

---

Vol. [VOL], No. [ISS]: 1–??

# Rendering Tubes from Discrete Curves with Anti-Aliasing and Continuous LOD with Hardware Tessellation

Gustavo Nunes, Alexandre Valdetaro, Alberto Raposo, Bruno Feijo

Pontifical Catholic University of Rio de Janeiro, Dept. of Informatics

Rodrigo de Toledo Federal University of Rio de Janeiro, DCC

**Abstract.** This paper introduces an approach to render 3D tubes using hardware tessellation. The proposed technique explores the new GPU pipeline, hull, tessellator and domain stages, so that the tube mesh can be created in the last possible step inside the pipeline, thereby reducing the bottleneck of the CPU to GPU bandwidth and enabling real time framerates for models with a massive number of tubes. As the proposed solution creates the meshes dynamically, it also enables viewing of the tubes even when the camera is far away from them, without the typical aliasing problem. This approach demonstrates a well balanced solution for 3D tube rendering in CAD applications. We made considerable gains on four major concerns in real time rendering: performance, image quality, simplicity of implementation and memory consumption.

## 1. Introduction

3D tube rendering has many applications. We will illustrate several of these applications through some examples. Visualization of the path taken by particles in time, in the form of streamlines is an appropriate case. Flow simulation is another example of this kind of application [6]. In medicine, there are multiple applications which can make use of tubes, for example visualization of white matter tracts [5] and heart fibrillation [3]. In physics, vector fields can also be viewed as a group of tubes. In the oil industry, tubes can be used in 3D simulations and for representing specific objects, such as wells and risers. This application is the main motivation for our technique (see Figure 1).

3D tubes are represented by a set of points in  $R^3$  and a scalar for its radius. In the conventional graphics pipeline, one needs to construct a polygonal mesh based on this representation before sending it to the GPU. There are also ray-casting approaches of 3D tube rendering, but these have been demonstrated to be too ALU intensive for thousands of tubes and, additionally, they may provide some unwanted artifacts [7]. A basic approach such as rendering the tubes as simple lines is reasonable from a performance point of view, but it lacks in visual quality and suffers with aliasing.

### 1.1. The Problem

We were challenged to represent a massive oil field with wells and ducts as sets of points by using GIS software. Rendering these objects as lines was not an option, as there was a requirement for the tubes to be viewed close up and their size needed to be comparable to other geometry nearby. We started by assigning a designer to create a model for each tube, and we added them as fixed meshes to our scene. Such an approach not only impractical because we constantly needed the designer to create tubes, it also resulted in an unwanted aliasing effect when viewing the tubes from a distance. Also, we always needed to see the tubes, even if they are distant and would not otherwise be rendered. So, we started to develop our current technique. At first, we implemented a technique that could render the 3D tubes from a set of points. The tubes were created in the CPU. Thus, there was no use of tessellators new pipeline. This approach resulted in an intense bottleneck in our visualizer at CPU to GPU bandwidth as we were rendering thousands of ducts, wells and risers. Our tubes were created in the CPU and passed to every frame to the GPU. Also, in CAD applications it can be important to see the 3D tubes, even when the camera is far away from them, so the tubes could not be culled. This requirement resulted in an unwanted aliasing.

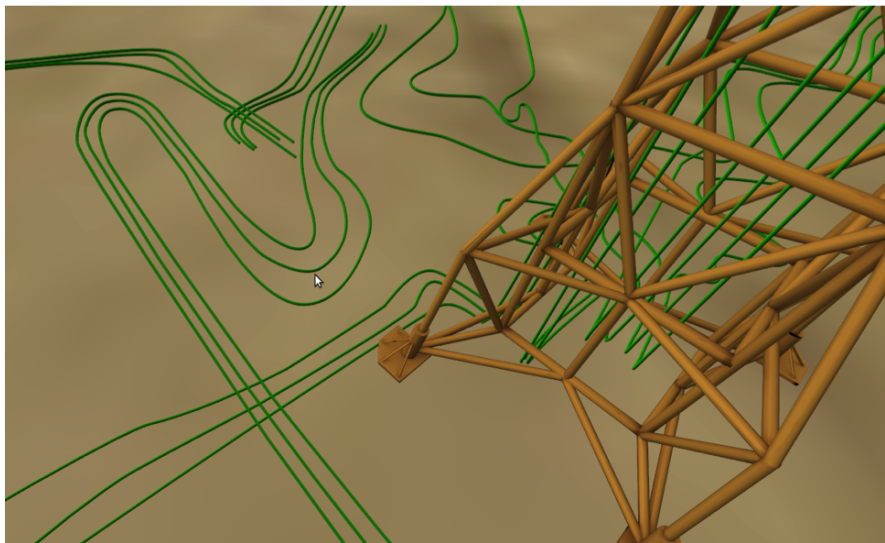
Considering these two main obstacles, bandwidth bottleneck and aliasing, we then developed a new technique to solve these problems. The new so-

Nunes et al: Rendering Tubes from Discrete Curves with Anti-Aliasing and Continuous LOD with Hardware Tessellation3

lution presented successful results for both visual quality and performance benchmarks.

### 1.2. *The Technique*

In this paper, we present the technique behind our new solution. This technique explores the new GPU pipeline, hull, tessellator and domain stages, so that the tube mesh can be created at the last possible step inside the pipeline. In order to achieve such a delay with mesh creation, we consider two ways to construct the 3D tubes from a set of points: they can be either directly connected or used as control points of a spline. In both cases, we only pass a set of points to the GPU, and some per-section auxiliary data (detailed later on), and with this data the mesh can be created. Also, as our solution creates the meshes dynamically, we were also able to solve the aliasing issue. Moreover, our approach exercises every new stage of the programmable pipeline with both clarity and simplicity. Our approach has proven to be a well-balanced solution for 3D tube rendering in CAD applications. We made considerable gains on four major concerns in real time rendering: performance, image quality, simplicity of implementation and memory consumption.



**Figure 1.** 3D tubes rendered with our technique in an oil field visualizer.

## 2. Background

Since GPUs became programmable, there have been many attempts to render 3D tubes more efficiently. Restricted to the first programmable stages (vertex and fragment), some work has used GPU ray casting combined with rasterization [5]; [6]. This technique, also known as extended GPU primitives [7], may present some unwanted artifacts in the case of 3D tubes.

Extended GPU primitives need a supporting rasterized primitive to run the ray casting algorithm, and quadstrips are the natural choice for cylinders. However, in high curvature location, when it is aligned with the viewing angle, quadstrips flip directions, preventing correct ray casting. There are two approaches already proposed in previous work to address this limitation: the use of an extra sprite circle [5] and a locally increased quad-strip resolution [6]. In both cases, an extra pass is necessary to relieve the visual problem. In our work, we have not used any ray cast algorithms and the tubes are solely rendered as polygonal meshes.

In the new GPU pipeline, with hull and domain programmable stages, it is possible to create vertices inside the GPU to accelerate visualization (although the geometry stage could also create vertices on the fly, it is not tailored for massive polygon creation due to low performance of the geometry shader).

There are already some solutions based on real-time vertex generation using the new programmable GPU stages for different applications: terrains [8] and subdivision surfaces [4], but, to the best of our knowledge, those new stages haven't been used to generate tubes in massive models.

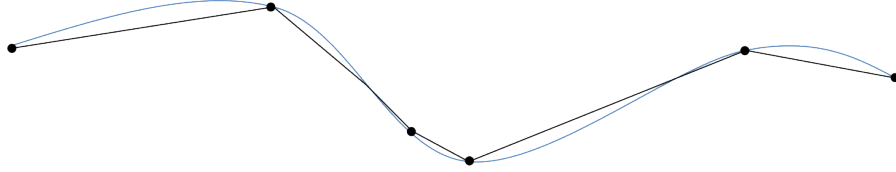
## 3. The Algorithm

The following sections explain the algorithm used in our technique. The workflow is divided in three main parts. In the first, which occurs during a pre-processing phase, we categorize the different kinds of point sequences that can be used as input, and approach them in different ways accordingly. We extract all the necessary data needed to feed the graphics pipeline from this point sequence and move on. In the second part, we create the geometry that will be rendered inside the GPU. In the third part, we then transform the created geometry to a generalized cylinder in world coordinates. We describe these three parts thoroughly in the following sections.

### 3.1. Preparing Data for Rendering

#### 3.1.1. Defining the 3D tubes from Point Sequences

3D tubes are considered generalized cylinders with a constant section area. They are guided by a given curve as its path in 3D space. Our algorithm creates a geometry that reconstructs these generalized cylinders. In order to create the geometry, it is necessary to obtain the sequence of points that define the path. As the points are sequential, we can assume that each point is connected to its neighbors by a straight line segment. Therefore, each point shall have a numerical derivative. However, not every point sequence is a curve representing the actual tube (Blue line in Figure 2). There is still a problem when the point sequence is a mere path that a smooth cylinder should touch. In such situations, we transform the sparse points defining a mere path. We enhance the point sequence precision by smoothly interpolating with Catmull-Rom splines [2] so that the point sequence more precisely defines the central line of the cylinder, as we show in Figure 2. The interpolation increment factor required by the spline decides how many points are going to be generated.

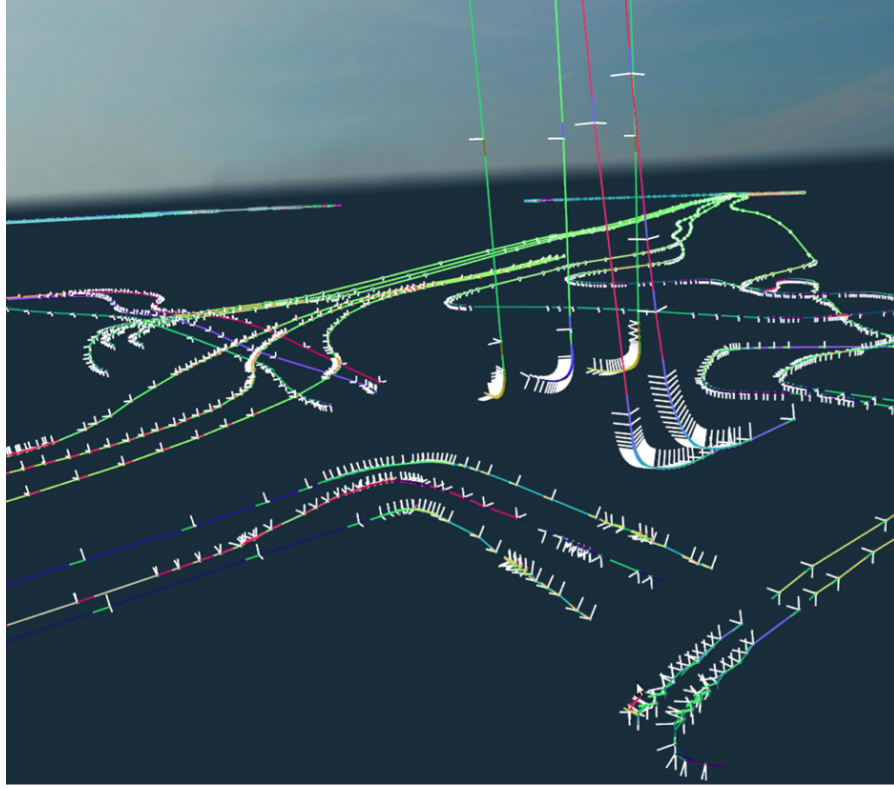


**Figure 2.** A set of points in black representing a tube’s path. In blue the central line of a tube

#### 3.1.2. Making a Good Approximation

Our algorithm approximates a continuous curved generalized cylinder as a discrete set of smaller straight cylinders. Naturally, the point amount enhances the reconstruction precision. Moreover, spots containing high derivative values, such as turns and knees, require more points (Figure 3). However, each point will have a geometry associated with it during the rendering. Thus, we maintain the point amount at a necessary minimum, as seen in Figure 3. The problem is rather simple: we need to cull points that have a low derivative and maintain points with a high derivative. This filter is applied to the internal points by navigating through the point sequence and selecting the relevant points whenever the direction deviation of the curve hits a threshold.

The desired amount of geometry determines the number of selected points. We describe the geometry generation below.



**Figure 3.** Point selection with associated tangent, normal and binormal along a tubes curve. High derivative areas require more points for a precise reconstruction.

### 3.2. *Creating the geometry*

The geometry of the tubes mesh is generated by the tessellator (Section 4), resulting in a very efficient rendering. The CPU-GPU bandwidth is used only to invoke the pipeline and to pass some topological information. As is explained in Section 4, the tessellator can output a set of generated vertices in a chosen domain. We chose a quad topology, thus our vertices fall into a UV  $[0..1]^2$  domain (Figure 4E). The goal is to transform a regular 2D grid and a set of points into a 3D tube. Let us isolate the problem to one single point  $\mathbf{P}_i$  of the curve. For now, consider that our domain is a straight line  $L_i$  (Figure 4F) composed by a discrete set of points  $\{\mathbf{p}_0, \dots, \mathbf{p}_n\}$ . Our objective is to transform  $L_i$  into a circular orthogonal cut of the tube at  $\mathbf{P}_i$  (Figure 4H). In order to convert each point of  $L_i$  to the cross section, we start by transforming every point  $\{\mathbf{p}_0, \dots, \mathbf{p}_n\}$  from 2D line to a point  $\{\mathbf{p}'_0, \dots, \mathbf{p}'_n\}$  in a

3D circle (Figure 4G) on the  $y = 0$  plane by directly transforming the position of  $\mathbf{p}_i$  relative to the total length of  $L_i$  to an angle:

$$\Theta = 2\pi \left( \frac{\mathbf{p}_i}{\mathbf{p}_n} \right) \quad (1)$$

Consider  $\mathbf{p}_i/\mathbf{p}_n$  as the length of  $\mathbf{p}_i$  along  $L_i$ . Now that the points are mapped to a simple circle on  $y = 0$  plane, the problem is to transform this circle to the tubes cross section circle at  $\mathbf{P}_i$ . This transformation is made through a calculation of reference frames along a space curve [1], where the points final position  $\{\mathbf{p}_0'', \dots, \mathbf{p}_n''\}$  (Figure 4H) in world space is:

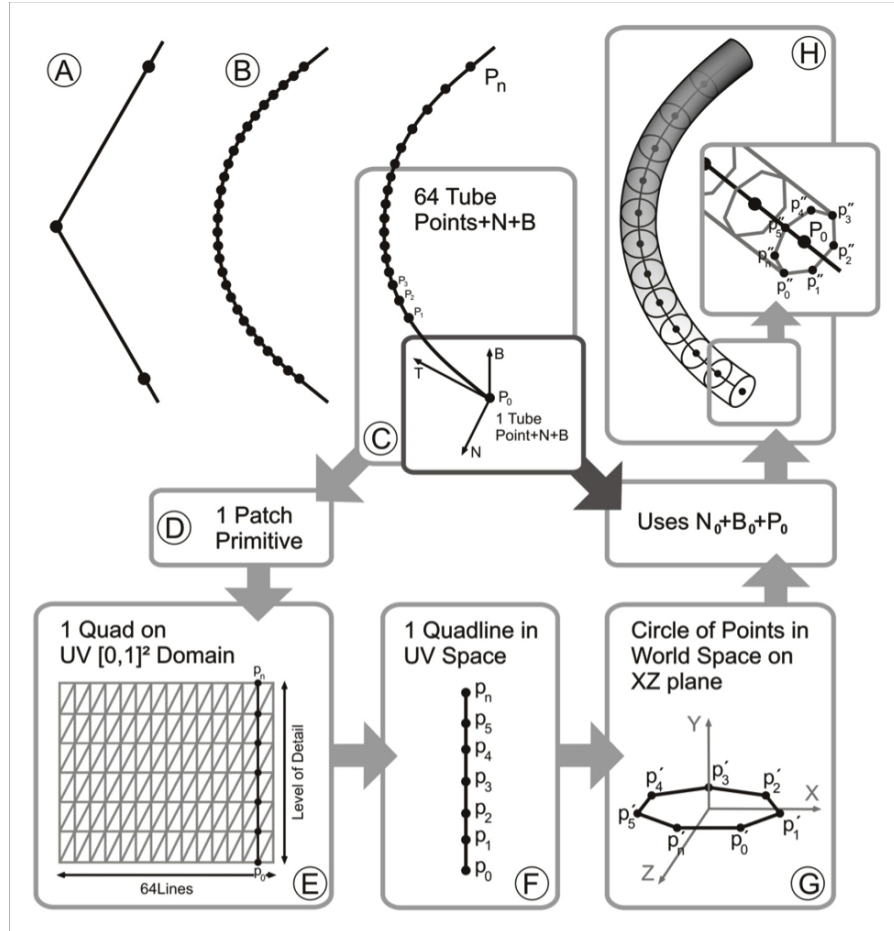
$$\mathbf{F}_p = (\mathbf{P}_{ix} + \mathbf{p}'_x N_x + \mathbf{p}'_z B_x, \mathbf{P}_{iy} + \mathbf{p}'_x N_y + \mathbf{p}'_z B_y, \mathbf{P}_{iz} + \mathbf{p}'_x N_z + \mathbf{p}'_z B_z) \quad (2)$$

Where N and B stand for the Normal and Binormal at  $\mathbf{P}_i$ . Further details are explained at the implementation section. With the algorithm to convert a line to a cross section in world coordinates, there is just a small additional step needed to be able to render a full tube. As the tessellator gives us a 2D regular grid of vertices, we just need to transform every line of the grid to a cross section as described by Figure 4. The circles radius is scaled adaptively, as explained in Section 3.3, but for now we just assume it has a fixed value. In order to use the tessellator as much as possible, our primitive to be transformed in a tube section is a regular grid with 64 lines in one axis, so that every line will be a cross section. As for the other grids axis, there is no fixed number of lines, as this amount of lines will be regulated by the camera distance, resulting in an on-the-fly LOD control. Refer to the next sections for further explanation of these requirements and of the tessellator. The connection between two tube sections (every primitive that represents 64 points) is at a cross section. Moreover, if the amount of points along a cross section differs between two adjacent tube sections, there would be cracks in the rendering. However, as the amount of points in the cross section depends only on the camera distance and both adjacent sections connection point are in the same position, there will be no cracks.

### 3.3. Rendering

#### 3.3.1. Level of detail

The tube geometry is rendered with a simple Level-of-detail technique. As the amount of cross sections along the curve is not supposed to vary, because it could result in a deformation of the tubes path, our LOD technique changes the mesh refinement only on the points along a cross section. The amount



**Figure 4.** A) A raw point sequence. B) The refined point sequence after interpolating with Catmull-Rom spline. C) The selection of relevant points from the sequence and calculation of Tangent Normal and Binormal. D) Every 64 points imply in one patch primitive. E) The patch primitive is a quad domain with 64xLOD lines. F) 1 line from the quad with a number of points determined by the LOD. G) Every line point is first transformed into a circle in 3D space on  $y=0$  plane. H) Using the Normals and Binormals every point is transformed from the circle to a tube cross section.

of geometry is regulated based on the camera distance, we used a simple quadratic function in our implementation. The amount of points may only be restricted to a minimum of 3 points, so the cross section will be a triangle instead of a circle.



### 3.3.2. Reducing the Aliasing

The aliasing effect is expected when rendering a line, as one of its dimensions is many times smaller than the other. Even with a GPU anti-aliasing 16x turned on, the quality can be undesirable (Figure 7). Our approach to reduce aliasing is rather simple, and also very effective. For each point  $\mathbf{P}_i$  of the point set representing the 3D tube we calculate the size of a pixels diagonal in world coordinates at  $\mathbf{P}_i$ s location. If the radius  $r$  of the cross section at  $\mathbf{P}_i$ s location is smaller than a pixels diagonal, we set  $r$  with the pixels diagonal size. This approach combined with the LOD described in the previous section solves the visual problem of aliasing. However, as the radius of the tubes is being changed, the scene will be disproportionately represented; objects near the tubes will seem smaller when viewed from distance. In our renderer, however, the goal is to always view the tubes, as they have a different semantic than the rest of the scene, therefore this disproportion is natural. Nevertheless, if the tubes are supposed to disappear at a given distance, then an alpha correction should be applied alongside with the radius inflation, so there will be no disproportion.

## 4. The Tessellator Pipeline

The first versions of the programmable pipeline were not able to create primitives in the graphics card. In 2006, DirectX 10 capable graphics cards were launched with the Geometry Shader stage. This stage is able to create new primitives in the GPU, but it is not very effective. If one codes a Geometry Shader that adds many primitives in a single call, the performance decreases drastically. In order to solve this issue, hardware vendors added a new tessellator unit to the graphics pipeline see <sup>1</sup>Microsofts Presentation on Tessellation for further information. This new pipeline part has two programmable parts and one fixed but configurable part. We show a diagram of this pipeline in Figure 5. The programmable stages are the Hull Shader and the Domain Shader, while the Tessellator is the only configurable one. Another new concept is the lack of pre-defined topology. It is not specified to the Input Assembler if the incoming vertices are triangles, quads or lines. All primitives are patches. Patches are primitives with no explicit topology, they can be interpreted as triangles, quads, control points for Bezier surfaces or just points that represent some sort of information for the shader programmer. A patch has from 1 to 32 control points. The Hull Shader is responsible for transforming the base of the input patch (e.g. quad Bezier bi-cubic) and also for specifying

<sup>1</sup><http://www.microsoft.com/downloads/en/details.aspx?familyid=2D5BC492-0E5C-4317-8170-E952DCA10D46>

the amount of subdivision for the tessellated domain to the Tessellator. The domain may be quad, triangle or line. The tessellation levels are specified per edge and for the internal part of the domain. This allows for subdividing the surface without cracks at the junctions with other patches. The Tessellator is responsible for creating the vertices within the chosen domain and also for sending the Domain Shader the coordinates (within the range  $[0..1]^2$ ) where the vertices were created. It is Domain Shader’s responsibility to move the created vertices to the correct place in the world.

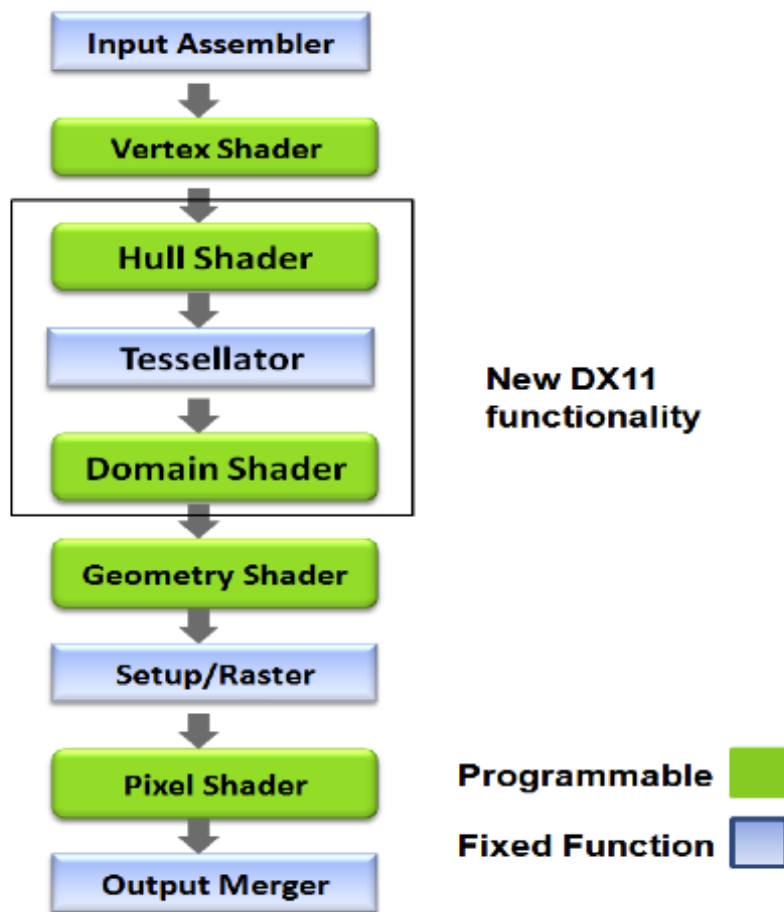


Figure 5. The new Tessellator pipeline

## 5. Implementation

### 5.1. Pre-processing

In order to pass the correct normal, bi-normal and central point information for each tube cross section, we need to execute an  $O(n)$  pre-processing step as explained in Section 3. This information is passed to the GPU as control points information to be used by the domain shader. Each invocation of the tessellator builds a quad that is transformed into a 3D tube part by the domain shader. The tessellator is able to subdivide a quad up to 64 times in each axis. As we demonstrate in Figure 4, one axis of the quad domain has maximum tessellation factor. Each line of this axis is transformed to follow the cross-section defined by the point sequence that represents the tubes path. As we show in Figure 7, the other axis tessellation values are flexible for level of detail values.

### 5.2. Setting up the input assembler

On a quad domain, the tessellator is able to create 64 lines on each axis. In order to make the most of tessellator effort, we should be able to pass 64 different positions, normals and bi-normals to the tessellator for each tessellated quad. But the input assembler only accepts 32 control points per quad. We are able to work this issue around by passing two positions, normals and bi-normals per control point. So, the input assembler is configured to accept a patch with 32 control points, and each of these control points should carry the information needed to correctly position two cross-sections. The following structure snippet shows the information that we need for each control point:

```
struct VS_CONTROL_POINT_INPUT
{
    float3 vPosition    : POSITION;
    float3 vBinormal    : TEXCOORD0;
    float3 vNormal      : NORMAL0;
    float3 vPosition2   : TEXCOORD1;
    float3 vBinormal     : TEXCOORD2;
    float3 vNormal2     : TEXCOORD3;
};
```

These control points are the only vertex buffer per-quad data that our algorithm passes to the GPU. Choosing a quad domain the tessellator is able to create up to 8192 triangles. Also a radius parameter may be optionally passed.

### 5.3. The Constant Hull Shader part

The Hull Shader constant part is the part of the new pipeline where the tessellation factor must be passed to the tessellator. Adaptive tessellation calculations are also made here. The tessellation factor is in the range [1..64]. There are six tessellation factors in the quad domain, four of them are edge factors and two are inside factors (one for each quad axis). Our algorithm transforms each line of the quad domain into a circle, as explained in Section 3. In order to take maximum advantage of the tessellation power, we need to maximize the number of lines in one axis of the quad domain. Consequently, to achieve our objective, we must set the tessellation factor of two edges and one inside axis to 64. This configuration guarantees that we transform the maximum amount of lines into tube sections. The three remaining parameters are varied adaptively in a straightforward Level-of-Detail according to either the distance from camera or edge screen-space size. Moreover, the camera position must be passed as a constant per-frame parameter to the shader. Figure 6 shows the same tube with two different LODs configured by the Hull Shader.

The following code snippet shows our Hull Shader constant part:

```
HS_CONSTANT_DATA_OUTPUT ConstantHS( InputPatch<
    VS_CONTROL_POINT_OUTPUT, INPUT_PATCH_SIZE> ip, uint
    PatchID : SV_PrimitiveID )
{
    HS_CONSTANT_DATA_OUTPUT Output;
    //these factors should be configured according to an
    adaptive tessellation                                //
    parameter(camera or edge screen-space size)
    Output.Edges[0]= Output.Edges[2]= Output.Inside[1] =
    g_fTessellationFactor;
    //maximum tessellator factor for one axis
    Output.Edges[1] = Output.Edges[3] = Output.Inside[0] =
    64;

    return Output;
}
```

### 5.4. The Main Hull Shader

A significant advantage of generating the tube mesh in the GPU is that the radius might be set dynamically. As explained in Section 3.3, with this feature,



**Figure 6.** Left Tube with low LOD. Right Tube with high LOD.

we are able to solve aliasing problems. The Hull Shader main part is executed once per control point, and it is here that we dynamically control the radius of each part of our quad (which will be transformed into a cross section later in the Domain Shader). Let  $\mathbf{P}_i$  be the central point of a cross section as explained above (there are 2 such points per control-point as explained in section 5.2). First we need to find the current depth of  $\mathbf{P}_i$  in screen space. Multiplying  $\mathbf{P}_i$  by the ViewProjection matrix yields  $\mathbf{P}_i$  in screen space ( $\mathbf{P}_{screen}$ ). The depth is obtained dividing the z-coordinate of  $\mathbf{P}_{screen}$  by the w-coordinate of it:

$$\mathbf{P}_{screen} = \mathbf{P} * ViewProjection \quad (3)$$

$$\mathbf{P}_{depth} = \frac{\mathbf{P}_{screenZ}}{\mathbf{P}_{screenW}} \quad (4)$$

For simplicity we assume a canvas with an aspect ratio of 1. Let  $res$  be the resolution of the canvas.  $\mathbf{S}_1 = (0, 0, \mathbf{P}_{depth}, 1)$  and  $\mathbf{S}_2 = (0.5/res, 0.5/res, \mathbf{P}_{depth}, 1)$  represent a pixel width in screen space. Our goal is to find the size of a pixel in world space at the  $\mathbf{P}_{depth}$  depth. Multiplying  $\mathbf{S}_1$  and  $\mathbf{S}_2$  by the inverse of the ViewProjection matrix and dividing by the w-coordinate yields both points in world space. The pixel size in world space is the length of the vector formed by those points:

$$PixelSize_{world} = \left\| \frac{\mathbf{S}_2 * ViewProj^{-1}}{S_{2w}} - \frac{\mathbf{S}_1 * ViewProj^{-1}}{S_{1w}} \right\| \quad (5)$$

The following code snippet shows our Hull Shader main part:

```
[domain("quad")]
[partitioning("integer")]
[outputtopology("triangle_cw")]
[outputcontrolpoints(32)]
[patchconstantfunc("ConstantHS")]
HS.OUTPUT HS( InputPatch<VS.CONTROL_POINT.OUTPUT, 32> p
    ,
    uint i : SV_OutputControlPointID ,
```

```

uint PatchID : SV_PrimitiveID )
{
    HS_OUTPUT Output;
    Output.vPosition = p[i].vPosition;
    Output.vBinormal = p[i].vBinormal;
    Output.vNormal = p[i].vNormal;
    Output.vPosition2 = p[i].vPosition2;
    Output.vBinormal2 = p[i].vBinormal2;
    Output.vNormal2 = p[i].vNormal2;
    float4 pScreen = mul(float4(p[i].vPosition,1),
        g_mViewProjection);
    float pDepth = pScreen.z/pScreen.w;
    float4 S2 = float4(0.5f/res,0.5f/res,pDepth,1);
    float4 S1 = float4(0,0,pDepth,1);
    float4 worldPixel2 = mul(S2,g_mInvViewProjection);
    float4 worldPixel1 = mul(S1,g_mInvViewProjection);
    worldPixel2.xyz = worldPixel2.xyz/worldPixel2.www;
    worldPixel1.xyz = worldPixel1.xyz/worldPixel1.www;
    float PixelDiagonalRadiusWorld = length(worldPixel2
        .xyz - worldPixel1.xyz);

    if(radius <= PixelDiagonalRadiusWorld) radius =
        PixelDiagonalRadiusWorld;
    Output.vRadius = radius;
    return Output;
}

```

### 5.5. The Domain Shader

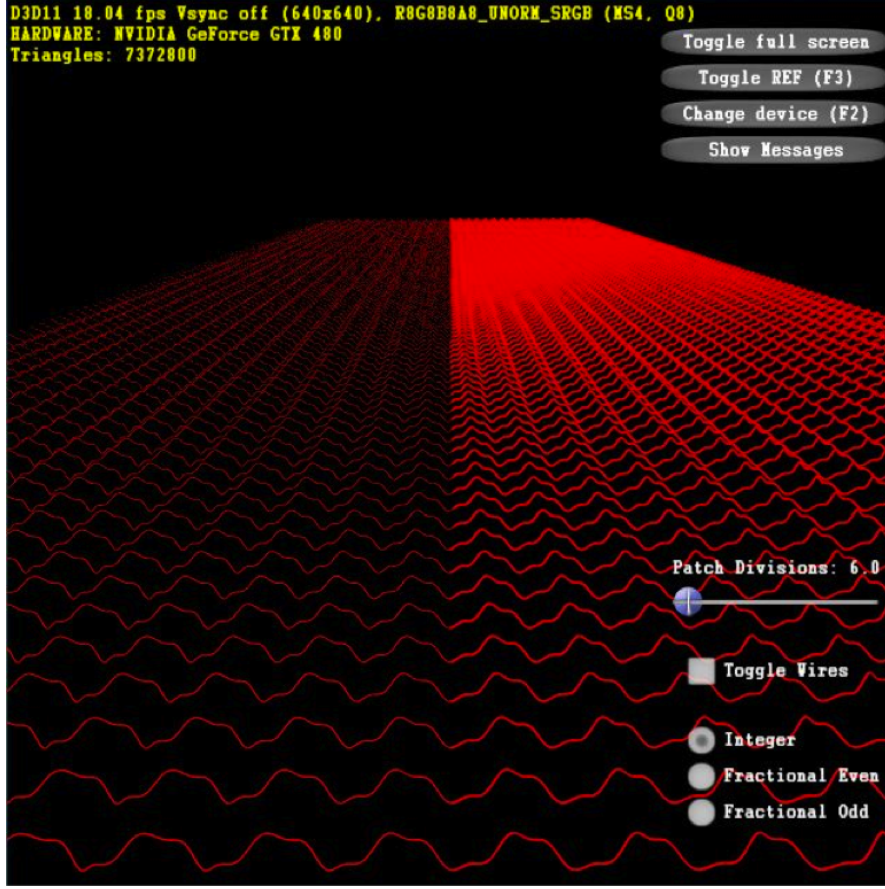
The Domain Shader receives UV coordinates in the  $[0..1]^2$  range. These coordinates specify where, in the quad domain, each new vertex generated by the tessellator is located. Each invocation of the domain shader corresponds to one vertex of the tessellated quad. First, we need to transform each quad line into a circle. Let  $\mathbf{p}'_i$  be a point of one circle in the  $y = 0$  plane and  $r$  is the radius of the tube (the radius comes from the Hull Shader output). The transformation is as following:

$$\Theta = 2\pi V \quad (6)$$

$$\mathbf{p}'_i = (r \cos \Theta, 0, r \sin \Theta) \quad (7)$$

Now the position ( $\mathbf{P}_i$ ), normal ( $\vec{N}$ ) and binormal ( $\vec{B}$ ) must be fetched

Nunes et al: Rendering Tubes from Discrete Curves with Anti-Aliasing and Continuous LOD with Hardware Tessellation 15



**Figure 7.** The Same scene: on the left with 16x GPU anti-aliasing (AA). On the right without GPU AA but with our radius correction AA

from control points data. As each control point has information for two cross sections we must get the right information for each Domain Shader invocation now. We simply multiply the  $U$  coordinate by 63 and do an even/odd choice with the modulus operator.

Now we need to correctly position and orient the tubes cross-section  $\mathbf{C}$ . We convert  $\mathbf{p}'_i$  to  $\mathbf{p}''_i$  according to equation 2. Then,  $\mathbf{p}''_i$  is transformed by the view and projection matrices and is set as one of the Domain Shader outputs.

Another Domain Shader output is the vertex normal,  $\vec{N}_v$ . It can be found easily by the following:

$$\vec{N}_v = (\mathbf{F}_p - \mathbf{P}) / \|\mathbf{F}_p - \mathbf{P}\| \quad (8)$$

The following code snippet shows our Domain Shader:

```
[domain("quad")]
DS_OUTPUT DS( HS.CONSTANT.DATA.OUTPUT input ,
               float2 UV : SV_DomainLocation ,
               const OutputPatch<HS.OUTPUT, 32> p)
{
    DS_OUTPUT Output;
    float v = UV.y;
    float u = UV.x;
    float pi2 = 6.28318530;
    float theta = v*pi2;
    float sinTheta, cosTheta;
    sincos(theta, sinTheta, cosTheta);
    int index = 63*u;
    float3 N,B,P;
    if( index % 2 != 0 )
    {
        index = (int)(index/2.0f);
        N = p[index].vNormal2;
        B = p[index].vBinormal2;
        P = p[index].vPosition2;
    }
    else
    {
        index = (int)(index/2.0f);
        N = p[index].vNormal;
        B = p[index].vBinormal;
        P = p[index].vPosition;
    }

    int radius = p[splineIndex].vRadius;
    float3 C = float3(raio*cosTheta,0,raio*sinTheta);
    float3 worldPos;

    worldPos.x = P.x + C.x*N.x + C.z*B.x;
    worldPos.y = P.y + C.x*N.y + C.z*B.y;
    worldPos.z = P.z + C.x*N.z + C.z*B.z;

    float3 normal = normalize(worldPos -
                              cylinderPos);
```



```

        Output.vPosition = mul( float4(worldPos,1),
                                g_mViewProjection );
        Output.vNormal = normal;
        Output.vWorldPos = float4(worldPos,1);

    return Output;
}

```

## 6. Results

Our tests were executed on an Intel Core i7 920 with a Nvidia GTX480 and 6GB of RAM. We did a comparison between approaches where all the triangles are passed from the CPU to the GPU with the tessellator disabled, versus our GPU tessellation method. No acceleration algorithm such as frustum culling was used. The tests purpose was to measure the efficiency obtained with the trade of memory bandwidth for ALU GPU operations. It is important to note that optimizations are possible with the tessellator pipeline, such as avoiding the subdivision of back faced patches, and tessellating, according to screen-space edge patch size, helps to avoid sub-pixel triangles. In Table 2, we show the results comparing the frame rate with and without our technique. The results show that our algorithm makes significant gains over the non-tessellator based approach. Furthermore, we are capable of accomplishing up to 184 million triangles with interactive frame rates. Using the CPU approach with at least position and normals information per-vertex would result in a prohibitory 13.2GB vertex buffer size to be passed from the CPU to the GPU, while our approach uses only 103.7MB for the same amount of triangles, as illustrated in Table 1. Moreover, our anti-aliasing solution demonstrated to be very effective, with a low frame rate drop against the test with no aliasing treatment. Figure 8 shows our algorithms gain percentage in FPS against a regular approach without anti-aliasing.

## 7. Improving per frame memory consumption even more

The technique explained above is a straightforward and performance balanced method of rendering 3D tubes. Although it is not our case, one might have an even more per frame memory consumer application. Instead of passing all the data (positions, normals, and bi-normals) through the control points, one might use only one control point per quad domain and map a texture with the information of the positions, normals and bi-normals. The single control point per quad would call the position where the texture should be

**Table 1.** FPS comparison for several amounts of triangles.

Millions of Triangles	FPS		
	CPU	Our technique with AA	Our technique without AA
184,3	0	10	11
28,6	1	59	60
12,3	64	102	104
11	71	111	114
9,8	79	124	130
8,6	89	136	147
7,4	99	145	167
6,1	120	178	194
4,9	141	210	231
3,7	181	247	286
2,5	242	320	373
1,2	335	418	500
0,61	518	621	720
0,3	730	835	911
0,12	930	999	1050
0,061	970	1050	1112
0,0061	1100	1111	1135

fetched for the data. This approach would reduce the memory usage by a factor of 64. According to Table 1 and Table 2, this method starts to show some improvement in memory consumption when the 1 million triangles mark is passed. Moreover, above the 20 million mark, this technique provides a strong performance boost.

## 8. Limitations and Drawbacks

### 8.1. Our use scenario

As described in section 1.1, our application was an oil field with lots of ducts, wells and risers. All of them are static lines defined by point sets. We wanted visual quality, without aliasing, and with the tubes visible from any distance. Our technique fit this application well, as we provided good visual quality by having a refined geometry through regulating the LOD according to the camera distance. We also adjusted the tube’s radius so it never disappeared, and there is no noticeable aliasing. The need for a small amount of pre-

**Table 2.** CPU-GPU memory bandwidth comparison

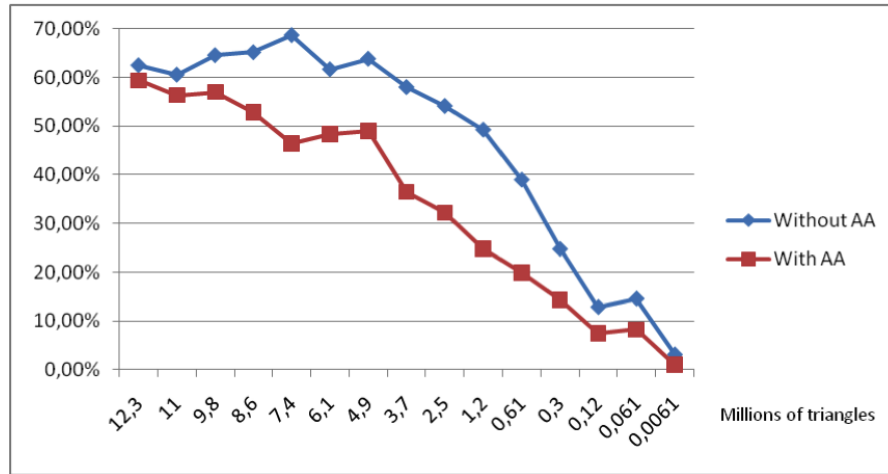
Millions of Triangles	Memory bandwidth in MB	
	CPU	Our technique
184,3	13270	103.7
28,6	2059	16.1
12,3	886	6.9
11	792	6.2
9,8	706	5.5
8,6	619	4.8
7,4	533	4.2
6,1	439	3.4
4,9	353	2.8
3,7	266	2.1
2,5	180	1.4
1,2	86	0.7
0,61	44	0.3
0,3	22	0.2
0,12	9	0.07
0,061	4	0.03
0,0061	0	0.00

processing is a minor drawback that we could not avoid.

## 8.2. Other use scenarios

In a scenario where the point sets are animated through time, our technique may not be suitable. If the points animation is defined by a discrete set of keyframes, and no blending is required, then our technique can be used with a pre-processing of each keyframe. Since our pre-processing is very small, and the amount of data generated is in the same order of magnitude as the point set itself, our technique might provide a good solution. However, if there is a continuous animation by a time function or interpolation, then our technique cannot be applied.

In most of the scenarios, different from our case, the tubes should be culled with the distance. In such cases, the minimum radius of the tube should not be arbitrary and fixed so that the tube cross section occupies 1 pixel. Also, the tubes transparency should increase proportionally to the radius correction. The transparency should reach maximum when the tube is supposed to be culled by the distance. If this transparency regulation is not used, there will be



**Figure 8.** Graph showing the percentage gain in FPS of this algorithm with and without AA against a CPU approach without AA

a disproportion effect between the tubes and the rest of the geometry nearby when viewed from far away.

### 8.3. Older Hardware

The main limitation of our technique is that it is only compatible with DirectX 11/OpenGL 4 video cards. One might think of implementing it through Geometry Instancing for support of older cards. It works to a degree, but there are issues with the rasterizer performance. Level-of-Detail control through Geometry Instancing is not as flexible as with the new pipeline, and if the application starts to create too many sub-pixel triangles, the rasterizer acts as the main bottleneck of the program due to overshading.

**Acknowledgments.** This work is funded by Petrobras, Brazilian Oil & Gas Company. Alberto Raposo also thanks FAPERJ for the individual support granted (#E-26/102.273/2009).

### References

- [1] Jules Bloomenthal. Graphics gems. In Andrew S. Glassner, editor, *Graphics gems*, chapter Calculation of reference frames along a space curve, pages 567–

Nunes et al: Rendering Tubes from Discrete Curves with Anti-Aliasing and Continuous LOD with Hardware Tessellation21

571. Academic Press Professional, Inc., San Diego, CA, USA, 1990.
- [2] E. Catmull and R. Rom. A class of local interpolating splines. *Proc. of International Conference on Computer Aided Geometric Design*, pages 317–326, 1974.
- [3] Polina Kondratieva, Jens Krüger, and Rüdiger Westermann. The application of gpu particle tracing to diffusion tensor field visualization. In *Proceedings IEEE Visualization 2005*, 2005.
- [4] Charles Loop, Scott Schaefer, Tianyun Ni, and Ignacio Castaño. Approximating subdivision surfaces with gregory patches for hardware tessellation. *ACM Trans. Graph.*, 28:151:1–151:9, December 2009.
- [5] Dorit Merhof, Markus Sonntag, Frank Enders, Christopher Nimsky, Peter Hatreiter, and Guenther Greiner. Hybrid visualization for white matter tracts using triangle strips and point sprites. *IEEE Transactions on Visualization and Computer Graphics*, 12:1181–1188, September 2006.
- [6] Carsten Stoll, Stefan Gumhold, and Hans-Peter Seidel. Visualization with stylized line primitives. In *IEEE Visualization*, page 88. IEEE Computer Society, 2005.
- [7] Rodrigo Toledo and Bruno Levy. Extending the graphic pipeline with new gpu-accelerated primitives. In *International gOcad Meeting, Nancy, France*, 2004. Also presented in Visgraf Seminar 2004, IMPA, Rio de Janeiro, Brazil.
- [8] Alexandre Valdetaro, Gustavo Nunes, Alberto Raposo, Bruno Feijo, and Rodrigo de Toledo. Lod terrain rendering by local parallel processing on gpu. *Games and Digital Entertainment, Brazilian Symposium on*, 0:182–188, 2010.