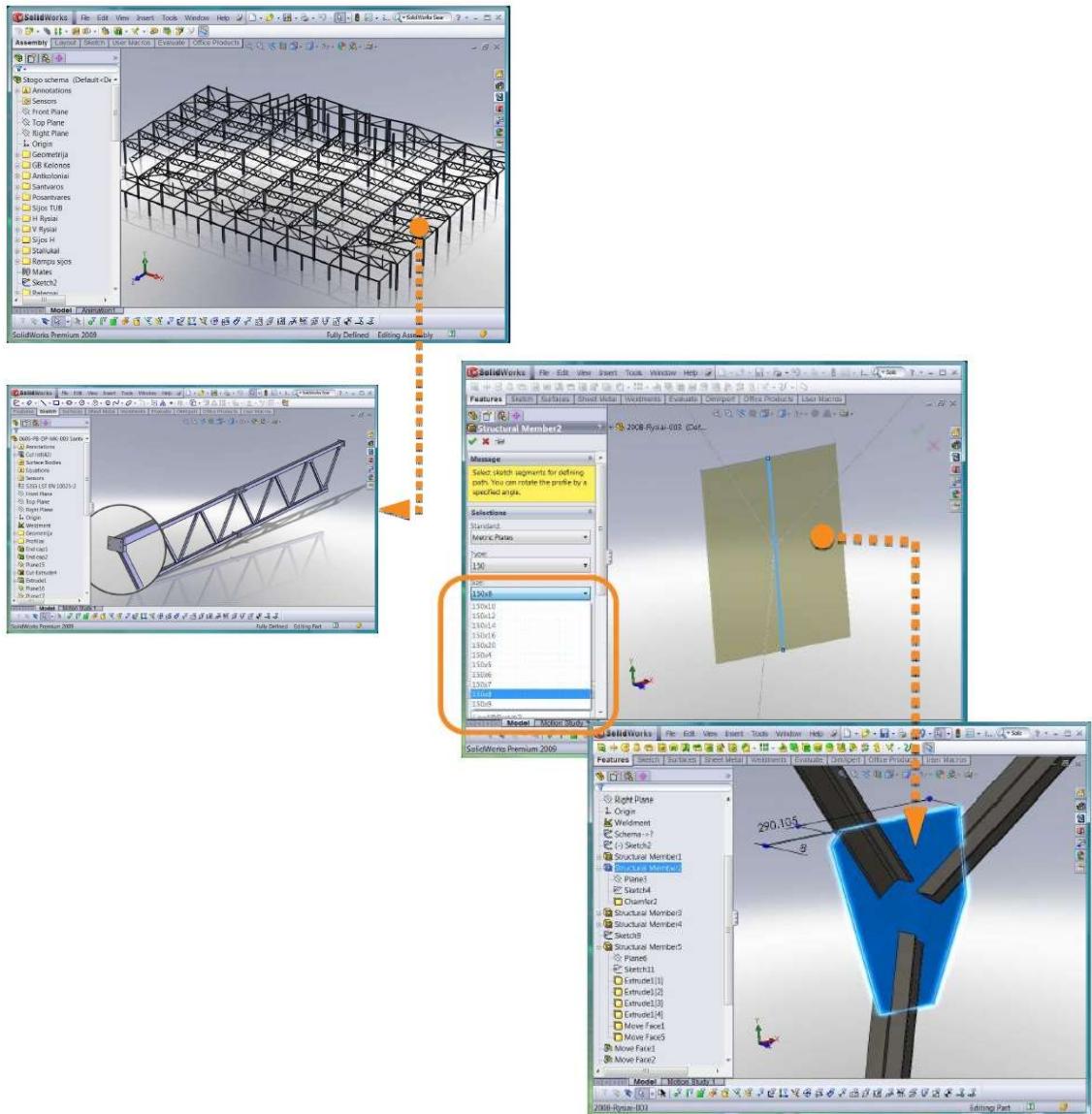


[POPOV2009]

# Modelagem Paramétrica



[POPOV2009]

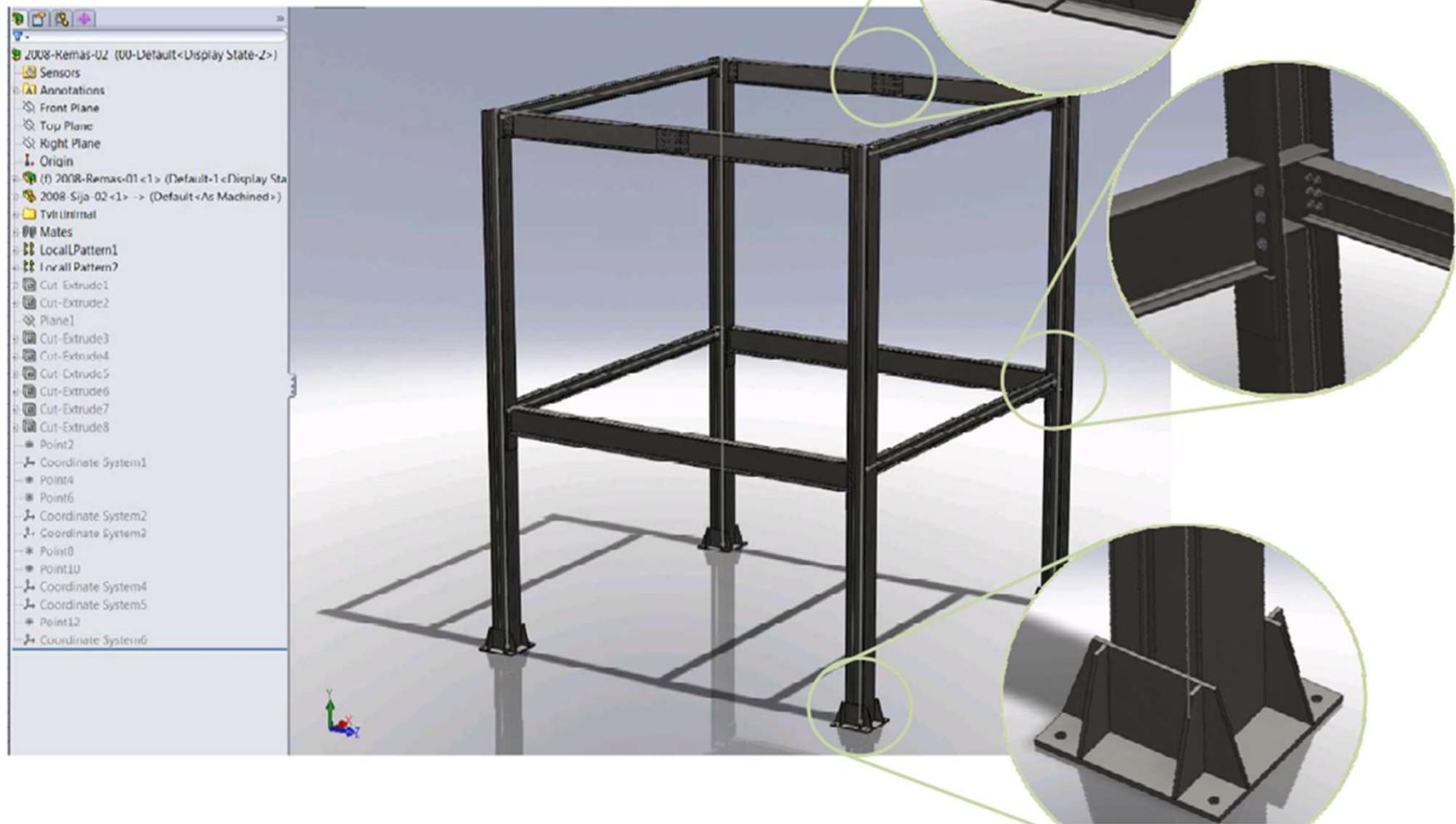




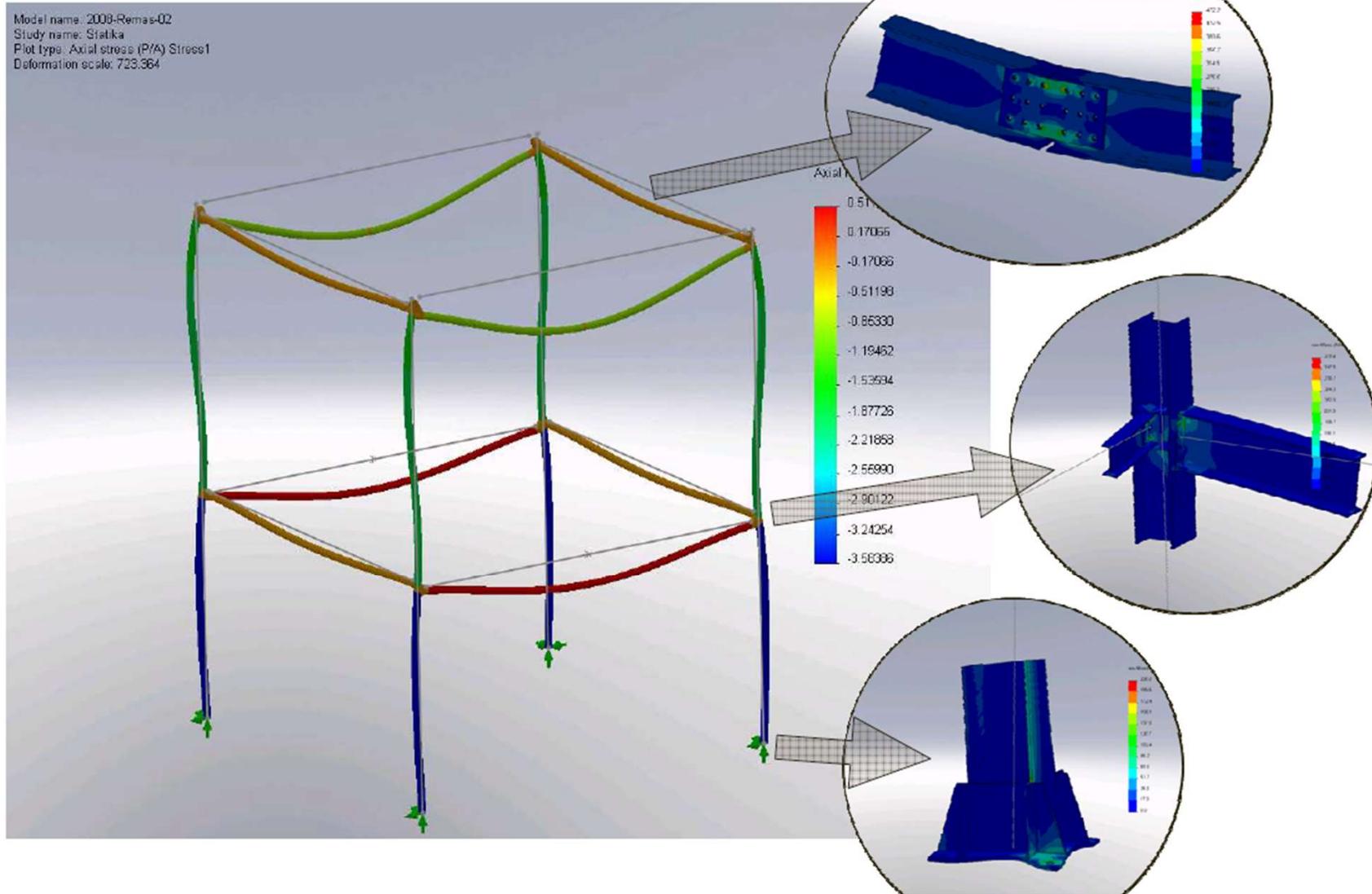
[POPOV2009]



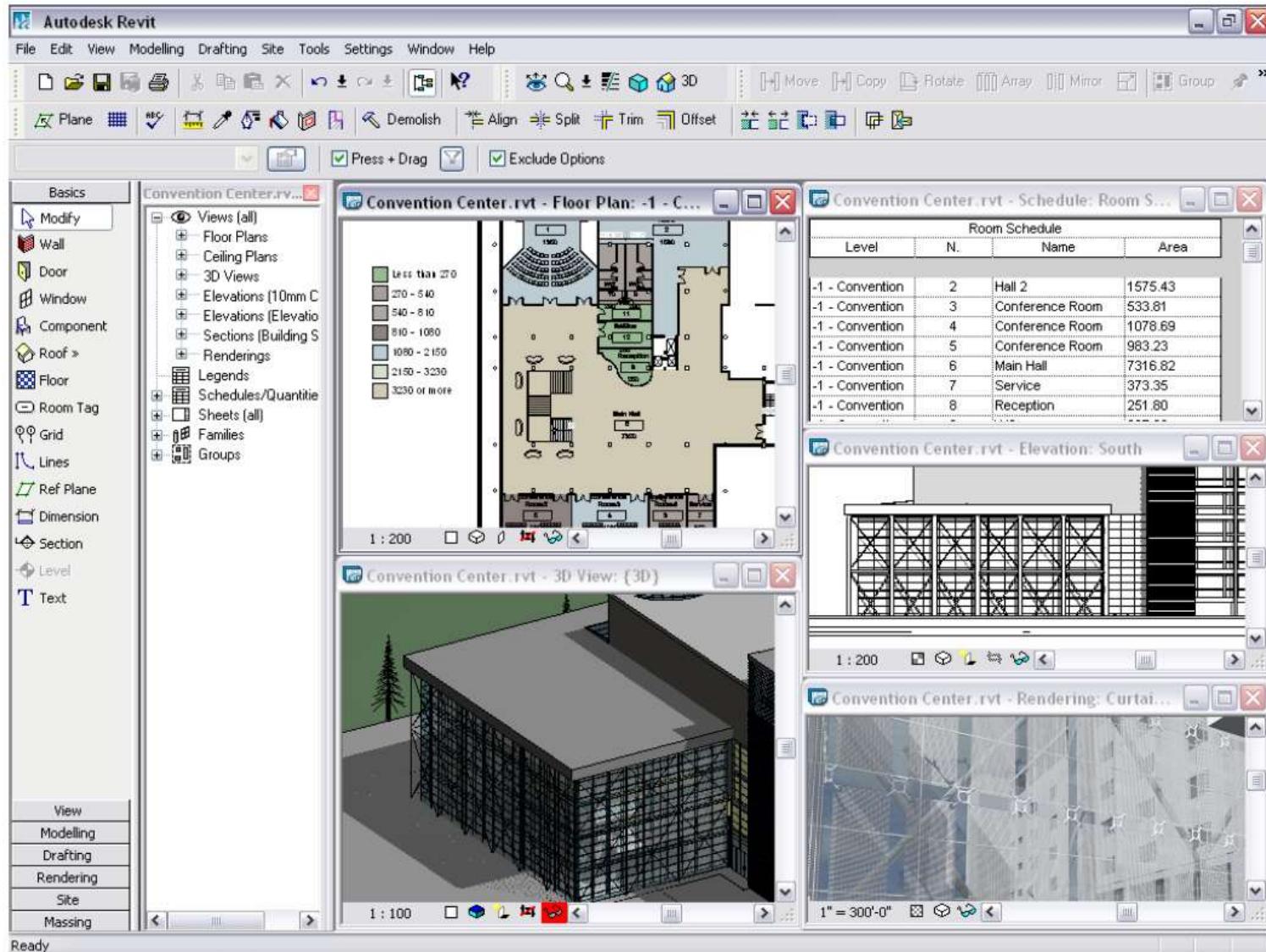
[POPOV2009]



## [POPOV2009]



# Modelagem Paramétrica



# BIM

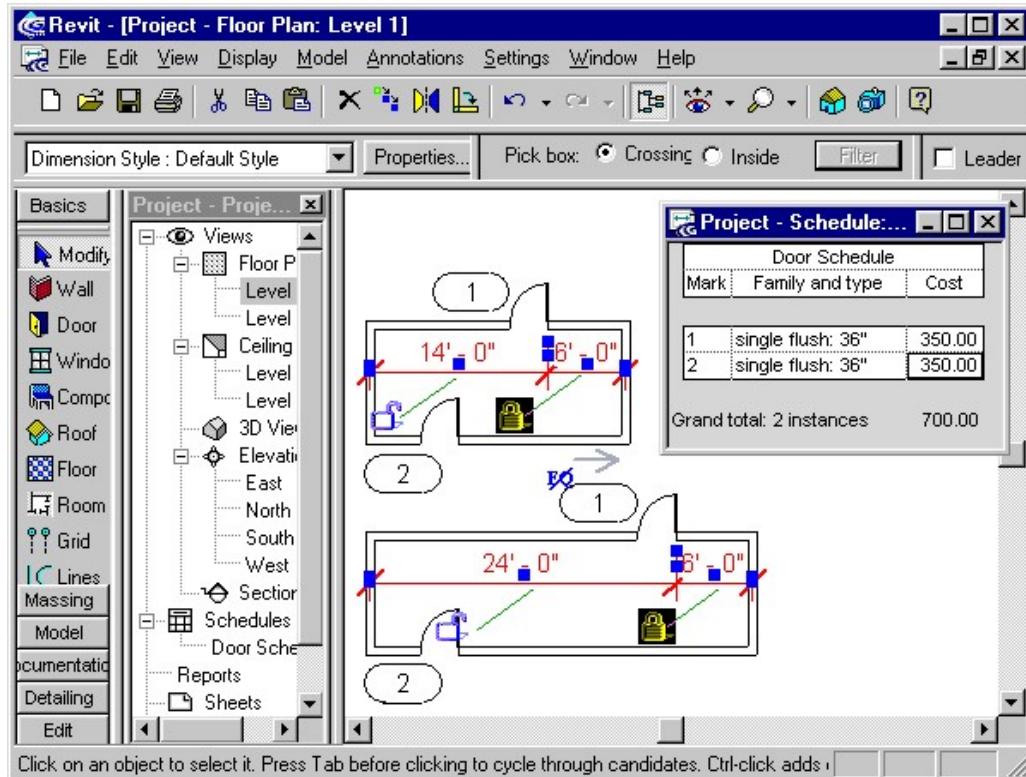


NEWS / OPINIONS / FEATURES / DEALS / HOW-TO / BUSINESS / SUBSCRIBE



ALL REVIEWS

LAPTOPS / TABLETS / PHONES / APPS / SOFTWARE / SECURITY / PRINTERS / CAMERAS / HDTVs



## ENCYCLOPeDIA.

A screenshot of an encyclopedia search interface. At the top is a search bar with a magnifying glass icon and a red 'SEARCH ENCYCLOPEDIA' button. Below the search bar is a grid of letters from A to Z and a 'MISC' button. Underneath the grid, a definition is displayed: 'Definition of: parametric modeling'

[PCMag2014]

*The door in this room has been "locked" to four feet from the right wall. When the wall is dragged to the right to make the room larger, the door maintains its relationship with the wall. This screen shot is in Autodesk Revit, the first parametric building modeler to tie together all component views and annotations parametrically for the A/E/C industry. In addition, the program maintains automatic interaction between graphic and schedule views (note door schedule at right). If either one is changed, its counterpart is updated. (Screen shot courtesy of Autodesk, Inc., [www.autodesk.com](http://www.autodesk.com))*

# Referências

## [HOFFMANN1992]

Christoph M. Hoffmann 1992  
Geometric and Solid Modeling

<https://www.cs.purdue.edu/homes/cmh/distribution/books/geo.html>

## [PCMAG2014]

PC Magazine 2014  
Encyclopedia: Parametric Modeling

<http://www.pc当地.com/encyclopedia/term/48839/parametric-modeling>

## [SHIH2006]

Randy Shih 2006  
Parametric Modeling: The new CAD Paradigm for Mechanical Designs

## [POPOV2009]

Vladimir Popov, Andrej Jarmolajev 2009  
Integrated Design and Analysis Applications for Structural Steelwork and Plant Systems